Enhancing Semantic Segmentation with Detection Priors and Iterated Graph Cuts for Robotics

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Abstract

To foster human-robot interaction, autonomous robots need to understand the environment in which they operate. In this context, one of the main challenges is semantic segmentation, together with the recognition of important objects, which can aid robots during exploration, as well as when planning new actions and interacting with the environment. In this study, we extend a multi-view semantic segmentation system based on 3D Entangled Forests (3DEF) by integrating and refining two object detectors, Mask R-CNN and You Only Look Once (YOLO), with Bayesian fusion and iterated graph cuts. The new system takes the best of its components, successfully exploiting both 2D and 3D data. Our experiments show that our approach is competitive with the state-of-the-art and leads to accurate semantic segmentations.

Keywords: Semantic Scene Understanding, Object Detection, Segmentation and Categorization, Mapping

1 1. Introduction

Semantic segmentation is the task of decomposing a scene into its mean ingful parts. It received great attention in recent years within the research
 community because of its importance in scene understanding, robotics and

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autonomous vehicles [1, 2, 3]. In general, this task is non-trivial given the 5 high level of variability in the world and the limits of vision sensors; however, 6 when dealing with moving robots, the same scene can be framed multiple 7 times from different locations, which can make the task easier. In [4, 5, 6, 7], 8 visual recognition techniques, which are usually applied to a single view at a 9 time, are combined with a Simultaneous Localization and Mapping (SLAM) 10 algorithm, which incrementally builds a global map. This allows to find 11 correspondences between multiple views, which can be exploited to improve 12 the semantic segmentation. Both single-view and multi-view problems have 13 received attention in different contexts and at different scales: indoor and 14 outdoor scenes, scaling up to entire cities [8]. Semantic segmentation can be 15 the sensory input fed to systems reasoning about contents and their represen-16 tation in the domain of natural language [9]. These systems can learn about 17 the inter-modal correspondences between language and visual data so that 18 they can describe the content of images, e.g. by means of rich and descrip-19 tive captions. Also, semantic segmentation can help robots and autonomous 20 cars in a variety of tasks, including object detection and picking [10] and 21 autonomous navigation [11]. 22

Prior work includes many approaches, based both on plain 2D RGB 23 data [12, 4] and RGB-D (or 3D) data [13, 7, 3]. In this work, we contribute to 24 the problem of segmenting objects, humans and coarse scene elements, e.g. 25 walls, floor and ceiling, on RGB-D data, showing that some components of 26 the proposed system can be used also when only RGB data is available. Our 27 approach can be successfully used in the context of service robotics [14, 15], 28 including applications like social companion and health care: the proposed 29 system can enhance navigation, planning and interaction thanks to an im-30 proved perception. Industrial applications can also be positively impacted 31 by the proposed methods. In [16], semantic segmentation is proposed to de-32 tect the key elements involved in production and automatically sand boat 33 components. Since high reliability is required to perform challenging manu-34 facturing operations, all sources of information, in particular multiple views 35 and contextual cues, are exploited. 36

Another interesting application of the proposed system is the automatic annotation of datasets [17]. Indeed, real products, that must satisfy accuracy and safety requirements, need huge labeled datasets if based on data-driven methods. Making the annotation process faster and less expensive is of utmost importance.

⁴² In this work, we build upon a setting consisting of a single-view semantic

43 segmentation method for indoor scenes called 3D Entangled Forest classifier
44 (3DEF), previously presented in [13], and a multi-view frame fusion scheme,
45 previously presented in [18] and in [16] for industrial applications.

3DEF is a 3D semantic segmentation approach which works on single 46 camera views of indoor environments and relies on an extension of the Ran-47 dom Forest. Given a single-view image, this approach is able to model its 48 complex contextual features in a single pass in about one second. The se-49 mantic segmentation problem is tackled in two stages. First, the scene is 50 over-segmented in such a way that each segment contains at most one ob-51 ject. Being an over-segmentation, objects can be split in many segments. 52 Second, the semantic label of each segment is inferred by means of the 3DEF 53 classifier. In particular, the classification of each segment depends on learned 54 geometric relations of neighbouring segments. Finding correspondences be-55 tween multiple views can further enhance the semantic segmentation thanks 56 to the various vantage points, namely the good observations points. 57

Despite the good results with coarse scene elements, e.g. walls, floor and 58 ceiling, this approach often struggle when dealing with objects: semantic seg-59 mentation does not rely on any high-level prior, but focuses on local geometry 60 and texture. In this context, object detection can be seen as a complementary 61 approach: it is based on strong priors about a given set of objects that need 62 to be recognized in a scene. This leads object detectors to accurately detect 63 and localize such objects, neglecting all the background, that is, the main 64 part of an image. In this work, we study how to exploit both approaches, ex-65 tending a state-of-the-art object detector with iterated graph cuts [19, 20] to 66 output accurate segmentation masks and then using Bayesian fusion to com-67 bine such segmentations with 3DEF and the multi-view frame fusion scheme. 68 While many approaches have been developed over the last years, we focus 69 on Mask R-CNN [21] and You Only Look Once (YOLO) [22, 23, 24]. Mask 70 R-CNN is a deep neural network used to detect objects in images while gen-71 erating a segmentation mask for each object detected. YOLO is also a deep 72 neural network but it does not generate any segmentation mask. In contrast 73 to prior works, these methods do not need object proposals to reduce the 74 search space; rather, they apply a neural network to the full image so pre-75 dictions are informed by global image context. These methods are fast: they 76 process images in real-time with a GPU acceleration and, using the lightest 77 models, they run in a few seconds per image on a CPU. Even with limited 78 computational resources, they can be successfully used to refine lighter and 79 less precise methods if executed asynchronously alongside them. 80

An example of the final result achieved by the proposed system is reported in Figure 1: (a) shows a dining room annotated pixel per pixel, (b) shows an outdoor scene with refined segmentation masks for each object.

- ⁸⁴ The main contributions of this paper are:
- the introduction of an object detector into our multi-view semantic
 segmentation pipeline, in order to deal with complex objects as well as
 coarse scene elements like walls;
- the Bayesian approach for incorporating the top-down cues of an object detector into the bottom-up semantic segmentation process, which achieves a good balance between the two systems;
- the extension of state-of-the-art object detector like Mask R-CNN and
 YOLO with graph cut optimization for accurate object detection and
 contour segmentation.

Our novel approach proved to be competitive with respect to the state-of-94 the-art. It can handle the multiple, sometimes overlapping, bounding boxes 95 and segmentation masks returned by the object detector. Furthermore, it 96 takes advantage of the confidences provided by the detection and semantic 97 segmentation systems to consider the best of the two predictions. The 3D 98 multi-view frame fusion technique further refines the semantic segmentation. 99 The remainder of the paper is organized as follows. Section 2 overviews 100 the state-of-the-art in object detection, single-view semantic segmentation 101 and multi-view semantic segmentation. Section 3 introduces both the single-102 view and multi-view approach for semantic segmentation. Special attention 103 is paid to the description of the process of creating accurate segmentation 104 using the detection priors and iterated graph cuts. Then, the fusion of Mask 105 R-CNN and You Only Look Once Detector (YOLO) with the 3D Entan-106 gled Forests (3DEF) is also described in depth. In Section 4, our methods 107 are thoroughly evaluated on the NYU Depth Dataset V2 [2]. Further tests 108 are performed on the Microsoft Common Objects in COntext (MS COCO) 109 dataset [25] showing that the 2D component of our method can be useful even 110 for computer vision applications lacking 3D data, both indoor and outdoor. 111 Finally, in Section 5, our achievements are recapped and future directions 112 of research identified. 113





(b)

Figure 1: Example of (a) multi-view semantic segmentation with object priors obtained on the NYU dataset and (b) refined segmentation masks obtained on the COCO dataset.

