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**Abstract:** This manuscript describes the operation of a droop-based controller for three-phase converters in the case of the absence of a neutral connection to the grid. The controller is capable of output power tracking and smooth transitions into the islanded operation. While independent per-phase control of the converter output power is possible if a neutral connection is present, its absence implies additional constraints to be considered. Focusing on this latter case, the controller described herein allows the independent control of the active power at the output of each phase of the converter and a smooth transition to the islanded operation. These features are paramount in future smart power systems, such as smart microgrids, for implementing demand–response, power-flow management, and uninterrupted power operation.

**Keywords:** converter control; droop control; grid-tied inverters; microgrids; power control; unbalanced power control

# 1. Introduction

Microgrids integrating distributed energy resources connected to the AC grid by means of electronic power converters (EPCs) should support a number of features [1,2]. The capability of flexibly controlling the exchanged active and reactive power, that is, the output power control, and the capability of islanded operation are some of the important functionalities in scenarios such as the one represented in Figure 1. Output power control is crucial for the implementation of demand–response and for unbalanced compensation in three-phase systems [3,4]. Islanded operation is crucial to make the microgrid subsystem resilient against the adverse events affecting the main power system [5].



**Figure 1.** Microgrid scenario in which distributed electronic power converters (EPCs) track defined power references and are capable of sustaining the operation of the microgrid in case of disconnection from the upstream grid (i.e., islanding). The control of  $3\phi$ -3w EPCs is considered herein.

Solutions such as the per-phase power control in [6] limited to three-phase four-wires (i.e.,  $3\phi$ -4w) systems allow the control of the output power of grid-connected inverters and



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). also permit their transition to the islanded operation. Considering other relevant solutions described in the literature, such as [7–10], the per-phase control can harmoniously integrate multiple merits, in terms of (i) independent output power control for each phase of a three-phase four-wire grid-connected inverter, (ii) smooth transitions into the islanded operation mode, (iii) operation in islanded conditions, even when multiple parallel-connected EPCs integrating the proposed controller are present. The solution described herein integrates the features indicated above and, in addition, it allows operation in case of the absence of a neutral connection, that is, in  $3\phi$ -3w systems. This latter configuration is relevant in low-voltage grid scenarios, as shown in some European low-voltage distribution benchmarks [11], and also considered in recent research papers in the field, such as [12–14].

To highlight the features of the presented solution, a comparison with other control approaches is given in Table 1. Grid-feeding converters, for example, require the presence of the main grid or, in order to operate in an islanded microgrid of other voltage-forming units [15]. Traditional droop control using P-f and Q-V droop laws allows islanded operation; however, the regulation of the total active and reactive power (i.e., power tracking) during grid-tied operation is achievable only by control adaptations, as shown in [14,16,17]. In [17], indicated as a droop with a  $3\phi P\&Q$  track in Table 1, the tracking of the total three-phase inverter output power and a smooth transition to the islanded operation is achieved and shown; however, per-phase power regulation is left unexplored. In fact, it is impossible to independently impose droop laws on each phase, as this would result in different frequencies at the different phases of the three-phase system. The approach analyzed herein allows all the functionalities reported above and indicated in Table 1, but it was exclusively presented in [6] and only restricted to the case of three-phase four-wire (i.e.,  $3\phi$ -4w) networks.

Table 1. Comparison with other approaches.

Control Kind	Islanded Operation	Grid-Tied/ Island. Trans.	Three-Phase Power Tracking	Power Tracking	3φ-4w & 3φ-3w Operation
Grid feeding	-	-	+	+	+
Traditional droop	+	+	-	-	+
Droop with $3\phi P \& Q$ track	+	+	+	-	+
Per-phase control in [6]	+	+	+	+	-
Technique proposed herein	+	+	+	+	+

While operation with a neutral connection is of significant importance and gives full flexibility for output power control [10,18–20], the case *without a neutral connection* is still of interest and can be commonly found in grid-tied applications [21–23]. For this latter case originally considered herein, the independent, phase-by-phase control of the output active and reactive power, which results in six variables in total, is not possible, and only a subset of the output powers can be controlled instead. As shown here, four variables can be controlled in three-wire systems and exploited, for example, for balancing distributed power or for control needs of local distribution system operators or microgrid controllers [24,25], as recommended in modern microgrid standards [26].

