

Building gas rings and rejuvenating S0 galaxies through minor mergers

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ABSTRACT

We investigate the effects of minor mergers between an S0 galaxy and a gas-rich satellite galaxy, by means of N -body/smoothed particle hydrodynamics simulations. The satellite galaxy is initially on a nearly parabolic orbit and undergoes several periapsis passages before being completely stripped. In most simulations, a portion of the stripped gas forms a warm dense gas ring in the S0 galaxy, with a radius of ~ 6 –13 kpc and a mass of $\sim 10^7 M_{\odot}$. The ring is generally short-lived ($\lesssim 3$ Gyr) if it forms from prograde encounters, while it can live for more than 6 Gyr if it is born from counter-rotating or non-coplanar interactions. The gas ring keeps memory of the initial orbit of the satellite galaxy: it is corotating (counter-rotating) with the stars of the disc of the S0 galaxy, if it originates from prograde (retrograde) satellite orbits. Furthermore, the ring is coplanar with the disc of the S0 galaxy only if the satellite’s orbit was coplanar, while it lies on a plane that is inclined with respect to the disc of the S0 galaxy by the same inclination angle as the orbital plane of the satellite galaxy. The fact that we form polar rings as long-lived and as massive as co-planar rings suggests that rings can form in S0 galaxies even without strong bar resonances. Star formation up to $0.01 M_{\odot} \text{ yr}^{-1}$ occurs for >6 Gyr in the central parts of the S0 galaxy as a consequence of the interaction. We discuss the implications of our simulations for the rejuvenation of S0 galaxies in the local Universe.

Key words. galaxies: interactions – methods: numerical – galaxies: kinematics and dynamics – galaxies: star formation – galaxies: ISM

1. Introduction

A large fraction of S0 galaxies (~ 20 –25%, Laurikainen et al. 2013) show signatures of rings (i.e. closed structures composed of stars, gas and dust) and pseudo-rings (incomplete versions of rings, sometimes formed by arm-like structures, Comerón et al. 2014). Far ultraviolet (FUV) observations frequently evidence rings and pseudo-rings of gas and/or young stars in early-type galaxies (ETGs), and especially in S0 galaxies (Thilker et al. 2007; Salim & Rich 2010; Salim et al. 2012). Salim & Rich (2010) analyse 22 ETGs with an extended ultraviolet (UV) morphology in GALEX data, and find rings in 15 of them. Salim et al. (2012) investigate a sample of ETGs at $z < 0.1$, 27 of which have been observed with the *Hubble* Space Telescope (HST) in FUV. These ETGs are UV structured, showing ring and/or arm-like structures, while in the optical they have an old stellar disc, i.e. they are S0 galaxies. The UV emission is consistent with a low-level galaxy-scale star formation (SF) of $\sim 0.5 M_{\odot} \text{ yr}^{-1}$.

Rings in S0 galaxies are found at different distances from the galaxy nucleus, often connected to the presence of bars/see e.g. Aguerri et al. 2009; Laurikainen et al. 2013). Such kind of rings are often classified, depending on their distance from the nucleus, as (i) nuclear rings (surrounding the nucleus of the galaxy); (ii) inner rings (generally surrounding the bar, if present); and (iii) outer rings (more external than the former ones).

The origin of the rings is still debated. The fact that many rings are associated with bars (or other non-axisymmetric structures) has led to the idea that the formation of rings is connected

with resonances induced by the rotation of the bar (i.e. either an inner Linblad’s resonance, or an outer Linblad’s resonance, or a ultraharmonic resonance, Binney & Tremaine 1987; Buta & Combes 1996). However, a resonance cannot be invoked for the outer polar rings (e.g. Marino et al. 2009), as well as for the most asymmetric and off-centre rings (e.g. Thilker et al. 2010). In addition, bars should be more common than observed in S0 galaxies ($\sim 30\%$, Aguerri et al. 2009) to explain the large fraction of ringed S0 galaxies found in Salim & Rich (2010).

Alternative scenarios to a bar-driven resonance include gas-rich minor or major mergers, and accretion from filaments/clouds of intergalactic medium. Mergers and gas accretion from filaments are the only models able to explain the most massive polar rings (Bekki 1998; Iodice et al. 2002, 2006; Moiseev et al. 2011; Spavone et al. 2010, 2011; Spavone & Iodice 2013). Evidences of gas accretion either from filaments or from interactions with gas-rich satellite galaxies have been found in a large number of galaxies (e.g. de Blok et al. 2014; Serra & Oosterloo 2010; see Sancisi et al. 2008 for a review). Similarly, the analysis of a large sample of disc galaxies in the Sloan Digital Sky Survey reported by Kaviraj (2014a) suggests that minor mergers played a major role in driving SF in galaxy discs (see also Kaviraj 2010, 2014b; Kaviraj et al. 2012, 2013). Numerical simulations also indicate the importance of minor mergers for the accretion of fresh gas in ETGs (e.g. Kaviraj et al. 2009; Peirani et al. 2010). Finally, Marino et al. (2011) investigate five S0 galaxies with outer rings in UV (NGC 1533, NGC 2962, NGC 2974, NGC 4245, and NGC 5636). While all the considered galaxies are barred and

the rings might be related to bar-induced resonances, there are several indications that NGC 1533, NGC 2962 and NGC 2974 have accreted gas from satellite galaxies. Thus, [Marino et al. \(2011\)](#) hypothesize that the outer rings in their sample are an effect of (bar-driven) secular evolution, but at the same time this process was aided by fresh gas accreted from gas-rich satellites. Using N -body/smoothed-particle hydrodynamics (SPH) simulations with chemo-photometric implementation, [Mazzei et al. \(2014\)](#) showed that the pseudo-ring in NGC 1533 and its star forming properties may be a transient phase during a major merger episode involving two halos with mass ratio 2:1.

In this paper, we study the formation of gas rings in S0 galaxies, by means of N -body/SPH simulations of minor mergers with small gas-rich companions. In Sect. 2, we describe the adopted numerical techniques. In Sect. 3 we present our results, with particular attention for the formation of co-planar and polar gas rings. In Sect. 4 we discuss the main implications of our results, while in Sect. 5 we summarize our conclusions.

2. Method: N -body simulations

We simulate interactions between a primary S0 galaxy and a secondary gas-rich galaxy. The initial conditions for both the primary galaxy and the secondary galaxy in the N -body model are generated by using an upgraded version of the code described in [Widrow et al. \(2008\)](#); see also [Kuijken & Dubinski 1995](#) and [Widrow & Dubinski 2005](#)). The code generates self-consistent disc-bulge-halo galaxy models, derived from explicit distribution functions for each component, which are very close to equilibrium. In particular, the halo is modelled with a Navarro et al. (1996, NFW) profile. We use an exponential disc model ([Hernquist 1993](#)), while the bulge is spherical and comes from a generalization of the Sersic law ([Prugniel & Simien 1997](#); [Widrow et al. 2008](#)).