114 2. Related Work

Nowadays, Deep Neural Networks (DNNs) are boosting many fields. Con-115 volutional Neural Networks (CNNs) already revolutionized semantic segmen-116 tation. One of the early attempts belongs to Couprie *et al.* [3, 26], who 117 proposed a multiscale CNN architecture to combine information at different 118 perceptive field resolutions. They were among the first to train a CNN with 119 depth information for this task. Later, many other approaches have been 120 proposed [7, 12, 27, 28, 29, 30]. The work by L. P. Tchapmi *et al.* [28] pro-121 poses a deep neural network called SEGCloud able to work with point clouds, 122 instead of regular 3D voxel grids or collections of images. The method com-123 bines the advantages of neural networks, trilinear interpolation and fully 124 connected Conditional Random Fields to enforce global consistency. For 125 robotic or mobile applications, for which computational power is often con-126 strained, the trade-off between speed and accuracy have been further ex-127 plored [31, 13, 32]. To reduce the computational power required, other non 128 CNN-based approaches also exist in this scenario, like the two works by D. 129 Wolf et al. [31, 13]. Interestingly, in [13], D. Wolf et al. outperform [31] 130 introducing the 3D Entangled Forest, an extension to the standard Random 131 Forest. This classifier is able to model complex contextual features in one 132 single pass in less than one second per frame on a standard CPU, without 133 relying on complex graphical models, random fields or other post-processings 134 as e.g. in [33]. In this work, the capabilities of this approach are further ex-135 plored. First, it is coupled with an object detector. Then, to get the best 136 out of the two methods, Bayesian fusion and a refinement step working in 137 3D are proposed. 138

In applications with moving robots, recognition techniques can be en-139 hanced by observing the environment from several points of view. This 140 problem is a particular instance of semantic mapping, described in [34] as the 141 problem of identifying and recording the signs and the symbols that contain 142 meaningful concepts for humans. These can be coarse scene elements [35], 143 objects [35, 36, 37, 38, 39], places [40, 37] and other elements of interest [41]. 144 In the literature, the creation of such representation is tackled at different 145 scales, indoor and outdoor, and using a reference system that can be either 146 local, (e.g. with respect to the sensor), or global. In this work we focus 147 on multi-view semantic segmentations of indoor scenes in the camera refer-148 ence system. Solutions to this problem have been proposed by J. Stückler et 149 al. [42], A. Hermans et al. [4] and J. McCormac et al. [5]. They differ because 150

of the adopted registration system and semantic segmentation method. For 151 registration, they use a Multi-Resolution Surfel Map-based SLAM, a cam-152 era tracking system without explicit loop closure and Elastic Fusion [5], re-153 spectively. For semantic segmentation, they use random decision forests, a 154 combination of random decision forests and conditional random fields, and a 155 CNN, respectively. They all adopt a Bayesian framework for combining the 156 multiple views. In [43], a new method for incrementally building a dense, 157 semantically annotated 3D map in real-time is studied. It assigns class prob-158 abilities to each region, not each element, of the 3D map, which is built 159 up through a robust SLAM framework and incrementally segmented with a 160 geometric-based segmentation method. Alternative multi-view approaches 161 incorporating multi-view information into state-of-the art convolutional net-162 works have been proposed in [44, 45, 46]. Another multi-view frame fusion 163 scheme was introduced by Antonello et al. [18]. This method is tested with 164 a light SLAM algorithm like RGB-D SLAM [47], which finds the correspon-165 dences between the views. The multi-view semantic fusion considers the 166 neighbourhood of each point and adds a geometrical verification step, useful 167 for improving the semantic segmentation of the single-frames. Wrong con-168 tributions due to lens distortions or alignment errors are filtered out. In this 169 work, this method is further studied. With respect to the previous work, the 170 single-view contributions are enhanced by detection priors refined with iter-171 ated graph cuts. As discussed in [48], the lack of a uniform representation, 172 as well as standard benchmarking suites, prevents the direct comparison of 173 many semantic mapping algorithms. Here, since our focus is more the clas-174 sification task, we cast the problem as multi-view semantic segmentation 175 and, as in [4, 5, 43], evaluate each single frame after taking into account the 176 multiple points of view. 177

In the past, the most successful approaches to object detection utilized 178 a sliding window paradigm, in which a computationally efficient classifier 179 tests for object presence in every candidate image window [49, 50, 51]. The 180 steady increase in complexity of the classifiers has led to improved detec-181 tion quality, but at the cost of significantly increased computation time per 182 window. Thus, in order to reduce the search space, many top performing 183 object detectors [52, 53, 54] work on detection proposals [55, 56], i.e. only 184 a small subset of all the possible windows. Two in-depth reviews can be 185 found in [57, 58]. In contrast to prior works, the state-of-the-art family of 186 object detectors known as You Only Look Once (YOLO) [22, 23] does not 187 need object proposals and applies a single neural network to the full image, 188

so its predictions are informed by global context in the image. This network 189 divides the image into regions and predicts bounding boxes and related de-190 tection probabilities for each region. These bounding boxes are weighted by 191 the predicted probabilities. Such methods are fast: they process images in 192 real-time with GPU acceleration and, using a lighter model, they run on a 193 CPU at a few seconds per image. In recent years, object detectors capable 194 of generating a high-quality segmentation mask for each instance have been 195 proposed, e.g. Mask R-CNN [21]. Mask R-CNN extends Faster R-CNN by 196 adding a branch for predicting an object mask in parallel with the existing 197 branch for bounding box recognition. Given an image as input, Mask R-198 CNN generates proposals about the regions where there might be an object 199 and predicts its class. Based on the proposal, it then generates a mask of 200 the object. The boxes and masks returned by these methods can be coarse 201 and benefit from a further refinement. In the literature, there exists meth-202 ods for segmenting foreground and background given some initial hints, e.g. 203 boxes, incomplete segmentation masks [19, 20] and extreme points [59]. In 204 this work, we prefer boxes and segmentation masks over extreme points, 205 i.e. left-most, right-most, top, bottom pixels, to better cope with imperfect 206 boxes and mask. In addition to refining the detected objects in the multiple, 207 likely overlapping, priors, we also study how to combine these priors with a 208 multi-view semantic segmentation system. 209

210 3. Methods

Our approach tackles the fusion of a bottom-up semantic segmentation 211 with top-down object detection priors and the preliminary refinement of the 212 object detector priors. The semantic segmentation and object detection ap-213 proaches are fused with the aim of leveraging the best of the two algorithms, 214 which have different properties as they assume different prior knowledge 215 about the observed scene, and they are based on 3D data (semantic seg-216 mentation) and 2D data (object detection). Such a combination needs to 217 handle multiple, likely overlapping, object priors returned by the detector. 218 This will be achieved by integrating the object priors in the right order, fus-219 ing the two contributions in a Bayesian way and smoothing the results in 220 3D. For improved results, the object detection priors are refined before fu-221 sion. The obtained single-view semantic segmentation is further improved 222 by means of our multi-view fusion scheme. An overview of both the single-223 view and multi-view algorithms is reported in Figure 2. The existing setting 224



Figure 2: Overview of the proposed approach. The single view approach can be 3DEF or our combination of 3DEF with an object detector, Mask R-CNN or YOLO. The multi-view frame fusion technique is based on the multiple frame fusion scheme introduced in [18]. The number of frames can be configured. Here, for visualization purposes, just three frames are visualized.

is presented from Subsection 3.1 to 3.3. Our contributions are thoroughlydiscussed in Subsection 3.4.

227 3.1. 3D Entangled Forest Classifier

The 3DEF approach in [13] operates on 3D point clouds, which can be acquired with an RGB-D sensor. The approach comprehends three phases:

- supervoxel over-segmentation in 3D patches;
- fusion of similar adjacent segments into larger, mostly planar segments;
- segment classification.