This manuscript discusses and proposes the per-phase power control of three-phase inverters without a neutral connection to the grid, as displayed in the representative configuration in Figure 2. This kind of operation without neutral connections has been foreseen in [6], anticipating the need for dedicated studies and discussions for this extension, which are then presented in this study. Specifically, in Section 2, the basics of active and reactive power flow are overviewed for both three-phase four-wire and three-phase three-wire systems, highlighting the additional constraint and related reduced control flexibility present in this latter case. The per-phase power control for three-phase three-wire systems proposed herein is then described in Section 3. Section 4 demonstrates the behavior of the control in a couple of practical conditions. Finally, Section 5 concludes the paper.



**Figure 2.** An electronic power converter (EPC) connected to a three-phase low-voltage network *without* a neutral connection (i.e., three-phase three-wire connection,  $3\phi$ -3w) whose per-phase output power control is proposed in this study.

#### 2. Basics of Power Control

2.1. Three-Phase Four-Wire (3φ-4w) Networks

The power exchange of a single-phase inverter connected to the grid is now considered, which is helpful as a preliminary analysis for setting the nomenclature and overviewing some key relations. Assume  $V_i \angle \varphi_i$  is the phasor of the inverter output voltage, and  $V_g \angle 0$  is the grid voltage phasor. Considering Thevenin's inverter model, namely, a voltage generator with its equivalent series impedance, connected to the grid, the equations describing the flow of the active power and the reactive power among the two equivalent generators can be derived. Assuming the grid frequency  $\omega = 2\pi f$ , the interconnection impedances being mainly inductive, and small voltage and phase differences, the following linearized relations yield [27,28]:

$$P \simeq \gamma_p \varphi_i , \quad Q \simeq \gamma_q \left( V_i - V_g \right),$$
 (1)

with  $\gamma_p := V_g^2/\omega L$  and  $\gamma_q := V_g/\omega L$ . Such relations hold for each of the phases of a  $3\phi$ -4w connection. In this case, there is no interdependence between the phases, which means that the output power at a phase does not affect the output powers measured at the other phases. This is not the case in  $3\phi$ -3w connections, which are addressed herein.

# 2.2. Three-Phase Three-Wire $(3\phi-3w)$ Networks

Consider the  $3\phi$ -3w connection of Figure 3 with the indicated nomenclature for voltage phasors. In this case, fully independent power control is not physically possible; that is, the power exchanged by one generator is affected by the phase and voltage differences imposed by the others, which is the neutral point voltage  $\bar{V}_N = -(\bar{V}_a + \bar{V}_b + \bar{V}_c)/3$ , under the hypothesis of a symmetric grid voltage.



Figure 3. Thevenin model of a grid-tied three-phase three-wire inverter.

The linearized relations (1) derived from the model in Figure 3 yield:

$$S = M \cdot \Theta \tag{2}$$

where vectors  $S = [P_a, P_b, P_c, Q_a, Q_b, Q_c]^T$  and  $\Theta = [\varphi_a, \varphi_b, \varphi_c, \Delta V_a, \Delta V_b, \Delta V_c]^T$ , with  $\Delta V_x = V_x - V_{gx}$ , and M the matrix defined as

$$M = \frac{1}{6} \begin{bmatrix} 4\gamma_p & \gamma_p & \gamma_p & 0 & \sqrt{3}\gamma_q & -\sqrt{3}\gamma_q \\ \gamma_p & 4\gamma_p & \gamma_p & -\sqrt{3}\gamma_q & 0 & \sqrt{3}\gamma_q \\ \gamma_p & \gamma_p & 4\gamma_p & \sqrt{3}\gamma_q & -\sqrt{3}\gamma_q & 0 \\ 0 & -\sqrt{3}\gamma_p \sqrt{3}\gamma_p & 4\gamma_q & \gamma_q & \gamma_q \\ \sqrt{3}\gamma_p & 0 & -\sqrt{3}\gamma_p & \gamma_q & 4\gamma_q & \gamma_q \\ -\sqrt{3}\gamma_p \sqrt{3}\gamma_p & 0 & \gamma_q & \gamma_q & 4\gamma_q \end{bmatrix}$$
(3)