Both the primary and the secondary galaxy have a stellar bulge and a stellar disc. The giant S0 galaxy has no gas, whereas the secondary galaxy has an initial gas mass of $1.38 \times 10^8 M_\odot$, distributed according to an exponential disc. Therefore, the initial configuration of the secondary galaxy is consistent with a low-mass gas-rich disc galaxy. The assumption that the primary has no gas is quite unrealistic, but allows us to easily distinguish between the triggering of SF in the pre-existing gaseous disc of the S0 galaxy and the effect of fresh gas accretion from the companion galaxy.

The total mass of the secondary is $\sim 1/20$ of the mass of the primary, classifying the outcome of the interaction as a minor merger. The masses of the various components and the scale lengths of the simulated galaxies are listed in Table 1. Table 2 shows the orbital properties (impact parameter, relative velocity, orientation angles and total energy) of the six runs. The adopted orbits are nearly parabolic (Table 2), in agreement with predictions from cosmological simulations ([Kochfar & Burkert 2006](#)). The main implication of such nearly parabolic orbits is that the stripping of the satellite galaxy proceeds slowly: the merger is not yet complete in most simulations at $t = 11$ Gyr since the first periaxis passage.

In all the simulations, the particle mass in the primary galaxy is $2.5 \times 10^5 M_\odot$ and $5 \times 10^4 M_\odot$ for dark matter (DM) and stars, respectively. The particle mass in the secondary galaxy is $2.5 \times 10^4 M_\odot$ for DM and $5 \times 10^3 M_\odot$ for both stars and gas. The softening length is $\epsilon = 100$ pc.

We simulate the evolution of the models with the N -body/SPH tree code gasoline ([Wadsley et al. 2004](#)). Radiative cooling, SF and supernova blastwave feedback are enabled, as

Table 1. Initial conditions of the N -body simulations: masses and scale lengths.

Model galaxy properties	Primary	Secondary
M_{DM} ($10^{11} M_\odot$)	7.0	0.3
M_* ($10^{10} M_\odot$)	7.0	0.2
$f_{\text{b/d}}$	0.25	0.25
M_{G} ($10^8 M_\odot$)	0	1.38
R_s (kpc)	6.0	3.0
R_d (kpc)	3.7	3.0
h_d (kpc)	0.37	0.30
r_B (kpc)	0.6	0.6

Notes. M_{DM} is the DM mass; M_* is the total stellar mass of the galaxy (including both bulge and disc); $f_{\text{b/d}}$ is the bulge-to-disc mass ratio; M_{G} is the total gas mass. The primary has no gas, while the gas of the secondary is distributed according to an exponential disc ([Hernquist 1993](#)), with the same parameters (scale length and height) as the stellar disc. R_s is the NFW scale radius $R_s \equiv R_{200}/c$, where R_{200} is the virial radius of the halo ([Navarro et al. 1996](#)) and c the concentration (here we assume $c = 12$ for both galaxies). R_d and h_d are the disc scale length and height, respectively ([Hernquist 1993](#)), while r_B is the bulge scale length.

described in [Stinson et al. \(2006, 2009\)](#); see also [Katz & Rix 1992](#)). The adopted parameters for SF and feedback are the same as used in recent cosmological simulations capable of forming realistic galaxies in a wide range of masses (e.g., [Governato et al. 2010](#); [Guedes et al. 2011](#)), and in recent simulations of galaxy-galaxy collisions ([Mapelli & Mayer 2012](#); [Mapelli et al. 2012, 2013a,b](#)).

In runs A and B the orbit of the satellite galaxy is co-planar with the disc of the S0 galaxy. The only difference between run A and B is that the orbit of the satellite galaxy is retrograde and prograde (i.e. the orbital angular momentum of the satellite is counter-aligned and aligned with respect to the spin of the primary galaxy) in run A and B, respectively (Table 2). Run A, C and D differ for the inclination angle between the relative velocity vector \mathbf{v}_{rel} and the symmetry axis of the primary disc (θ , see Table 2): $\theta = -\pi/2$, $-\pi/4$ and 0 for run A, C and D, respectively. This means that the orbit of the satellite galaxy is inclined by 45° and 90° with respect to the disc of the primary galaxy in run C and D, respectively.

In runs E (retrograde) and F (prograde), the impact parameter (30 kpc) is a factor of 3 larger than in run A. In all simulations, the primary galaxy develops a strong bar ~ 200 Myr after the beginning of the simulation. Our galaxy models are marginally stable against the formation of a bar: evolving the galaxy in isolation, the bar does not appear. The perturbation induced by the interaction with the intruder satellite galaxy plays an important role in the formation of the bar.

3. Results

Figure 1 shows the radial distance of the satellite galaxy from the centre of the primary galaxy for all simulations, as a function of time (in this figure and in the following, time $t = 0$ corresponds to the first periaxis passage). From this figure, we can derive information about the periaxis passages. The impact parameter is extremely important to determine the amount of tidal disruption of the satellite at the first periaxis passage, and the subsequent orbital decay. In fact, the orbital decay is slower in the two runs with the largest impact parameter: in 10 Gyr, the satellite undergoes only 2 and 3 periaxis passages in runs E and F,

Table 2. Initial conditions of the N -body simulations: orbital properties.

Run	b (kpc)	v_{rel} (km s $^{-1}$)	θ, ϕ, ψ (rad)	E_s (10^4 km 2 s $^{-2}$)	L_s (10^3 km s $^{-1}$ kpc)	e	Orbit spin
A	10.0	200	$-\pi/2, 0, 0$	0.38	2.0	1.003	retrograde
B	10.0	200	$\pi/2, 0, 0$	0.38	2.0	1.003	prograde
C	10.0	200	$-\pi/4, 0, 0$	0.38	2.0	1.003	–
D	10.0	200	$0, 0, 0$	0.38	2.0	1.003	–
E	30.0	200	$-\pi/2, 0, 0$	0.38	6.0	1.03	retrograde
F	30.0	200	$\pi/2, 0, 0$	0.38	6.0	1.03	prograde

Notes. b and v_{rel} are the impact parameter and the relative velocity between the centres of mass (CMs) of the two galaxies at the initial distance, respectively. For the definition of θ, ϕ, ψ , see Fig. 1 of Hut & Bahcall (1983). In particular, θ is the angle between the relative velocity vector v_{rel} and the symmetry axis of the primary disc, ϕ describes the orientation of v_{rel} projected in the plane of the primary disc and ψ describes the orientation of the initial distance vector \mathbf{D} (between the CMs of the two galaxies) in the plane perpendicular to v_{rel} . E_s is the specific orbital energy, i.e. the total energy divided by the reduced mass $\mu = m_1 m_2 / (m_1 + m_2)$, where m_1 and m_2 are the mass of the primary and of the secondary galaxy, respectively. $E_s \equiv -GM/D + v_{\text{rel}}^2/2$, where $M = m_1 + m_2$ is the total mass of the two galaxies, G is the gravitational constant and D the initial distance between the CMs. L_s is the modulus of the specific orbital angular momentum, i.e. the angular momentum divided by the reduced mass. e is the eccentricity ($e = [1 + 2E_s L_s^2 / (GM)^2]^{1/2}$). An orbit is classified as prograde/retrograde depending on the alignment/counter-alignment of the orbital angular momentum of the secondary galaxy with respect to the spin of the primary galaxy.