The input point cloud is over-segmented into homogeneous 3D patches 233 by means of the Voxel Cloud Connectivity Segmentation (VCCS) [60]. This 234 solution aims at preserving the edges by finding patches not crossing ob-235 ject boundaries and, at the same time, it reduces the noise and the amount 236 This is a region growing method which incrementally expands of data. 237 patches, in particular supervoxels, i.e. volumetric over-segmentations of 3D 238 point cloud data, from a set of seed points distributed evenly in space on a 239 grid of fixed resolution R_{seed} . Expansion from the seed points is governed 240 by a distance measure D calculated in a feature space consisting of spatial 241 extent, color, and normals: 242

$$D = \sqrt{w_c D_c^2 + \frac{w_s D_s^2}{3R_{seed}^2} + w_n D_n^2},$$

in which the spatial distance D_s is normalized by the seeding resolution, the color distance D_c is the euclidean distance in normalized RGB space, and the normal distance D_n measures the angle between surface normal vectors. Three weights can be controlled by the user: w_c , w_s and w_n . This method was proved to be more effective than existing 2D solutions.

In the subsequent step, this approach applies a region growing algorithm, 248 which recursively merges two adjacent segments c_i and c_j into larger ones. 249 The underlying idea is that bigger segments are better since the classifier 250 features tend to be more reliable. This merging step is performed evaluating 251 a distance function $d(c_i, c_j)$. In particular, given a threshold τ_{merge} , the 252 constraint $d(c_i, c_j) < \tau_{merge}$ must hold. This distance function is a linear 253 combination of the color, surface normal and point-to-plane distance between 254 the segments: 255

$$d(c_{i}, c_{j}) = w_{c}d_{c}(c_{i}, c_{j}) + w_{n}d_{n}(c_{i}, c_{j}) + w_{p}d_{p}(c_{i}, c_{j})$$

in which d_c is the color distance in Lab CIE 94 color space, d_n the surface normal difference indicated by the dot product $(1 - n_i n_j^T)$, d_p is the max of the point-to-plane distance from c_i to c_j and viceversa. The user can control three weights: w_c , w_n and w_p , normalized to sum up to 1. The algorithm stops if there are no more adjacent segments to be merged and returns the final set of segments S.

For each segment generated by the over-segmentation, a feature vector 262 x of length 18 is calculated. Besides simple color features, it includes fast 263 geometric features. Some of them are calculated from the eigenvalues of the 264 scatter matrix of the segment, which represent the variance magnitudes in 265 the main directions of the spread of the segment points. Others are calculated 266 from the Oriented Bounding Box (OBB) including all the segment points. A 267 complete list of features is given in Table 1. Then, for each segment s_t , a set 268 of close-by-segments s_i is selected on the basis of three constraints: point-269 to-plane distance, enclosed angles and Euclidean distance. During training 270 and inference, this set can be used to evaluate five binary tests defining 271 the entangled features, which are capable of describing complex geometrical 272 relationship between segments in a neighbourhood. A complete list is given 273 in Table 2. They are briefly explained as follows: 274

• Existing Segment Feature: this evaluates to true if the set of close-bysegments s_i is nonempty;

Unary features	Dimensionality
Color mean and std. dev.	2
Compactness (λ_0)	1
Planarity $(\lambda_1 - \lambda_0)$	1
Linearity $(\lambda_2 - \lambda_1)$	1
Angle with floor (mean and std. dev.)	2
Height (top and bottom point)	2
OBB dimensions	3
OBB face areas	3
OBB elongations	3
Total dimensionality	18

Table 1: List of unary features calculated for each 3D segment and their dimensionality.

Table 2: List of entangled features calculated for each 3D segment and their dimensionality.

Entangled features	Dimensionality
Existing segment	4
TopN segment	6
Inverse TopN segment	6
Node descendant	5
Common ancestor	5
Total dimensionality	26

• TopN Segment Feature and Inverse TopN Segment Feature: these features take into account the class label distributions of the current tree nodes, which the candidate segments s_i have reached so far during classification. Two parameters are learned: a label l and the bound N. In particular, they evaluate to true if a certain label l is among the most frequent N labels;

• Node Descendant Feature and Common Ancestor Feature: these features consider the path a target segment s_t or candidate segment s_i took through the tree during classification. Two parameters are learned: a label l and the bound M. They evaluate to true if a certain label l is



Figure 3: Confusion matrix of 3DEF on the NYUv2 dataset. Two challenging classes are the labels *Object* and *Furniture*, which comprehend many different objects of different sizes and shapes. The main confusion values appear between *Wall/Wall Decoration*, *Wall/Wall Window* and *Wall Decoration/TV*.

encountered within M steps.

For further details, we refer to [31]. In our tests, we stuck to the original parameters for the sake of comparison.

The shortcomings of the 3DEF classifier can only be mitigated by the 290 availability of multiple points of view, as found out in [18]. To quantita-291 tively analyze its main weaknesses, we calculated its confusion matrix on the 292 NYUv2 dataset, see Figure 3. Two challenging classes are the generic labels 293 Object and Furniture, which comprehend many different objects of different 294 sizes and shapes making it hard for a classifier to capture any distinct prop-295 erties. Also, the class *Chair* is often confused with the class *Sofa*. Finally, 296 the classes TV, Decoration and Window are challenging since they all are 297 objects located/mounted on walls so their segmentation can rely mainly on 298 color cues. Given that a multi-view method can only slightly improve over 299 these underlying issues, we further studied how to combine the strengths of 300 3DEF with those of a state-of-the-art object detector. A semantic segmenta-301 tion approach like 3DEF can accurately segment many coarse scene elements 302 and relatively big objects like Floor, Ceiling, Wall, Bed, Sofa, Chair or Book-303

shelves. Instead, an object detector like Mask R-CNN or YOLO is trained
 to detect a variety of objects with clear boundaries.

306 3.2. Multi-view Frame Fusion Scheme

The multi-view frame fusion scheme presented in [18] operates on se-307 quences of RGB-D frames, which may be acquired during normal robot op-308 erations (consider, for example, a typical patrolling task). These frames may 309 overlap and contain different views of the same entity (object or scene ele-310 ment) from different angles and distances. This module is composed of three 311 steps which can potentially run in parallel: the 3D reconstruction step, the 312 semantic segmentation step and the multi-view frame fusion step. The 3D 313 reconstruction step, here based on RGB-D SLAM [47], takes a new frame 314 from a sequence of RGB-D frames and registers it to the 3D reconstruction 315 returning its rigid transformation with respect to the reference frame. The 316 semantic segmentation step can be the original 3DEF approach applied to 317 each frame or our combination of 3DEF with Mask R-CNN or YOLO. The 318 multi-view frame fusion step, which is the focus of this section, fuses together 319 the semantic information for each point in order to exploit the availability of 320 multiple points of view. 321

Given a sequence S of RGB-D frames I_i with i varying from 1 to N, a 322 reference frame $I_{\rm ref}$ can be selected, e.g. with ref = N/2. Every 3D point P^{xy} , 323 where x and y are the coordinates in the image reference system, belonging 324 to it can be forward-projected to all the other frames in S. This way, the 325 optimal label of each point P^{xy} can be estimated after considering all the 326 contributions from all the N points of view. Figure 4 shows that the optimal 327 label of $P_{N/2}^{xy}$ can be selected after considering also the contributions from 328 forward-projected points FP_i^{xy} in the frames I_1 and I_N while Figure 5 shows 329 that not always a forward projection exists so the contribution from some 330 frames can be missing. 331

Anyway, due to lens distortions and SLAM errors like double walls or chairs, we cannot be sure that each point $P^{xy} \in I_{\text{ref}}$ truly coincides with the 3D points corresponding to each forward projection $\{FP_i^{xy}\}$. Hence, we introduced a geometrical validation step: each FP_i^{xy} is transformed to the reference coordinate system and can contribute only if:

$$\left| FP_i^{xy}.z - P_{\text{ref}}^{xy}.z \right| < \epsilon \,. \tag{1}$$



Figure 4: Forward projection from 3D to I_i , $i \neq \text{ref.}$ The red boxes around FP_1^{xy} and FP_N^{xy} denote the Moore neighbourhood. The red circle around $P_{N/2}^{xy}$ the geometric validation step: only the points side it can contribute.