The rank of  $M \in \mathbb{R}^{6\times 6}$  is four, which is the number of variables that can be regulated arbitrarily. On this basis, for a  $3\phi$ -3w connection, it is not possible to regulate all of the six active and reactive powers of the phases a, b, and c at the same time, as it is possible with a  $3\phi$ -4w connection instead [6]. A possible choice of variables to be controlled for output power tracking may be  $P_a$ ,  $P_b$ ,  $Q_a$ ,  $Q_b$ , or, equivalently,  $P_a$ ,  $P_b$ ,  $P_c$ ,  $Q_{3\phi} = \sum Q_x$ . This latter option is considered herein, yielding

$$\begin{bmatrix} P_a \\ P_b \\ P_c \\ Q_{3\phi} \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 4\gamma_p & \gamma_p & \gamma_p & 0 \\ \gamma_p & 4\gamma_p & \gamma_p & 0 \\ \gamma_p & \gamma_p & 4\gamma_p & 0 \\ 0 & 0 & 0 & 18\gamma_q \end{bmatrix} \cdot \begin{bmatrix} \varphi_a \\ \varphi_b \\ \varphi_c \\ \Delta V \end{bmatrix}$$
(4)

To avoid the control actions related to homopolar components, which are not controlled by using this approach, such components can be removed by processing the voltage measurements with a decoupling matrix (such as the one used in (8)).

# 3. Per-Phase Power Control in Three-Phase Three-Wire Systems

The block diagram of the proposed controller is displayed in Figure 4. On the top, a P-f droop relation processes the total three-phase power  $P_{3\phi}$  exchanged at the inverter output and provides the phase  $\varphi_{3\phi}$ , which is the integral of the angular frequency given by the droop characteristic:

$$\omega^* = \omega_0 + k_{p,3\phi} \left( P_{3\phi}^* - P_{3\phi} \right)$$
(5)



**Figure 4.** Per-phase power controller. As shown at the top, synchronization branch provides a reference angle  $\varphi_{3\phi}$  to the three phases, represented by the generic symbol *x* (i.e., *a*, *b*, *c*). The angle and amplitude of each phase are adjusted for per-phase power control. The resulting references *V* sin  $\varphi_x$  are given to EPC current and voltage regulators (zero-level control) for output voltage control.

In this way, the droop-controlled converter can synchronize to the grid voltage, keeping the known synchronization characteristics of the P-f droop, as shown, for example, in [29]. The top branch in Figure 4 is referred to as the synchronization branch in the following. Then, two different behaviors are established: grid-connected and islanded operation.

# 3.1. Grid-Connected Operation

During a grid-connected operation, output power tracking is possible due to the presence of the main grid [30]. The total  $P_{3\phi}^*$  is adjusted using a three-phase power regulator:

$$H_{3\phi}^{\mathrm{p}}(s) = \frac{h_{i,3\phi}^{\mathrm{p}}}{s} \tag{6}$$

whose output  $P_{3\phi}^*$  modifies the total three-phase output power of the inverter, by shifting the droop characteristic (5).

To achieve the output power tracking of controllable quantities  $P_a$ ,  $P_b$ ,  $P_c$ , and  $Q_{3\phi}$ , the obtained  $\varphi_{3\phi}$  is then adjusted phase-by-phase, as displayed by the central blocks in Figure 4 referring to the generic *x*-th phase. Here a proportional-integral controller denoted as

$$H_{x}^{p}(s) = h_{p,x}^{p} + \frac{h_{i,x}^{p}}{s}$$
(7)

produces the phase shift  $\Delta \varphi_x$  that adds to the instantaneous three-phase angle  $\varphi_{3\phi}$  and allows the phase power  $P_x$  to follow the respective reference power  $P_x^{\text{ref}}$  during grid-tied operation. In order to decouple the balanced active power control and unbalanced power control, making the first component relevant only to the top, the synchronization loop, it is possible to use a decoupling matrix *T* to remove the balanced terms from the per-phase control loop. The matrix can be defined as follows:

$$T = \begin{bmatrix} 2/3 & -1/3 & -1/3 \\ -1/3 & 2/3 & -1/3 \\ -1/3 & -1/3 & 2/3 \end{bmatrix}$$
(8)

Finally, the total delivered output reactive power is adjusted by acting on the amplitude of the generated three-phase voltages, using the following regulator:

$$H_{3\phi}^{q}(s) = \frac{h_{i,3\phi}^{q}}{s} \tag{9}$$

### 3.2. Islanded Operation

During islanded operation, the generated and dissipated power must be exactly equal within an islanded subsystem; then, a transition into islanded operation makes output power control no more possible and automatically leads the power regulator  $H_{3\phi}^{\rm p}$  into saturation. Consistently, the integral part of the per-phase regulator  $H_x^{\rm p}$  is also disabled. The saturation limits  $P_{3\phi}^{*\max}$ , or  $P_{3\phi}^{*\min}$  can be designed as discussed in [6]. Remarkably, during the islanded mode of operation, the controller behaves as a traditional droop controller, through which the converter frequency  $\omega^*$  changes linearly with the total delivered three-phase power:

$$\omega^* = \omega_0 + k_{p,3\phi} \left( P_{3\phi}^{*\text{sat}} - P_{3\phi} \right) \tag{10}$$

where  $P_{3\phi}^{*sat}$  is a constant saturation limit, namely,  $P_{3\phi}^{*max}$  or  $P_{3\phi}^{*min}$ . In the same way, the reactive power controller  $H_{3\phi}^{q}$  also saturates

$$V = V_0 + k_{q,3\phi} \left( Q_{3\phi}^{*sat} - Q_{3\phi} \right) \tag{11}$$

leading the control to operate as a traditional droop scheme with a smooth transition to the islanded operation.

As a final remark, even though some fundamental relations such as (6), (7), (9), and (10) are also used for control with  $3\phi$ -3w systems, the characteristics of the control problem highlighted in (2) and the controller organization derived from (4) and discussed by referring to Figure 4 require substantial modifications on the control scheme presented for  $3\phi$ -4w systems in [6], which can not be used in the case of the absence of neutral wires.

# 4. Validation Results

The proposed controller was tested with simulation and by means of a laboratoryscale experimental prototype implementing the system in Figure 2. The system parameters related to the EPC hardware and control are listed in Table 2. The control technique in Figure 4 was deployed in a B-Box controller manufactured by Imperix Ltd., through which the EPC controller was implemented. The EPC hardware was implemented by using three modules PEB8032 manufactured by Imperix Ltd., and the grid voltage was generated by using a three-phase voltage source implemented with three additional modules of the same type. A photo of the used experimental setup is displayed in Figure 5.



**Figure 5.** Photo of the experimental setup used to validate the proposed approach implementing the configuration displayed in Figure 2.

Parameter	Symbol	Value
EPCs parameters		
DC-link voltage	$V_{dc}$	350 V
DC-link capacitor	$C_{dc}$	3.3 mF
DC-link inductor	$L_{dc}$	2.5 mH
Output filter capacitor	$C_{f}$	50 µF
Output filter inductor	$L_{f}$	1.5 mH
Switching frequency	$f_{sw}$	20 kHz
Nominal power rating	$S_N$	3 kVA
Nominal grid voltage rms	$V_{q}^{nom}$	110 V
Nominal grid frequency	$\omega_g^{nom}$	$2\pi \cdot 50 \text{ rad/s}$
Main grid frequency range	$\omega_g^{\min}, \omega_g^{\max}$	$2\pi \cdot [49.9, 50.1] \text{ rad/s}$

Table 2. Inverters (EPCs) and control parameters.

Parameter	Symbol	Value
control parameters		
<i>P</i> – <i>f</i> droop coefficient	$k_{p,3\phi}$	0.209 mHz/W
V–Q droop coefficient	$k_{q,3\phi}$	0.917 mV/VAr
3-phase P contr. integ. gain	$h_{i,3\phi}^{\rm p}$ 1/s	
3-phase P saturation limit	$P_{3\phi}^{*sat}$	$\pm 6 \text{ kW}$
Per-phase <i>P</i> contr. integ. gain	$h_{i,x}^{\rm p}$	0.628 mrad/Ws
Per-phase <i>P</i> contr. prop. gain	$h_{p,x}^{\mathbf{p}'}$	49.867 μrad/W
3-phase $Q$ contr. integ. gain	$h_{i,3\phi}^{q}$	16.26 1/s
Per-phase $Q$ saturation limit	$Q_{3\phi}^{*sat}$	$\pm 6$ kVAr
Nominal voltage amplitude	$V_0$	$\sqrt{2} \cdot 110 \text{ V}$
Nominal frequency	$\omega_0$	$2\pi \cdot 50 \text{ rad/s}$
Maximum frequency variation	$\Delta \omega_g^{\max}$	$0.4~\%~\omega_0$
Maximum voltage variation	$\Delta V_g^{max}$	10 % V <sub>0</sub>

Figures 6 and 7 display the most significant experimental waveforms to show the chief features of the control. The instantaneous three-phase voltages and currents are reported in subfigure (a), while subfigure (b) displays the related active power  $P_a$ ,  $P_b$ , and  $P_c$  and reactive power  $Q_{3\phi}$ , the voltage amplitudes deviation  $\Delta V$ , the frequency deviation  $\Delta \omega^*$ , and the phase displacement with respect to the first phase (i.e.,  $\varphi_b^* - \varphi_a^*$  and  $\varphi_c^* - \varphi_a^*$ ). The results are discussed next.