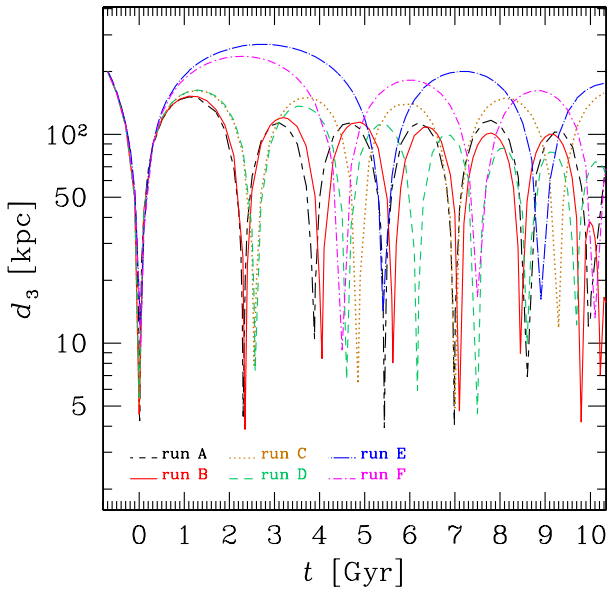


Fig. 1. Radial distance of the satellite galaxy from the centre of the primary galaxy for all simulations, as a function of time. Time $t = 0$ corresponds to the first periapsis passage. Long-short dashed black line: run A; solid red line: run B; dotted ochre line: run C; dashed green line: run D; long-dash-dotted blue line: run E; short-dash-dotted magenta line: run F.

respectively. In the other runs, the satellite undergoes between 4 and 8 periapsis passages in 10 Gyr. Generally, the orbital decay is faster for prograde satellites (runs B and F) than for their retrograde analogs (runs A and E): tidal disruption occurs faster in prograde encounters, because of the lower relative velocity between the stars of the primary galaxy and the gas and stars of the secondary galaxy (Toomre & Toomre 1972).

3.1. The gas rings

At each periapsis passage, gas and stars are stripped away from the satellite galaxy, and remain bound to the primary galaxy. In some runs, a portion of the stripped gas settles into a warm gas ring ($T \sim 10^4$ K), with an average radius of ~ 6 – 13 kpc. Figure 2 shows the total mass of stripped gas that resides in the inner 15 kpc of the primary galaxy ($M_{\text{g, in}}$), as a function of

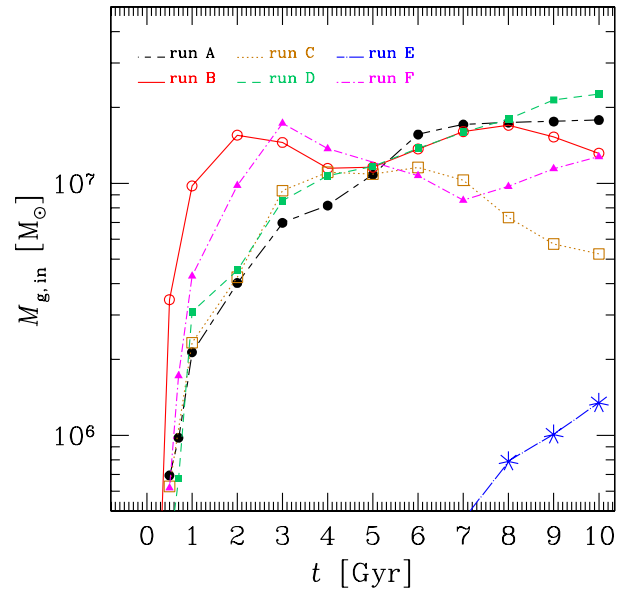


Fig. 2. Mass of the gas that lies in the inner 15 kpc of the S0 galaxy ($M_{\text{g, in}}$) for all simulations, as a function of time. Time $t = 0$ corresponds to the first periapsis passage. Long-short dashed black line and filled black circles: run A; solid red line and open red circles: run B; dotted ochre line and open ochre squares: run C; dashed green line and filled green squares: run D; long-dash-dotted blue line and blue asterisks: run E; short-dash-dotted magenta line and filled magenta triangles: run F.

time. By definition, $M_{\text{g, in}}$ includes all the gas that lies in the inner 15 kpc of the S0 galaxy, including diffuse hot gas, the gas that is funnelled in the nucleus of the galaxy, and the gas that is confined into the ring. $M_{\text{g, in}}$ becomes non-negligible ($\geq 2 \times 10^6 M_{\odot}$) soon after the first periapsis passage ($t \sim 0.5$ – 1.0 Gyr) in all simulations apart from run E. In run E (retrograde and with a large impact parameter), gas stripping starts only in the last Gyrs. In all simulations apart from run E, $M_{\text{g, in}}$ reaches a maximum value of 1 – $2 \times 10^7 M_{\odot}$ (i.e. $\sim 1/10$ of the total gas mass of the satellite galaxy). From Fig. 2, we also notice that the peak value of $M_{\text{g, in}}$ is reached earlier in the prograde runs (run B and F) than in the retrograde runs (runs A and E) and in the non-coplanar runs (runs C and D). This confirms that gas stripping is more

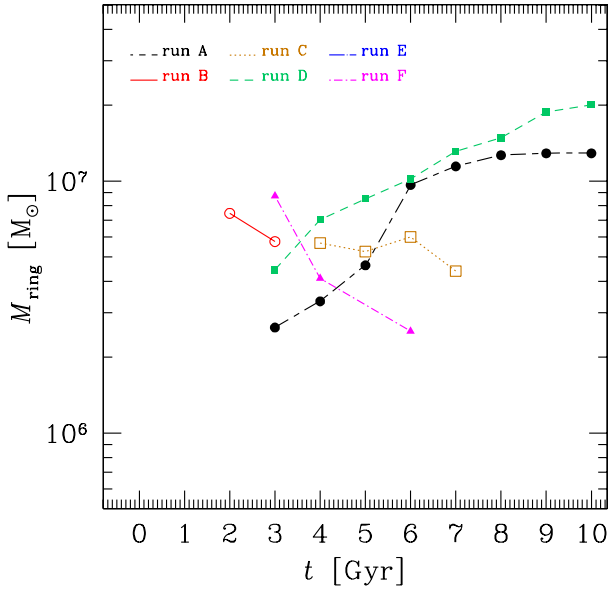


Fig. 3. Mass of the gas ring (M_{ring}) for all simulations, as a function of time. Time $t = 0$ corresponds to the first periapsis passage. Long-short dashed black line and filled black circles: run A; solid red line and open red circles: run B; dotted ochre line and open ochre squares: run C; dashed green line and filled green squares: run D; short-dash-dotted magenta line and filled magenta triangles: run F.

efficient in the prograde runs. The fact that retrograde runs and non-coplanar runs behave in a similar way is remarkable.