Figure 5: Example of missing forward projection.

³³⁷ A good ϵ proved to be 0.05 m since just the contributions of truly coinciding ³³⁸ 3D points are of interest.

To consider the contributions from the other frames, an approach based on the Bayesian fusion at the pixel level is considered. Not only this method operates on labels but it takes in input also the classifier confidences. Given a point $P_{\text{ref}}^{xy} \in I_{\text{ref}}$ and the respective forward projected points $\{FP_i^{xy}\}$ with $i \in \{1, ..., N\} \land i \neq \text{ref}$, let j be a semantic label and $z^{\text{ref}} = \{z_1, ..., z_{\text{ref}}, ..., z_N\}$ its measurements in each frame I_i , i.e. the labels assigned to the point $P_{\text{ref}}^{xy}(z_{\text{ref}})$ and its forward-projections $FP_i^{xy}(z_i, \text{ with } i \neq \text{ref})$. According to Bayes' rule:

$$p(j|z^{ref}) = \frac{p(z_{ref}|j, z^{\overline{ref}})p(j|z^{\overline{ref}})}{p(z_{ref}|z^{\overline{ref}})} ,$$

where $z^{\overline{\text{ref}}} = z^{\text{ref}} \setminus \{z_{\text{ref}}\}$, i.e. the labels assigned to the forward-projections only. Under the assumptions of i.i.d. condition (independent and identically distributed condition) and equal a-priori probability for each class, it can be simplified to:

$$p(j|z^{\mathrm{ref}}) = \tau_j \prod_i p(z_i|j) \,,$$

where τ_j is a normalization factor such that:

$$\sum_{j=1\dots N} \tau_j p(j|z^{\text{ref}}) = 1 \,.$$

³⁵¹ In particular τ_j is calculated as:

$$\tau_j = \frac{1}{\sum_{k=1\dots N} p(k|z^{\text{ref}})} \,.$$

Parity cases are important and must be addressed appropriately. In the event
of parity, the label from the reference frame is kept.

Finally, the forward projection is improved by means of a smoothing step. 354 This step takes into account the pixel context so as to improve robustness 355 with respect to errors in the forward projection process, which can be due to 356 noise or locally imprecise registration. Each forward-projected point FP_i^{xy} 357 does not contribute with its label only but with the most frequent label in its 358 Moore neighbourhood, which comprehends itself and the eight neighbours, 359 NP_{ik}^{xy} with $1 \le k \le 8$, see the red boxes enclosing them in Figure 4. Formally, 360 let $d_{FP^{xy,j}}$ denote whether the classifier selects the label j on point FP^{xy}_{ref} or 361 not, and let $d_{NP_{ik}^{xy}, j}$ denote whether the classifier selects the label j on point 362 NP_i^{xy} or not. The majority label combination leads to the class J receiving 363 the largest total vote: 364

$$d_{FP_{\text{ref}}^{xy},J} + \sum_{k \in 1...8 \bigwedge i \neq \text{ref}} d_{NP_{ik}^{xy},J} = \max_{j=1,...,c} \left(d_{FP_{\text{ref}}^{xy},j} + \sum_{k \in 1...8 \bigwedge i \neq \text{ref}} d_{NP_{i}^{xy}k,j} \right) \,.$$

In addition, each forward-projected point does not contribute with its label confidences but with those of the neighbour pixel with the most frequent label J in the Moore neighbourhood. Nevertheless, without any geometrical verification step, this method could introduce noise in the labelling results. To be sure that each point in the 2D Moore neighbourhood is a real neighbour in 3D, only the points passing the geometrical verification step previously introduced in Equation 1 can contribute, in this case:

$$\left| NP_{ij}^{xy}.z - P_{\text{ref}}^{xy}.z \right| < \epsilon \,.$$

372 3.3. Object Detector

We selected two state-of-the-art real-time one-shot object detectors, Mask R-CNN [21] and You Only Look Once (YOLO) [22], more precisely the second version YOLOv2 [23].

Mask R-CNN generates bounding boxes and segmentation masks for each 376 instance of an object in the image. Mask R-CNN extends Faster R-CNN [53] 377 by adding a branch for predicting an object mask in parallel with the existing 378 branch for bounding box recognition. Given an image as input, Mask R-379 CNN generates proposals about the regions where there might be an object 380 and predicts its class. Based on the proposal, it then generates a mask of 381 the object. The implementation used in this work [61] is based on Feature 382 Pyramid Network (FPN) and a ResNet101 backbone. For a full description, 383 we refer to [21]. 384

In contrast to Mask R-CNN, YOLO generates only the bounding boxes. 385 It feeds a single neural network with a full RGB frame so that its predictions 386 can be informed by the global frame context. The network divides the image 387 into regions and predicts bounding boxes and probabilities for each region. 388 These bounding boxes are weighted by the predicted probabilities. The net-389 work architecture of the first version YOLOv1 is inspired by the GoogLeNet 390 model [62] for image classification. The network has 24 convolutional lay-391 ers followed by 2 fully connected layers. Instead of the inception modules 392



Figure 6: (a) Mask R-CNN finds a set of bounding boxes as well segmentation masks, for each of which a label and a confidence are associated (b) Similarly, YOLO finds a set of bounding boxes.

used by GoogLeNet, it uses 1×1 reduction layers followed by 3×3 convolutional layers, similar to Lin *et al.* [63]. The detection framework of YOLOv2 improves in speed and accuracy thanks to various design choices making it competitive with respect to region-based approaches like Faster R-CNN or Mask R-CNN. For a full description, we refer to [23].

For both detectors, we selected a model trained on the COCO detection 398 dataset [25], containing over 200 000 images with 80 different object classes. 399 The annotations of this dataset are accurate and the models learned from it 400 can be reused in other contexts, as shown also in this work. These classes, 401 which do not include coarse or large scene elements like Wall, Ceiling and 402 *Floor*, can be easily mapped to the other classes of the semantic segmentation 403 problem: most of the COCO classes simply falls in the *Object* class. For our 404 tests, we considered the proposals with a high confidence threshold, greater 405 than 0.5. The output of the detectors on two sample images is shown in 406 Figure 6. 407

408 3.4. Object Detection and Semantic Segmentation Fusion

Two steps are required to integrate the detector into our semantic segmentation pipeline:

• refinement of the object detection priors with Grabcut;



Figure 7: (a) Overview of the algorithm performing semantic segmentation with an object detector. In this scheme, for ease of visualization, the detector generates only three priors. (b) Overview of the algorithm to combine 3DEF and an object detector. The Bayesian fusion leverages on the strengths of both methods. The cluster smoothing is a final refinement.

• fusion of the refined detection priors with the semantic segmentation.

⁴¹³ The two steps are illustrated in Figure 7 and detailed as follows.