File Edit Utžity Help Waveform View	$P_{a,b,c}^{\text{ref}} = 11$	kW	$P_{a,b}^{ref} =$	$1 \text{ kW}, P_c^{\text{ref}}$	$= 0 \mathrm{kW}$	Tektron
150 W/div 0 W		1.0 kW				$P_a$
150 W/div 0 W		1.0 kW				$P_b$
150 W/div 0 W		1.0 kW				$P_c$
50 VAr/div		~~~~~			G	$2_{3\phi}$
800 mV/div		4.8 V		[ 4.0 V	Δ	$\Delta V$
					Δ	ω*
10 mHz/div						-16 mi -20 mi
9 15 mDeg/div		-90 mdeg			$\varphi_b^*$ –	$\varphi_a^*$
■ 60 mDeg/div		-360 mde	\$		$\varphi_c^*$ –	$\varphi^*_a {\scriptstyle {}^{\scriptscriptstyle 40} \atop {}^{\scriptscriptstyle 4$
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		(b)				

**Figure 6.** Experimental results with EPC in Figure 2 implementing the proposed control scheme in Figure 4: (**a**,**b**) reference step change  $P_a$ ,  $P_b$ ,  $P_c^{\text{ref}} : 0 \rightarrow 1 \text{ kW} @ 0 \text{ s}$  and  $P_c^{\text{ref}} : 1 \rightarrow 0 \text{ kW} @ about 3 \text{ s}$  while connected to the grid.

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1.0 A/div			i <sub>out,c</sub>		
Ch1         Ch2         Ch3         Ch4         Ch5         Ch4           50 Weiw         50 Weiw         50 Weiw         1 Addir         1 Addir         1 Addir           6         %         %         %         %         1 Addir         1 Addir         1 Addir           21892         %         2 kHz         %         2 kHz         %         2 kHz         %		7 8 Add Add Add Horizontal 7 8 March New New Stationard Statistics March Bart Data Statistics 4	s Soundst Control Strategy of		
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40 W/div	270 W				$P_c$	200.5 200.5 120.5 40.5 -40.5
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1.5 V/div	] 9.0 V				$\Delta V$	16.5 7.5 4.5 1.5 4.5
200 mHz/div	-1.4 Hz				$\Delta \omega^*$	-200 mil -600 mil -1 10 -1 4 H
o 5 mDeg/div				$\varphi_b^*$	$-\varphi_a^*$	15 mDe 15 mDe -15 mDe -25 mDe 18 mDe
5 mDeg/div				$\varphi_c$	$-\varphi_a$	9 De -15 mbe -26 mbe
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**Figure 7.** Experimental results with EPC in Figure 2 implementing the proposed control scheme in Figure 4: (**a**,**b**) transition into the islanded operation with a balanced local load connected.

### 4.1. Balanced and Unbalanced Power Reference Variations

Figure 6a,b show the response of the system to a power reference step change. Specifically, the response to a balanced reference step change  $P_a$ ,  $P_b$ ,  $P_c: 0 \rightarrow 1$  kW is shown first. Then, a subsequent transient is displayed in which phase-*c* is solely subject to a reference change  $P_c$  : 1 kW  $\rightarrow$  0, making the system's operation unbalanced. The total requested reactive power reference is kept fixed at zero. Figure 6b demonstrates the expected transient in terms of active and reactive power, with zero steady-state tracking errors. As expected, during balanced power reference tracking, phase displacements  $\varphi_h^* - \varphi_a^*$  and  $\varphi_c^* - \varphi_a^*$  are not affected by balanced power references, as they are the necessary phase-shift to allow the desired active power exchange the same in the three phases and included in variations in the instantaneous phase  $\varphi_{3\phi}$  related to the integral of the shown  $\Delta \omega^*$ . Moreover, in this transient, the decoupling matrix T in (8) prevents any reaction of the per-phase control loops involving  $P_x$ . Some voltage variations  $\Delta V$  can be noticed as a secondary effect, due to the residual resistive components of the interconnection impedance between the inverter and the grid of the experimental setup. The following unbalanced transient  $P_c: 1 \,\mathrm{kW} \rightarrow 0$  stimulates the reaction of the per-phase control loops, which introduces the required phase deviation  $\varphi_c^* - \varphi_a^*$  in order to allow the unbalance power flow at phase-*c*. Due to the decoupling matrix T, which prevents the per-phase loops from regulating balanced power terms, variation in the resulting total power and balanced power stimulates the response of the synchronization loop too. This results in a transient variation in the instantaneous frequency  $\omega^*$ , which gives the instantaneous phase  $\varphi_{3\phi}$  and a corresponding further adjustment of  $\varphi_b^* - \varphi_a^*$ .