Figure 3 shows the total mass of stripped gas that is confined in a gas ring (M_{ring}), as a function of time. During the ring’s life, the value of M_{ring} spans from 20% to 90% of $M_{\text{g, in}}$, depending on the run. From Fig. 3, it is apparent that the formation of a ring, its survival, and the amount of mass that is locked into the ring strongly depend on the characteristics of each run. In some runs, the ring never forms (run E), or is relatively short-lived (1–3 Gyr, runs B, C and F), while in other runs the ring grows steadily and is long-lived (>7 Gyr, runs A and D).

In run A (Fig. 4) a co-planar ring of gas forms in the disc of the S0 galaxy at $t \sim 3$ Gyr, i.e. approximately after the second periapsis passage. The ring has a radius of ~ 8 – 10 kpc, which means that it forms just at the end of the stellar bar, but is counter-rotating with respect to the disc, because it keeps memory of the retrograde orbit of the satellite. The ring in run A is extremely long-lived: it survives for the entire simulation (Fig. 3). In contrast, a gas ring forms earlier (at $t \sim 2$ Gyr) in run B (the prograde analogous of run A), is co-rotating with the stellar disc, and survives only for ~ 1 Gyr (Fig. 3). The main reason for the early disappearance of the ring in run B is that most of the gas is channelled inwards by the bar, and ends up in the nucleus.

The fact that the radius of the ring coincides almost with the size of the bar in runs A and B might lead to the conclusion that the ring is the consequence of a bar-driven resonance. On the other hand, rings form even in runs C and D (Fig. 5), in which the orbit of the satellite is inclined by 45 and 90° with respect to the disc of the primary galaxy, respectively. Actually, it seems that the ring preserves the inclination of the orbit of the satellite with respect to the primary galaxy, as the gas ring of run C and D forms with an inclination of ~ 45 and $\sim 90^\circ$ with respect to the disc of the primary galaxy. In particular, the gas ring of run D is a true polar ring, and cannot be produced by a bar-driven resonance. The ring of run D grows steadily in mass and survives till the end of the simulation. The radius of the ring

in both run C and D is ~ 12 – 13 kpc, slightly larger than in the other runs.

The fact that the ring has approximately the same orientation as the initial satellite orbit is consistent with our expectations: no dynamical process (e.g. bar-driven resonance, differential precession) is sufficiently efficient to perturb the initial orbit of gas and stellar streams within a few Gyr, if the satellite’s orbit has a large inclination. Even shocks and virial heating (e.g. Keres et al. 2005) are partially inefficient for our systems, given the lack of gas in the halo of the S0 galaxy. Finally, Theis et al. (2006) find that spiral arm-like perturbations might develop in a polar ring surrounding a S0 galaxy, but these perturbations are confined in the initial plane of the polar ring. We warn that our results are valid only for spherical halos. A triaxial halo is expected to exert torques, and to induce warps and tilts in the stellar disc (e.g. Sparke 1984; David et al. 1984; Steiman-Cameron et al. 1984; Nelson & Tremaine 1995; Dubinski & Chakrabarty 2009). Such effects might perturb a polar gas ring significantly.

Furthermore, our findings are consistent with previous studies which investigate the formation of polar rings from the disruption of gas-rich satellite galaxies (e.g. Richter et al. 1994; Mazzei et al. 2014). In particular, there is consensus that the initial plane of the ring is the orbital plane of the companion if this is promptly destroyed (e.g. Katz & Rix 1992; Thakar & Ryden 1996; Eliche-Moral et al. 2011). The initial ring plane might then evolve to a preferred plane (either the equatorial or a polar plane) on a timescale longer than the orbital or azimuthal smearing time (i.e. several Gyr, e.g. Rix & Katz 1991; Cox & Sparke 1996, see also Struck 1999, and references therein). Based on a sample of 78 polar ring galaxy candidates, Smirnova & Moiseev (2013) recently proposed that the DM halo and the stellar bar are crucial to stabilize outer and inner polar rings, respectively. This is fairly consistent with our results, which suggest that the formation of the ring is not due to bar-driven resonance, but the bar and the DM halo contribute to stabilize the ring, and make it long-lived.

In both runs E (retrograde) and F (prograde) the orbit of the satellite is co-planar with the disc of the primary galaxy. The main difference with runs A and B is that the periapsis passage is 3 times larger in runs E and F. Only in run E does no significant ring form over the duration of the simulation ($t \sim 10$ Gyr), because the periapsis distance of the satellite is too large and the relative velocity too high to produce significant stripping.

In run F, which is the prograde analogous to run E, a ring forms already at $t \sim 3$ Gyr since the first periapsis passage (Fig. 3). This confirms that gas stripping is much more efficient if the satellite orbit is prograde. Despite the larger periapsis with respect to the other runs, the ring of run F forms again at the end of the stellar bar, with a radius of ~ 10 – 12 kpc. The ring of run F disappears quite fast ($t \sim 6$ Gyr). This result is analogous to what we already discussed for run B: in the prograde runs the ring appears earlier than in the retrograde ones, but disappears earlier.