A straightforward implementation of the first step consists in labeling all 414 the pixels in the detection prior, i.e. the segmentation mask returned by 415 Mask R-CNN and the bounding box returned by YOLO. Instead, we further 416 refine these priors with the approach illustrated in Figure 7(a) and formally 417 described in Algorithm 1. The approach exploits both 2D and 3D data and 418 handles overlapping priors. For each RGB frame, the detector proposes a 419 set of detection priors associated with a label and a confidence. Given each 420 detection prior, the detected object is segmented with a method based on 421 Grabcut, a state-of-the-art unsupervised segmentation algorithm [19]. It can 422 be initialized in three ways using: 423

Algorithm 1 Detector Prior Refinement with Grabcut 1: procedure REFINE_PRIORS (I_{RGB}, I_{depth}) \triangleright Input images $priors \leftarrow \text{DETECT}(I_{BGB})$ ▷ Mask R-CNN or YOLO 2: 3: $sorted_priors \leftarrow SORT(priors)$ \triangleright Decreasing size order $new_priors \leftarrow \emptyset$ 4: for all $prior : prior \in sorted_priors$ do 5: $new_{prior_{RGB}} \leftarrow \text{REFINE}(prior, I_{RGB})$ \triangleright Grabcut 6: ▷ Grabcut $new_prior_{depth} \leftarrow \text{REFINE}(prior, I_{depth})$ 7: $new_prior \leftarrow new_prior_{RGB} \lor new_prior_{depth}$ 8: $new_priors \leftarrow new_priors \cup \{new_prior\}$ 9: 10: $I_{labeled} \leftarrow LABEL_IMAGE(new_priors)$ \triangleright With objects classes and confidences return I_{labeled} 11:

• a mask with pixels labeled as foreground, background, probable foreground and probable background;

- a bounding box around the foreground region;
- both the mask and bounding box.

For Mask R-CNN, we exploit the first option. The third option did not prove helpful since the bounding box is too coarse to help refining the mask. In particular, we set the border of the original mask as probable foreground, the inner area as foreground and the outer area as background. We determine the border thickness t as a fraction f of the radius r of a circle with perimeter p as long as the bounding box perimeter:

$$t = fr = f\frac{w+h}{\pi} \,,$$

where f was set to 0.1 in our experiments, w is the bounding box width and 434 h the bounding box height. For YOLO, we exploit the second option since 435 YOLO does not provide any segmentation mask. This option corresponds 436 to marking the outer area as background and the inner area as probable 437 foreground. Given the labeled masks in input, Grabcut creates the back-438 ground/foreground segmentation by solving a max-flow min-cut problem. A 439 weighted graph is created based on the pixel neighbouring and the labeled 440 masks. In particular, given the label α , the color z and some parameters θ 441 describing foreground and background color distributions, the cost function 442

 $E(\alpha, \theta, z)$, that Grabcut minimises with iterated graph cuts, is defined by a data term $U(\alpha, \theta, z)$ and a smoothness term $V(\alpha, z)$:

$$E(\alpha, \theta, z) = U(\alpha, \theta, z) + V(\alpha, z)$$

The two terms describe how well the pixels fit the background/foreground 445 color distributions and how smooth the labeling is over similar/a-similar 446 neighboring pixels. The optimization is followed by border matting to deal 447 with blur and mixed pixels along smooth object boundaries on which both 448 Mask R-CNN and 3DEF struggle. For robustness, given that not always a 449 segmentation can be found, Grabcut is run on both RGB and depth frames. 450 This way, the segmentations obtained from RGB and depth frames can be 451 fused using a pixel-per-pixel OR operation. We run the graph cut opti-452 mization for 5 iterations; if Grabcut cannot return any segmentation, we 453 consider the initial object detection priors as foreground. This solution does 454 not penalize labels like *Object* and *Book*, which can be characterized by tight 455 bounding boxes. Then, a label and confidence is assigned to each pixel. 456

Since detection priors can overlap, the order with which the bounding 457 boxes are processed may negatively impact the results. For instance, de-458 pending on the processing order of Grabcut, an object on a table may be 459 segmented before the table itself, so the subsequent table segmentation may 460 override the previous object segmentation, see examples in Figure 6. Because 461 of this, a straightforward method running Grabcut on each bounding box is 462 not ideal. Here, with a heuristic, detection priors are sorted in decreasing 463 order of size. This way, bigger boxes are segmented before smaller ones. In-464 deed, big boxes might be supporting surfaces like tables while small boxes 465 may contain objects lying on them. This component already improves the 466 semantic segmentation of 3DEF. 467

Given that the detector does not support the detection of all the 13 classes 468 (e.g. it cannot detect coarse scene elements like floor, walls and ceiling, be-469 cause they do not have clear boundaries) the output it provides is incomplete 470 and needs to be fused with a semantic segmentation approach. An overview 471 of the fusion process is illustrated in Figure 7(b) and formally described in 472 Algorithm 2. For each frame pixel, the predictions of 3DEF and of the detec-473 tor are fused in a Bayesian way. The two contributions can be easily retrieved 474 in 2D by iterating over the output of 3DEF and of our semantic segmentation 475 method based on the detector. Indeed, both outputs are semantic images, 476 encoding the most likely label and the probability distribution over the set 477

Algorithm 2 Semantic Segmentation with Refined Priors

1:	procedure SEMANTIC_SEGMENTATIC	$ON(cloud, I_{RGB}, I_{depth}) \triangleright$
	Input point cloud and images	
2:	$I_{labeled} \leftarrow \text{REFINE}_PRIORS(I_{RGB}, I_{depth})$	\triangleright With confidences
3:	$cloud_labeled, \ clusters \leftarrow 3\text{DEF}(cloud)$	\triangleright With confidences
4:	$cloud_labeled \leftarrow BAYESIAN_FUSION(I_{la})$	$_{beled}, cloud_labeled)$
5:	$cloud_labeled \leftarrow SMOOTH_CLUSTERS(d)$	$cloud_labeled, clusters)$
6:	${\bf return} \ cloud_labeled$	\triangleright Labeled point cloud

of labels. For simplicity, we assume that the two semantic segmentations are 478 independent and identically distributed. This is reasonable since the detector 479 and semantic segmentation rely on different features, 2D and 3D, therefore 480 they have different strengths and weaknesses. Given a frame I and a frame 481 pixel $P^{xy} \in I$, let j be its semantic label, z_{3DEF} the semantic label returned 482 by 3DEF and z_{Det} the semantic label returned by the detector. According to 483 Bayes' rule and under the assumption of i.i.d. condition, confidences can be 484 accumulated as follows: 485

$$p(j|z_{3\text{DEF}} \wedge z_{\text{Det}}) = \tau_j p(z_{3\text{DEF}}|j) \times p(z_{\text{Det}}|j) ,$$

where $p(z_{\text{Det}})$ is the confidence returned by 3DEF, $p(z_{\text{Det}})$ is the confidence returned by the detector and τ_j is a normalization factor such that:

$$\sum_{j=1\dots N} \tau_j p(j|z_{3\text{DEF}} \wedge z_{\text{Det}}) = 1.$$

488 The selected label J is the one with the highest probability:

$$J = \arg\max_{j} p(j|z_{3\text{DEF}} \wedge z_{\text{Det}})$$

Nevertheless, errors in the detector prior location or in the Grabcut-based 489 segmentation may lead to the assignment of wrong labels and confidences 490 to the pixels close to the object borders. To alleviate this, a subsequent 491 cluster smoothing step is performed. In contrast with previous steps, this 492 one exploits the point cloud, in particular the 3D preliminary segmentation 493 based on the the Voxel Cloud Connectivity Segmentation (VCCS) [60] and 494 the subsequent region growing, see Section 3.1. Given each unlabeled cluster 495 C, which is the output of the preliminary segmentation phase in the 3DEF 496

⁴⁹⁷ approach, the most frequent label of the points in C is considered. Each ⁴⁹⁸ point in C is labelled consistently with the most voted label in the cluster. ⁴⁹⁹ In the same way, the respective confidences are propagated inside the cluster ⁵⁰⁰ to all the other points.

The performance of the presented methods will be extensively discussed in the following section.

503 4. Experiments

504 4.1. Datasets

We assessed the performance of our methods on the popular NYU Depth dataset NYUv2 [2] and further evaluated the detection refinement on the Microsoft Common Objects in COntext (MS COCO) dataset [25].