## 4.2. Transition of Grid-Tied to Islanded Operation

Figure 7a,b show the response of the system to a sudden disconnection from the main grid, namely, a transition to the islanded operation. In this test, the local load is balanced,

composed of three 50- $\Omega$  resistors in parallel with three 50- $\mu$ F capacitors, star-connected at the output of the inverter. At the opening of the circuit breaker *CB*, in Figure 2, the proposed controller is capable of maintaining the local voltage, without any discontinuity in the supply of the load. Due to the absence of the main grid, ensuring the balance between power generation and absorption, i.e., power tracking, makes the active and reactive power regulators deviate toward the set saturation limits. Notably, this does not impact the quality of the supplied voltage, producing voltage deviations  $\Delta V$  and frequency deviations  $\Delta \omega^*$ that are within tolerable limits by design. Based on the parameters in Table 2, the range of the operating frequency of the islanded microgrid falls within 49.7–50.3 Hz [17].

Commonly, in droop control, static P-f characteristics are also represented. The trajectory on the P-f plane during the considered transition to the islanded operation is displayed in Figure 8. Some representative points are reported: *A* corresponds to the operation during grid-connected operation, *B* and *C* are points during the transition toward the islanded operation mode, and *D* is the point of operation during the islanded mode. The speed of change in the operating point during the transition, which is explicit in the representation of quantities in the time domain in Figure 7, is qualitatively indicated in Figure 8 in the colored trajectory, from fast, shown in red, to slow, shown in blue.



**Figure 8.** Representation of the trajectory on the f-P plane during the transition shown in Figure 7, with total equivalent load in islanded operation of 800 W. Colored dashed lines indicate the limits (10). The speed of change in operating point is qualitatively indicated in color on the trajectory: fast changes in red and slow changes in blue.

### 4.3. Example of Application

The proposed approach allows the transition to the islanded operation and also allows power tracking during grid-tied operation, which was experimentally verified in the previous section. An example of a practical application of the latter feature of output power tracking is now further demonstrated by simulation results in Figure 9, in which the objective is to provide unbalanced power compensation at the interface with the main grid, in scenarios such as those outlined in the introduction (see, for example, Figure 1). In general, power control and the capability of allowing distributed unbalanced compensation are the available ancillary services within modern electricity grids [1,2,12].



**Figure 9.** Example of application: unbalanced compensation at the interface with the main grid: (a) currents at the interface with the main grid with related total rms currents in (b); (c) active powers phase-by-phase at the interface with the grid with related average.

This is shown in Figure 9 considering the unbalanced compensation in the configuration in Figure 2, where an unbalanced load is locally connected. The load consists of a 20  $\Omega$  resistive load connected between phase *a* and phase *b*. A grid impedance of 100 m $\Omega$ is considered. Initially, the per-phase power references are equal to zero, so the grid is completely supplying the unbalanced load. At *t* = 2 s, the inverter received new power reference signals, in order to compensate for the unbalance. These references may be computed, for example, using a higher-level control layer implementing grid services, as contemplated in Figure 1 and envisioned in recent studies such as [2,12,25]. Notice that the total active power supplied by the inverter is still zero, but now the per-phase power is such that the unbalance component of the load is entirely supplied by the inverter; thus, the current absorbed by the grid becomes a balanced current. The total rms current at the interface with the grid significantly reduces owing to the control, which is beneficial considering grid losses and stresses.

# 5. Conclusions

In this study, a controller achieving output power reference tracking at the phases of inverters connected to three-phase three-wire electrical systems was described and demonstrated. In three-phase three-wire systems, it is not possible to independently control the active and reactive power of all three phases of the converter; thus, a suitable control scheme is required to accommodate the requirements of power flow control, which are crucial in advanced power systems and the limited degrees of freedom due to the absence of neutral wires. In addition, the capability of maintaining uninterrupted operation in case of disconnection from the main grid is also of paramount importance in microgrids. The experimental validation showed that the proposed controller succeeds in harmoniously integrating phase-by-phase output power tracking and the capability of a smooth transition to the islanded operation.

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