3.2. The long-lived gaseous and stellar halo

A considerable fraction of the initial stellar and gaseous mass of the satellite galaxy is scattered into the halo of the S0 galaxy, as a consequence of the encounter. Figure 6 shows the total mass of stars ($M_{*, \text{out}}$) and gas ($M_{\text{g, out}}$) that was initially bound to the satellite galaxy and that, at time t , lies at a distance > 50 kpc both from the centre of the S0 galaxy and from the centre of the satellite galaxy. In our definition of $M_{*, \text{out}}$ and $M_{\text{g, out}}$, we exclude all stars and gaseous particles that lie at a distance < 50 kpc from both the nucleus of the S0 galaxy and the satellite galaxy,

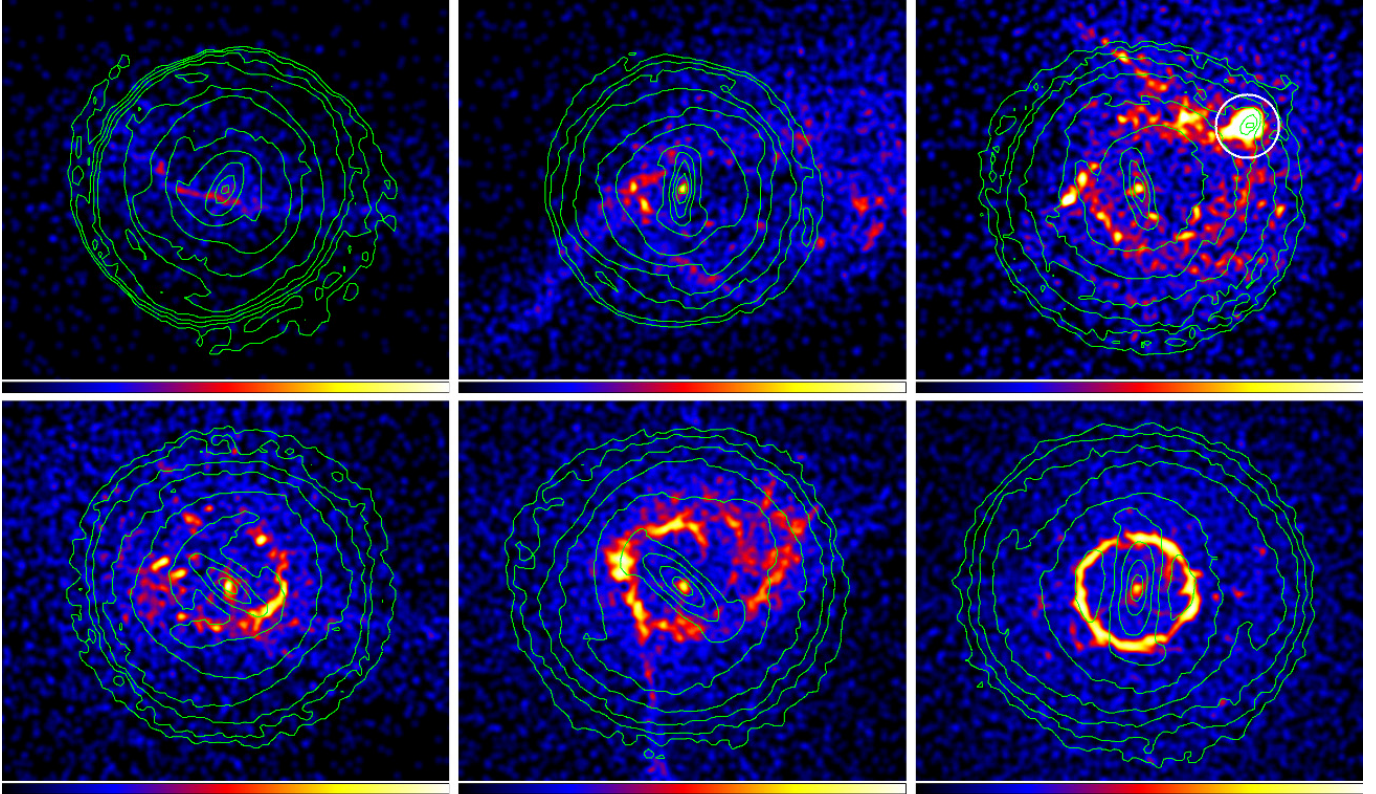


Fig. 4. Projected density of gas (logarithmic colour-coded map) and stars (isocontours) of the primary galaxy in run A. From top left to bottom right: 1, 2, 2.35, 3, 5, and 7 Gyr after the first periapsis passage. Each panel measures 79×67 kpc. In the top right-hand panel, the white circle marks the position of the nucleus of the satellite galaxy, ~ 50 Myr after the second periapsis passage.

because we want to estimate the mass of the diffuse stellar and gaseous halo, which forms as an effect of the tidal encounter (a distance of 50 kpc is a conservative limit, to exclude matter that is still in the disc of the S0 galaxy or that can be re-accreted by the satellite galaxy).

From Fig. 6 it is apparent that $M_{*,\text{out}}$ and $M_{\text{g,out}}$ grow very fast after the first periapsis passage (the only exception being run E). After the first Gyr, $M_{*,\text{out}}$ and $M_{\text{g,out}}$ remain almost constant, or keep growing slowly, till the end of the simulation. Thus, the first periapsis passage plays a major role in the formation of the stellar and gaseous halo. Furthermore, the halo is extremely long-lived. At the end of the simulation (10 Gyr after the first periapsis passage), $\sim 70\text{--}95\%$ of the stars initially bound to the satellite galaxy lie in the stellar halo of the S0 galaxy (including the case of run E). Similarly, $\sim 60\text{--}80\%$ of the gas initially bound to the satellite galaxy ends up in the gaseous halo of the S0 galaxy at $t = 10$ Gyr. The only exception is run E, where $M_{\text{g,out}}$ is only $\sim 30\%$ of the initial gas mass at the end of the simulation.

3.3. The stellar shells

The main feature of the minor mergers in the stellar component of the S0 galaxy is the formation of shells (Fig. 7). Shells are ubiquitous in the stellar component of our simulations: they start forming already during the first apoapsis passage, and last for the entire simulation in all runs. Our finding is consistent with the results of previous studies (e.g. Peirani et al. 2010).

In all simulations, the mass confined in the stellar shells is $\geq 0.5 M_{*,\text{out}}$, i.e. it is more than half of the total mass of the stellar halo discussed in Sect. 3.2 (Fig. 6). On the other hand,

the surface brightness of most shells is quite low. For example, the total mass of stars in the shells in run A at 5 Gyr is $\sim 7 \times 10^8 M_{\odot}$, i.e. it is nearly 35% of the initial stellar mass of the satellite galaxy, but this mass is spread over $\sim 400 \times 400$ kpc. The maximum density in the strongest shells visible in Fig. 7 is $\sim 1.4\text{--}2.6 \times 10^4 M_{\odot} \text{ kpc}^{-2}$, much lower than the density in the outer parts of the S0 disc ($\sim 10^7 M_{\odot} \text{ kpc}^{-2}$). At 7 Gyr, the total mass of stars in the shells in run A rises up to $\sim 9 \times 10^8 M_{\odot}$, i.e. it is nearly 45% of the initial stellar mass of the satellite galaxy, but the density in the single shells and the ratio between density of the stellar disc and density of the shells do not change. Most shells in our simulations lie at much larger radii than the disc scale-length of the S0 galaxy, and are composed of matter removed from the satellite galaxy. We do not find evidence of shells composed of matter from the S0 galaxy (as proposed by Wallin & Struck-Marcell 1988).