The NYUv2 dataset contains 1449 pixel-wise labeled RGB-D frames which are commonly split into a subset of 795 frames for training/validation and 654 for testing. It was recorded with a Kinect v1 sensor. In contrast to its predecessor NYUv1, the annotation quality is higher and it does not wrap the class *Object* in the class *Background*. In particular, we tested our methods on the 13-class semantic segmentation problem. The 13 classes include objects, furniture and coarse scene elements, e.g. walls, ceiling and floor.

⁵¹⁵ MS COCO is a large-scale dataset object detection and segmentation ⁵¹⁶ dataset containing about 200k labeled RGB images. The object detection ⁵¹⁷ and segmentation problem considers 80 class labels of common objects in ⁵¹⁸ everyday scenes from all around the world. The dataset is split into a subset ⁵¹⁹ of 155k training images, 5k validation images and 40k test images. The labels ⁵²⁰ of the test set are not public available and the evaluation is performed in a ⁵²¹ test server.

522 4.2. Experiments on NYUv2

Similarly to the other approaches evaluated on this dataset, we used two 523 performance indicators: pixelwise recall (in the following: Global Accuracy – 524 GA) and classwise recall (in the following: Class Accuracy – CA). In addition, 525 we also reported a third performance indicator, the classwise precision (in 526 the following: Class Precision - CP), useful to further compare the variants 527 of our methods. Considering a label set with n class labels and based on the 528 elements of the confusion matrix (true positives tp, false positives fp and 529 false negatives fn, the metrics are defined as follows. GA is calculated as 530 the overall portion of correctly labeled points: 531

Table 3: Evaluation of the fusion of 3DEF with Mask R-CNN and YOLO on the NYUv2. The methods are reported in increasing order of class-wise accuracy CA. The best result are in bold. Integrating an object detector always improves over the baseline 3DEF. 3DEF+YOLO+Grabcut performs slightly better than 3DEF+Mask R-CNN. Using the depth image improves Grabcut segmentations.

Method	CA	GA	CP
3DEF [13]	55.7	65.0	53.3
3DEF+YOLO+Grabcut (rgb)	60.9	67.4	56.0
3DEF+Mask R-CNN+Grabcut (rgb)	61.2	67.3	56.1
3DEF+Mask R-CNN+Grabcut (rgb and depth)	61.2	67.3	56.2
3DEF+Mask R-CNN	61.2	67.4	56.2
3DEF+YOLO+Grabcut (rgb and depth)	61.3	67.6	56.3

$$GA = \frac{\sum_{i=1}^{n} tp_i}{\sum_{i=1}^{n} (tp_i + fn_i)}$$

⁵³² CA is the average class recall:

$$CA = \frac{1}{n} \frac{\sum_{i=1}^{n} tp_i}{\sum_{i=1}^{n} (tp_i + fn_i)}.$$

⁵³³ CP is the average class precision:

$$CP = \frac{1}{n} \frac{\sum_{i=1}^{n} tp_i}{\sum_{i=1}^{n} (tp_i + fp_i)}.$$

The last two indicators are less biased towards frequent classes. In the following, we will analyze the different combinations of 3DEF and object detector, the multi-view contribution and how our best approaches do in comparison with other state-of-the-art approaches.

We compared different ways to integrate 3DEF with Mask R-CNN and YOLO. Table 3 shows that integrating an object detector always improves over the baseline 3DEF, up to +5.6% in CA, +2.6% in GA and +2.0% in CP. 3DEF+YOLO+Grabcut performs slightly better than 3DEF+Mask R-CNN. Indeed, even if Mask R-CNN segmentations are precise, the method is penalized by misclassifications. Experimental results do not highlight any benefits in using Grabcut with Mask R-CNN: they report a situation of substantial



(c) Mask R-CNN

(d) Mask R-CNN+Grabcut

Figure 8: Examples of Mask R-CNN masks refined by Grabcut.

parity with a small detriment (-0.1%) in GA. Nevertheless, inspecting the 545 generated masks, we found out that Grabcut refines the segmentations, as 546 shown by a couple of examples in Figure 8. This improvement is counter-547 balanced by misclassified objects: in other words, the negative impact of 548 misclassified objects increases if their masks are refined. To further inves-549 tigate the combination of Mask R-CNN with Grabcut, we detail additional 550 tests on the COCO dataset in Section 4.3, which better show the benefits of 551 using Grabcut both quantitatively and qualitatively. In Figure 9, we present 552 additional qualitative results for 3DEF+YOLO+Grabcut. We report the 553 initial output of 3DEF in Figure 9(a). The integration of YOLO without 554 Grabcut, see Figure 9(b), generates a semantic labeling clearly less accurate 555 than the integration of YOLO with Grabcut, see Figure 9(c). We also re-556



Figure 9: Semantic segmentation of a fire extinguisher on the wall: (a) 3DEF: the object is mainly confused with a table; (b) YOLO-based semantic segmentation without Grabcut: the object is correctly classified but many points on the wall are misclassified; (c) YOLO-based semantic segmentation: many points are correctly classified but the object is still partially labeled as table and the wall as object; (d) 3DEF+YOLO with Bayesian fusion and the final cluster smoothing: there are no wrong labels on the object and only a few points of the wall are still labeled as object because of the imperfect initial segmentation of the 3DEF framework.

Table 4: Evaluation of the multi-view approaches on the NYUv2. The methods are reported in increasing order of class-wise accuracy CA. The best result are in bold. Using multiple views lead to the best results in CA, GA and CP.

Method	CA	GA	CP
3DEF [13]	55.7	65.0	53.3
MV-3DEF [18]	56.1	65.3	53.7
3DEF+Mask R-CNN (best)	61.2	67.4	56.2
3DEF+YOLO (best)	61.3	67.6	56.3
MV-3DEF+YOLO	61.5	67.7	56.4
MV-3DEF+Mask R-CNN	64.0	66.0	56.5

⁵⁵⁷ port the improved output after Bayesian fusion and clustering smoothing in ⁵⁵⁸ Figure 9(d).

We selected the best approaches in the previous experiment and tested the multi-view frame fusion scheme in [18] on them. For simplicity, we refer to 3DEF+YOLO+Grabcut as 3DEF+YOLO (the best approach). Table 4 shows that using multiple views does not have the same effect on all meth-

Table 5: Performance comparison on the NYUv2. The methods are reported in increasing order of class-wise accuracy CA. The class performance improvements with respect the baselines 3DEF and MV-3DEF are in boxes. The best result are in bold. Combining 3DEF with a detector makes the approach more competitive with respect to existing approaches.

Method	CA	GA	CP
Couprie <i>et al.</i> [3]	36.2	52.4	-
Hermans $et \ al. \ [4]$	48.0	54.2	-
3DEF [13]	55.7	65.0	53.3
MV-3DEF [18]	56.1	65.3	53.7
SEGCloud [28]	56.4	66.8	-
Nakajima <i>et al.</i> [43]	58.5	70.7	-
Eigen $[12, 5]$	59.9	66.5	-
3DEF+MaskRCNN (best)	61.2	67.4	56.2
3DEF+YOLO (best)	61.3	67.6	56.3
MV-3DEF+YOLO	61.5	67.7	56.4
Eigen-SF $[5]$	63.2	69.3	-
Eigen-SF-CRF $[5]$	63.6	69.9	-
MV-3DEF+MaskRCNN	64.0	66.0	56.5
MVCNet-MaxPool [45]	69.5	77.7	-

ods. In particular, MV-3DEF+YOLO slightly improves over all the coeffi-563 cients (+0.2%, +0.1%, +0.1%) while MV-3DEF+Mask R-CNN improves in 564 classwise recall and precision (+3.5% and +0.1%) but deteriorates the global 565 accuracy (-1.4%). This difference is expected since different methods have 566 different success and failure models, and different confidence distributions. 567 On this dataset, the average number of labelled frames per scene is 2.74. As 568 shown in [18], this reduces the performance benefit of the multi-view method, 569 which improves with the number of forward-projected frames. 570

In Table 5 and Table 6, we compare our methods with state-of-the-art methods for single-view and multi-view semantic segmentation. In Table 5, we report the results of single-view methods working on both RGB-D data, Couprie *et al.* [3] and Eigen *et al.* [12, 5], and 3D point clouds, 3DEF [13] and SEGCloud [28]. We also report the results of different multi-view methods, Hermans *et al.* [4], Eigen-SF-CRF [5], MV-3DEF [18], Nakajima *et al.* [43] and MVCNet-MaxPool [45]. These works are evaluated at full resolution

Table 6: Class performance comparison on the NYUv2. The class performance improvements with respect the baselines 3DEF and MV-3DEF are in boxes. The best result are in bold. Combining 3DEF with a detector makes the approach more competitive with respect to existing approaches.

Method	Bed	Opject	Chair	Furniture	Ceiling	Floor	Picture	Sofa	Table	Wall	Window	Books	TV
Couprie et al. [3]	38.1	8.7	34.1	42.4	62.6	87.3	40.4	24.6	10.2	86.1	15.9	13.7	6.05
Hermans et al. [4]	68.4	8.6	41.9	37.1	83.4	91.5	35.8	28.5	27.7	71.8	46.1	45.4	38.4
3DEF [13]	74.2	17.2	63.4	48.1	80.3	98.7	26.5	71.0	46.5	84.0	25.4	55.1	34.1
MV-3DEF [18]	73.2	17.5	64.5	48.8	80.2	98.7	27.2	74.5	50.4	84.2	29.5	56.0	42.7
SEGCloud [28]	75.1	39.3	62.9	61.8	69.1	95.2	34.4	62.8	45.8	78.9	26.4	53.5	28.5
Nakajima et al. [43]	83.7	52.5	56.7	76.1	24.4	83.3	40.8	77.7	53.0	75.3	64.4	15.6	57.3
Eigen [12, 5]	42.3	46.5	72.4	60.8	73.1	85.7	57.3	38.9	42.1	85.5	55.8	49.1	68.5
3DEF+Mask R-CNN	85.2	18.5	82.8	57.8	79.2	97.4	23.8	76.7	55.1	80.1	22.2	61.3	55.8
3DEF+YOLO	86.9	17.7	82.4	55.0	79.2	96.8	24.1	71.6	51.4	82.7	25.0	66.3	57.5
MV-3DEF+YOLO	87.8	17.7	82.3	54.8	81.3	96.6	23.0	71.6	51.2	82.7	25.8	66.7	57.3
Eigen-SF-CRF [5]	48.3	46.9	74.7	63.5	79.0	90.8	63.6	46.5	45.9	89.4	55.6	51.5	71.5
MV-3DEF+Mask R-CNN	95.3	18.9	85.9	62.8	89.4	96.2	22.6	75.9	53.7	79.8	14.5	68.8	67.7

 $_{578}$ (640 × 480) with the exception of the approaches presented in [5, 43] which report the result when working at half resolution (320 × 240). In Table 6, we compare the methods class by class. We do not report the results for MVCNet-MaxPool [45] since they are not available and we report the results of Eigen-SF-CRF over Eigen-SF since it is the best performing among the two.

As reported in both tables, a significant boost in performance is ob-584 tained by combining the 3DEF classifier and a detector, both Mask R-CNN 585 and YOLO. In particular, our best single-view 3DEF+YOLOs outperform 586 the baselines based on 3DEF (+5.2% in CA, +2.3% in GA and +2.5%587 in CP) as well as SEGCloud [28] (+4.9% in CA and +0.8% in GA) and 588 Eigen [5, 43] (+1.3% in CA and +1.1% in GA). 3DEF+YOLO outperforms 589 also Nakajima et al. [43] in CA (+3.0%) but not in GA (-3.0%) since 590 our method offers better performance class by class but not on classes with 591 more samples in the dataset. Using multi-views highlights the strengths of 592 our methods: MV-3DEF+YOLO gets closer to Eigen-SF, Eigen-SF-CRF 593 and MVCNet-MaxPool while MV-3DEF+Mask R-CNN outperforms Eigen-594 SF and Eigen-SF-CRF, and gets closer to MVCNet-MaxPool. In particular, 595 MV-3DEF+Mask R-CNN outperforms Eigen-SF-CRF in CA (+0.4%) but 596 not in GA (-3.9%). The method is stronger class by class but penalized 597 by the performance with the classes with more samples in the dataset, in 598 particular the class *Wall*. Neither the integration of the object detector nor 599 the multi-view allow to outperform MVCNet-MaxPool [45], (-5.5%) in CA 600

Table 7: Class performance differences between the two best methods on the NYUv2. MV-3DEF+YOLO and MV-3DEF+Mask R-CNN outperform MV-3DEF in 8 and 9 out of 13 classes, respectively. Improvements are in bold.

Method vs MV-3DEF $\left[18\right]$	Bed	Object	Chair	Furniture	Ceiling	Floor	Picture	Sofa	Table	Wall	Window	Books	TV
MV-3DEF+YOLO	+14.6	+0.2	+17.8	+6.0	+1.1	-2.1	-4.2	-2.9	+0.8	-1.5	-3.7	+10.7	+14.6
MV-3DEF+Mask R-CNN	+22.1	$^{+1.4}$	+21.4	+14.0	+9.2	-2.5	-4.6	$^{+1.4}$	+3.3	-4.4	-15.0	+12.8	+25.0

Table 8: Class performance differences between the two best methods on the NYUv2. MV-3DEF+YOLO and MV-3DEF+Mask R-CNN outperforms Eigen-SF in 7 out of 13 classes. MV-3DEF+Mask R-CNN and Eigen-SF-CRF are almost equivalent in 2 other classes. Improvements are in bold.

Method vs Eigen-SF-CRF [5]	Bed	Object	Chair	Furniture	Ceiling	Floor	Picture	Sofa	Table	Wall	Window	Books	TV
MV-3DEF+YOLO	+39.5	-29.2	+7.6	-8.7	+2.3	+5.8	-40.6	+25.1	+5.3	-6.7	-29.8	+15.2	-14.2
MV-3DEF+Mask R-CNN	+47.0	-28.0	+11.2	-0.7	+10.4	+5.4	-41.0	+29.4	+7.8	-9.6	-41.1	+17.3	-3.8

and -11.7% in GA). This approach already exploits multiple views and it would be interesting to study how to combine it with an object detector.

Class by class performance is further investigated comparing our best 603 methods against the baseline MV-3DEF [18] in Table 7 and against Eigen-604 SF-CRF [5] in Table 8. MV-3DEF+YOLO and MV-3DEF+Mask R-CNN 605 outperform MV-3DEF [18] in 8 and 9 out of 13 classes, respectively. The im-606 proved classes are Bed, Object, Chair, Furniture, Ceiling, Sofa, Table and 607 Bookshelf. MV-3DEF+YOLO and MV-3DEF+Mask R-CNN outperform 608 Eigen-SF-CRF [5] in 7 out of 13 classes, Bed. Chair, Ceiling, Floor, Sofa, 609 Table and Bookshelf. MV-3DEF+Mask R-CNN and Eigen-SF-CRF [5] are 610 almost equivalent in 2 other classes, Furniture and TV. Both tables show 611 that our methods suffer when classifying Wall, Picture and Window. This 612 is a weakness of 3DEF that cannot be compensated by the detectors since 613 they are not trained on those classes. This could be further investigated by 614 training the detector on the classes *Picture* and *Window* or by improving 615 the preliminary region growing segmentation in 3DEF. Indeed, the region 616 growing can erroneously merge the three classes in a single cluster making it 617 impossible for 3DEF to classify them correctly. 618

Additional qualitative results are reported in Figure 10. For each scene, the predicted semantic segmentation and its ground truth are reported side



Figure 10: Qualitative results on the NYUv2 dataset: (a)(c)(e)(g) multi-view semantic segmentation obtained with the best of our methods, MV-3DEF+Mask R-CNN and (b)(d)(f)(h) groundtruth semantic segmentation.