3.4. The star formation rate

Our simulations include recipes for stochastic SF, as described in Sect. 2. Because of our choice of not including gas in the initial conditions of the S0 galaxy, only the gas of the satellite galaxy can contribute to SF. This allows us to study SF from stripped gas in detail. Figure 8 shows the SF rate as a function of time in our simulations. In most simulations, SF starts at the first periapsis passage ($t = 0$), and occurs mainly in the centre of the satellite galaxy, which has been strongly perturbed by the close interaction (see Mapelli et al. 2012, 2013a for more details). As soon as gas is stripped and accretes onto the S0 galaxy, SF takes place mainly in the central parts of the S0 galaxy. Thus, the first SF burst in Fig. 8 occurs in the satellite galaxy during the first

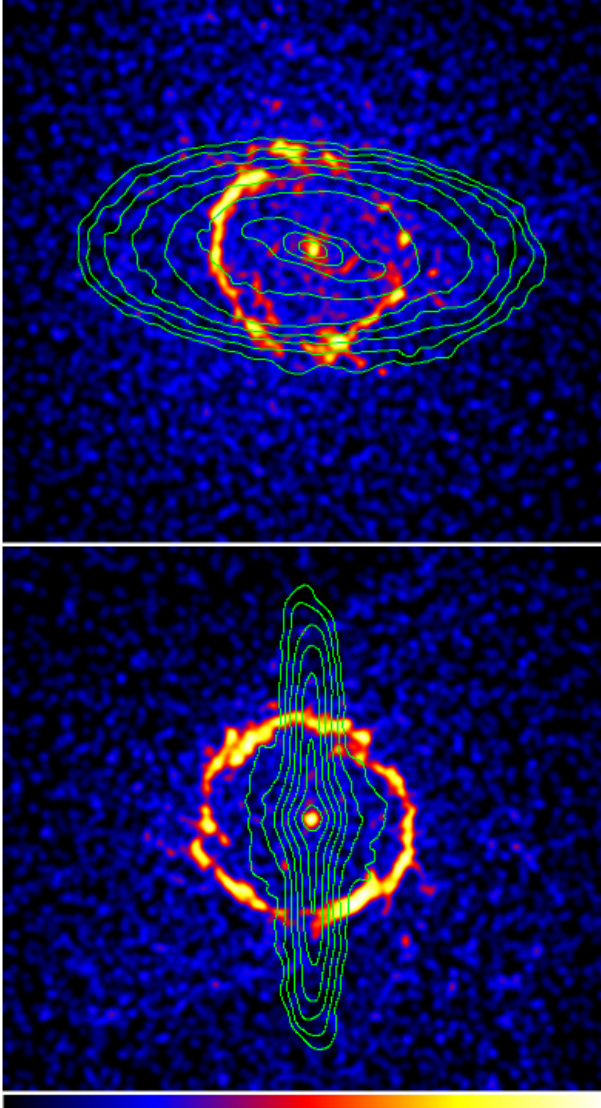


Fig. 5. Projected density of gas (logarithmic colour-coded map) and stars (isocontours) of the primary galaxy 4 Gyr after the first periastris passage. *Top panel:* run C. *Bottom panel:* run D. Each panel measures 79×67 kpc.

periastris passage, while the second, longer SF episode occurs at the centre of the S0 galaxy, and is powered by stripped gas. We notice that the SF episode in the satellite galaxy and the SF episode in the centre of the S0 galaxy have a very different duration: they last for <1 Gyr and for ~ 8 Gyr, respectively.

Interestingly, the SF rate is higher in runs B, F (i.e. the prograde runs) and C. These are also the three runs where the ring is more short-lived (apart from run E, in which the ring does not form). This suggests that the ring is suppressed when SF forms stars and stars explode as supernovae heating the surrounding gas. On the other hand, in our simulations most SF occurs in the nucleus of the S0 galaxy, rather than in the ring. This is likely an intrinsic limit of the stochastic recipes for SF (see e.g. [Mapelli et al. 2008, 2012, 2013a](#)): these cannot resolve SF in relatively diffuse warm gas regions (the ring), while enhance SF in the density peaks (the nucleus).

For most simulated galaxies, the SF rate is $\sim 10^{-2} - 10^{-3} M_{\odot} \text{yr}^{-1}$, almost constant for several Gyr. The run where gas stripping is less efficient (run E) is also the run

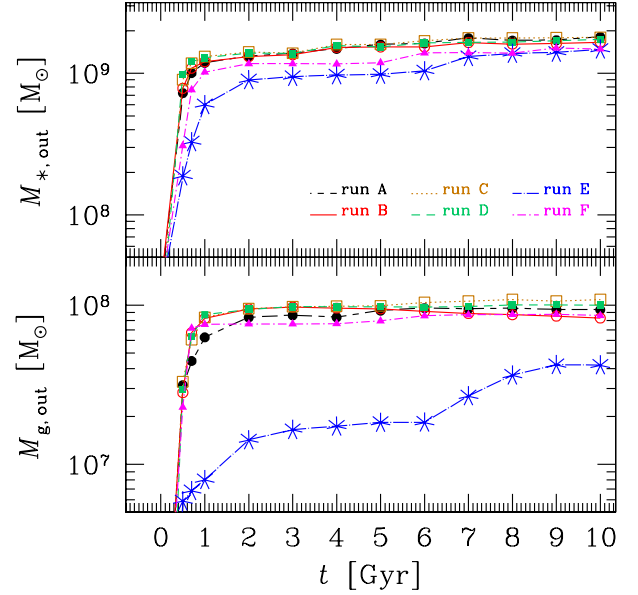


Fig. 6. *Top (bottom) panel:* mass of stars (gas) initially bound to the satellite galaxy that lie(s) at a distance >50 kpc both from the centre of the S0 galaxy and from the centre of the satellite galaxy, as a function of time. $M_{*,\text{out}}$ ($M_{g,\text{out}}$) can be considered as the mass of the stellar (gaseous) halo of the S0 galaxy. Time $t = 0$ corresponds to the first periastris passage. Long-short dashed black line and filled black circles: run A; solid red line and open red circles: run B; dotted ochre line and open ochre squares: run C; dashed green line and filled green squares: run D; long-dash-dotted blue line and blue asterisks: run E; short-dash-dotted magenta line and filled magenta triangles: run F.