Table 9: Average precision comparison on the COCO dataset. The performance improvements with respect to the baseline Matterport Mask R-CNN [61] are enclosed in boxes. The best results are in bold.

Method	AP	AP_{50}	AP_{75}	AP_S	AP_{M}	AP_{L}
Matterport Mask R-CNN [61]	28.2	47.1	30.0	12.7	30.0	38.0
Mask R-CNN+Grabcut	28.4	47.7	29.9	12.5	29.9	39.1
FAIR Mask R-CNN [21]	43.8	68.8	47.1	23.7	46.4	61.4

Table 10: Average recall comparison on the COCO dataset. The performance improvements with respect to the baseline Matterport Mask R-CNN [61] are enclosed in boxes. The best results are in bold.

Method	AR_1	AR_{10}	AR_{100}	AR_{S}	AR_{M}	AR_{L}
Matterport Mask R-CNN [61]	24.6	34.3	34.9	15.9	37.2	47.9
Mask R-CNN+Grabcut	25.0	34.9	35.5	15.7	37.5	49.8
FAIR Mask RCNN $[21]$	34.7	55.0	58.0	40.7	62.1	73.3

⁶²¹ by side. Generally, our approach successfully classifies several classes, e.g. ⁶²² Chair, Furniture, Table and Books in the reported scenes. Also some correct ⁶²³ instances of Object are visible. Nevertheless, as previously discussed, the ⁶²⁴ method struggles with Picture, Wall and Windows.

625 4.3. Experiments on COCO

We further investigate the performance of the 2D component of our ap-626 proach on the COCO dataset [25]. Similarly to other approaches evaluated 627 on this dataset, we characterized the performance of our method using the 628 12 metrics proposed by the authors. They capture the average precision at 629 different Intersection over Unions (IoU), i.e. with loose or strict detection 630 versus groundtruth matching criteria, and across scales, i.e. evaluating the 631 performance separately when dealing with small objects and large objects. 632 They capture also the average recall given a maximum number of objects per 633 frame and across scales. Each metric is described in the following: 634

• average precision with IoUs from 0.50 to 0.95 with a step of 0.05 (AP);

• average precision at IoU 0.50 (AP ₅₀)				• •		т тт	0 20		
	36	•	average	precision	at .	IoU	0.50 ($\left(AP_{50} \right)$);

- average precision at IoU 0.75 (strict metric) (AP₇₅);
- average precision for small objects with an area less than $32^2 \text{ px}^2 (\text{AP}_{\text{S}})$;
- average precision for medium objects with an area greater than 32^2 px^2 and less than $96^2 \text{ px}^2 (\text{AP}_{\text{M}})$;
- average precision for large objects with an area greater than 96^2 px^2 (AP_L);
- average recall given one detection per image (AR_1) ;
- average recall given 10 detections per image (AR_{10}) ;
- average recall given 100 detections per image (in the following: AR_{100});

• average recall for small objects with an area less than 32^2 px^2 (AR_S);

• average recall for medium objects with an area greater than 32^2 and less than $96^2 \text{ px}^2 (\text{AR}_{\text{M}})$;

• average recall for large objects with an area greater than $96^2 \text{ px}^2 (\text{AR}_{\text{L}})$.

In Table 9 and 10 we compare our method against Matterport Mask R-650 CNN [61] and FAIR Mask R-CNN [21]. Matterport Mask R-CNN [61] is 651 an open-source implementation of Mask R-CNN we use as baseline for de-652 veloping our method Mask R-CNN+Grabcut. FAIR Mask R-CNN [21] is 653 an ensemble of 30 Mask R-CNN methods. This method is the best per-654 forming one. As reported in Table 9 and 10, our approach obtains better 655 results in both AP and AR with respect to the baseline Matterport Mask 656 R-CNN [61]. The performance improvement with respect to the baseline is 657 enclosed in boxes. Most of the metrics (AP, AP⁵⁰, AP^L, AR¹, AR¹⁰, AR¹⁰⁰, 658 AR^M and AR^L) are improved while the two approaches are almost equivalent 659 with respect to the remaining ones $(AP^{75}, AP^{S}, AP^{M}, AR^{S})$. 660

Qualitative results are shown in Figure 11. Using our method, the object contours are better defined, as it is visible comparing Figure 11(a)(b) with Figure 11(b)(d). Nevertheless, the mask can get worse if the color model is not captured by Gaussian mixture model used by Grabcut. An example of this behaviour in shown in Figure 11(g)(h) in which Grabcut is confused by the square pattern of the shirt.





(b) Mask R-CNN+Grabcut



(c) Mask R-CNN



(d) Mask R-CNN+Grabcut



(e) Mask R-CNN



(f) Mask R-CNN+Grabcut



(g) Mask R-CNN



(h) Mask R-CNN+Grabcut

Figure 11: Qualitative results on the COCO dataset: (a)(c)(e)(g) segmentation masks obtained with Matterport Mask R-CNN [61] and (b)(d)(f)(h) refined segmentation masks obtained with Mask R-CNN+Grabcut. Our approach refines the mask contours.

Method	fps
Semantic segmentation with 3DEF	0.53
Mask R-CNN detector	0.94
YOLO detector	4.20
Mask R-CNN refinement with Grabcut	0.19
YOLO refinement with Grabcut	0.90
Multi-view frame fusion scheme	2.27
Full system with Mask R-CNN	0.12
Full system with YOLO	0.27

Table 11: Running times of our system on the laptop Dell Inspiron 15 7000 installed on our mobile robot [14].

667 4.4. Runtime Analysis

We tested our system on a standard laptop Dell Inspiron 15 7000 installed 668 on our mobile robot [14]. It runs Ubuntu 18.04 and is equipped with an Intel 669 Core i7-6700HQ CPU with 4 cores clocked at 2.60 GHz, the graphic card 670 NVIDIA GeForce GTX 960M and 16 GB of DDR3 RAM. We worked at full 671 resolution $(640 \times 480 \,\mathrm{px})$. The running times evaluated on the NYUv2 dataset 672 are reported in Table 11. The proposed approach makes use of a technique for 673 semantic segmentation, which requires approximately 0.53 fps on the CPU. 674 The object detectors Mask R-CNN and YOLO work on the GPU at 0.94 fps 675 and 4.20 fps, respectively. The combinations of the detectors with Grabcut 676 work at an average speed of $0.19 \, \text{fps}$ when using masks and $0.90 \, \text{fps}$ when 677 using boxes. The multi-view works at an average speed of 2.27 fps leading to 678 a total runtime of approximately 0.12 fps with Mask R-CNN and 0.27 fps with 679 YOLO. The current system requires more work to be used in real-time on a 680 standard laptop. Nevertheless, it is suitable in less demanding applications 681 requiring occasional accurate decisions or for offline processing. 682

5. Conclusions

In this work, we extended a multi-view semantic segmentation system based on 3D Entangled Forests (3DEF) by integrating and refining two object detectors, Mask R-CNN and You Only Look Once (YOLO), with Bayesian

fusion and Grabcut. The new system takes the best of its components, suc-687 cessfully exploiting both 2D and 3D data. Our experiments on two popular 688 datasets, NYUv2 and COCO, show that our approach is competitive with 689 the state-of-the-art and leads to accurate semantic segmentations. In par-690 ticular, the 2D component of our method can be useful even for computer 691 vision applications lacking 3D data, both indoor and outdoor. In the future, 692 we would like to explore other semantic segmentation techniques and study 693 how to perform accurate detection and segmentation of both objects and 694 coarse scene elements limiting the number of separate components. 695

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