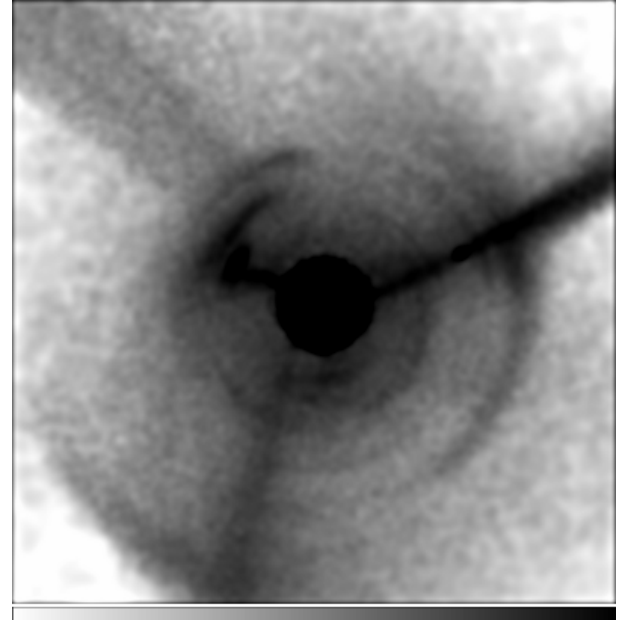


Fig. 7. Projected density of stars (logarithmic gray-scale map) 5 Gyr since the first periastris passage in run A. The box measures 400×400 kpc. The stellar disc of the S0 (seen face-on) is saturated.

with the lowest SF rate ($\sim 10^{-4} M_{\odot} \text{yr}^{-1}$, one order of magnitude lower than in the other runs). Our simulated SF rate is quite lower than the SF rate of rejuvenated S0 galaxies as estimated by [Salim et al. \(2012\)](#) ($\sim 0.5 M_{\odot} \text{yr}^{-1}$). This difference can arise from the fact that our simulated S0 galaxies are completely

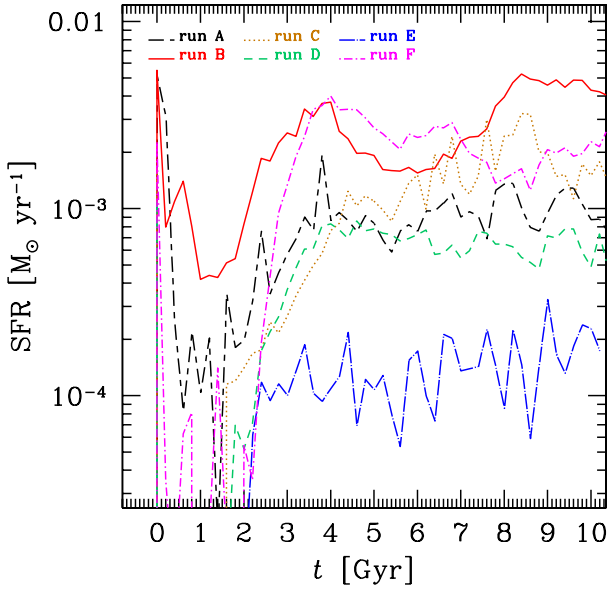


Fig. 8. Star formation rate in all simulations, as a function of time. Time $t = 0$ corresponds to the first periaapsis passage. Long-short dashed black line: run A; solid red line: run B; dotted ochre line: run C; dashed green line: run D; long-dash-dotted blue line: run E; short-dash-dotted magenta line: run F.

gas-free before the merger, while real S0 galaxies have a gas reservoir, in which SF can be triggered during the merger.

4. Discussion

Gas rings form in most of our simulations. Thus, minor mergers with gas-rich satellites appear to be a very promising scenario for the formation of the gas rings observed in S0 galaxies. But how many of these S0 rings can be explained by minor mergers?

Cosmological simulations combined with semi-analytic models (e.g. Bertone & Conselice 2009) indicate that the minor-merger fraction at redshift $z = 0$ (i.e. the fraction of galaxies that undergo a minor merger at $z = 0$) is $f_{\text{mm}} \sim 0.1\text{--}0.3$, for galaxies with stellar mass $M_* \sim 0.3\text{--}1 \times 10^{11} M_\odot$ (a reasonable mass range for S0 galaxies). Since the merger-induced SF episodes in our simulations are long-lived (≥ 6 Gyr, Fig. 8), we expect that all S0 galaxies that undergo a minor merger at $z = 0$ show signs of rejuvenation at present, under the reasonable assumption that all minor mergers occur with gas-rich satellites. Thus, we expect that $\sim 10\text{--}30\%$ of S0 galaxies appear somehow rejuvenated by a minor merger at $z = 0$.

On the other hand, we must keep in mind several *caveats* about this result. First, the minor-merger fraction estimated from cosmological simulations is quite uncertain. Furthermore, Bertone & Conselice (2009) show that the major-merger fraction estimated from the same cosmological simulations is in partial disagreement with the data. The same issue might affect even the estimate of minor mergers.

We can compare such estimates based on cosmological simulations with several observational signatures of minor mergers. Shell structures are one of the strongest scars left by merging episodes in ETGs. The literature provides quite different estimates about the fraction of ETGs showing shells, since the shell phenomenon likely depends on the galaxy environment (see e.g. Marcum et al. 2004). The fraction of ETGs showing systems of shells ranges from $\sim 16\%$ (Malin & Carter 1983; Reduzzi et al. 1996) up to $\sim 56\%$ (according to Seitzer & Schweizer 1990, who

study shell frequency among 74 field ETGs). A high fraction of shells, 44% and 41%, are found in ETGs by Schweizer & Ford (1985) and by Colbert et al. (2001), respectively.

Recently, the ultra-deep survey MATLAS investigated 92 out of 260 ETGs in the ATLAS^{3D} sample (Duc et al. 2015). Shell structures are detected in 21% of the ETGs examined. Furthermore, about half of the ETGs in Duc et al. (2015) sample show indications of minor merger (16%), major merger (12%), or interaction (22%). A large fraction of ETGs show perturbed/asymmetric halos (35%), streams (28%) and tails (17%). In summary, previous studies indicate that a significant fraction of nearby ETGs, including S0 galaxies, may have suffered minor merger episodes.

A possible estimate of the fraction of ETGs that underwent a recent SF episode may be obtained from mid infrared (MIR) spectra. Polycyclic aromatic hydrocarbons (PAH) visible at MIR wavelengths are considered a clear signature of recent SF activity (Thielens 2008). In ETGs, PAHs are detected with both normal and anomalous ratios (Kaneda et al. 2008). Vega et al. (2010) suggest that anomalous PAH ratios are due to the injection of carbonaceous material in the inter-stellar medium by carbon stars, which are present in the stellar populations with ages in the range of a few Gyr (Nanni et al. 2013). MIR spectra should then be able to provide indications about both on-going and recent (few Gyr) SF activity. Recently, Rampazzo et al. (2013) classified MIR Spitzer-IRS spectra in the nuclear region ($2\text{--}3 r_e/8$, where r_e is the effective radius) of 99 ETGs according to galaxy activity. In general, elliptical galaxies are significantly more passive than S0 galaxies. $46_{-10}^{+11}\%$ of elliptical galaxies and $20_{-7}^{+11}\%$ of S0 galaxies show passively evolving spectra, i.e. spectra without any signature of either emission lines or PAHs (see also Bressan et al. 2006). PAHs are found in $47_{-7}^{+8}\%$ of ETGs, but only $9_{-3}^{+4}\%$ have PAH ratios typical of star forming galaxies. MIR spectra then suggest that a significant fraction of ETGs have been rejuvenated in their *nuclear region* in the last few Gyr. Our simulations show that both the ring and the nuclear region are interested by the rejuvenation of the stellar population.

The aforementioned results are fairly consistent with the fact that about half of the S0 galaxies in the local Universe show signs of rejuvenation, and suggest that a significant fraction of these episodes in nearby S0 galaxies are induced by minor mergers with gas-rich satellites.

Furthermore, Annibali et al. (2007) modelled the nuclear Lick line-strength indices 65 nearby ETGs (Rampazzo et al. 2005; Annibali et al. 2006). By comparing the number of rejuvenated ETGs with the total number of galaxies in the sample, and by means of simple two-component single stellar population models, they estimate that the rejuvenation episodes do not involve more than 25% of the total galaxy mass. This estimate, together with morphological signatures and MIR indication, witnesses that the role of minor mergers could be very important in the evolution of ETGs in general, and of S0s in particular.

How efficient is gas transfer in minor mergers? Based on the WHISP survey (The Westerbork HI survey of irregular and spiral galaxies, van der Hulst et al. 2001), Sancisi et al. (2008) estimate that $\sim 25\%$ of local galaxies show signs of possible minor mergers (which is in agreement with the aforementioned value from cosmological simulations), but find that the mass accretion rate is only $\sim 1/10$ of the SF rate. Recently, Di Teodoro & Fraternali (2014) estimate that 22% of galaxies in a sub-sample of the WHISP have a dwarf companion, but the maximum gas accretion rate from these companions is about five times lower than the average SF rate of the sample (see also

Holwerda et al. 2011). These results suggest that minor mergers do not play a significant role in the total gas accretion budget. On the other hand, the galaxies considered by both Sancisi et al. (2008) and Di Teodoro & Fraternali (2014) are gas-rich spiral galaxies.

Spiral galaxies have their own reservoir of gas, and SF episodes might be triggered in several ways. In contrast, S0 galaxies do not have a rich reservoir of gas of their own: for S0 galaxies, the infall of a gas-rich companion might be the privileged way to refuel and re-activate SF.

5. Conclusions

In this paper, we investigated interactions between a S0 galaxy and a gas-rich small satellite galaxy, by means of N -body/SPH simulations. The satellite galaxy is initially on a nearly parabolic orbit with respect to the primary galaxy. We ran six simulations, varying the impact parameter (10 and 30 kpc), the inclination with respect to the plane of the S0 disc (0, 45 and 90°), and the orientation of the orbital angular momentum of the secondary galaxy with respect to the spin of the primary galaxy (prograde and retrograde). In all simulations, the satellite galaxy is slowly disrupted by the interaction, its gas is stripped during each periastris passage, and accretes onto the S0 galaxy.

We find that about 1/10 of the total gas mass of the satellite galaxy ends up in the central region of the S0 galaxy. Warm dense gas rings form in most our simulations, indicating that minor mergers are a viable scenario for the formation of gas rings in S0 galaxies and for the rejuvenation of S0 galaxies. The radius of the ring is of ~ 6 –13 kpc, depending on the simulation, and the total mass confined in the ring is 1/100–1/10 of the initial gas mass of the satellite galaxy.

We find that gas is stripped earlier in prograde runs than in retrograde ones, because tidal stripping is more efficient in prograde runs, where the relative velocity between the satellite galaxy and the particles in the S0 disc is lower. Thus, prograde encounters build gas rings earlier, but these rings have a shorter life (1–3 Gyr) than those formed in either retrograde encounters or non-coplanar encounters. Rings formed in retrograde encounters and non-coplanar encounters can live unperturbed for more than ~ 6 Gyr.

Furthermore, the rings keep memory of the orbit of the satellite galaxy: rings formed in prograde encounters are co-rotating with the disc of the S0 galaxy, while rings formed in retrograde encounters are counter-rotating. Similarly, satellite galaxies whose orbit was coplanar with respect to the disc of the S0 galaxy form co-planar rings, while satellite galaxies whose orbit was inclined by 45 and 90° with respect to the disc of the primary galaxy form rings that are inclined by 45 and 90°, respectively.

This result has another crucial implication: rings form and grow even without bar resonances. In our simulations, the strongest and most long-lived ring is polar (run D): it forms with an inclination angle of 90°.

Furthermore, the impact parameter appears to be a very important ingredient: if it is too large (30 kpc) and if the run is retrograde, the stripping is very inefficient and rings do not form for the entire duration of the simulation (> 10 Gyr).

The formation of stellar shells surrounding the S0 galaxy is also ubiquitous in our simulations, but such shells might be very faint: the mass density of stars in the shells is about three orders of magnitude lower than that in the disc of the S0 galaxy.

During the first periastris passage, SF occurs mainly in the disc of the satellite galaxy, which is strongly perturbed by the

interaction. As soon as the stripped gas reaches the centre of the S0 galaxy, SF switches on even in the S0 galaxy, while it is fast quenched in the satellite galaxy, whose initial gas was in large portion removed. The stripped gas powers an extremely long-lived (~ 8 Gyr) episode of SF in the central region of the S0 galaxy. The SF rate is $\sim 10^{-4}$ – $0.01 M_{\odot} \text{ yr}^{-1}$, depending on the simulation. We expect that it can reach higher values for a larger initial gas mass of the satellite galaxy and/or if we account for the gas reservoir of the S0 galaxy. SF and stellar feedback (supernova explosions) might play a strong role in the suppression of the gas rings: we find that gas rings disappear earlier in the runs where SF starts earlier and reaches the highest level (runs B and F).

Finally, we discuss our results in view of the minor-merger fraction derived from cosmological simulations (Bertone & Conselice 2009), from morphological signatures (shells and streams) investigated in deep surveys (Duc et al. 2015), and from the presence of PAHs in the nuclear region of S0 galaxies. We find that minor mergers might account for a significant fraction of rejuvenated S0 galaxies. This result is a fundamental clue for our knowledge of rejuvenation processes in ETGs, but deserves further investigations, since it relies on a very uncertain estimate of the minor-merger rate in the local Universe, and on a limited sample of galaxies investigated with MIR and optical spectroscopy.

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