

1 **BOND BEHAVIOR OF STEEL FIBER REINFORCED MORTAR (SFRM) APPLIED**  
2 **ONTO MASONRY SUBSTRATE**

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6  
7 **ABSTRACT**

8 Masonry was the most used material during the last centuries to build constructions. Most of  
9 the existing masonry structures (buildings, bridges etc.) were built without considering some  
10 important structural considerations that are important nowadays. Moreover, due to factors such  
11 as the increasing of service loads, materials aging, structural damage, etc., existing masonry  
12 structures require strengthening interventions. The definition of optimal strengthening  
13 strategies using traditional and innovative materials is still an important issue of the scientific  
14 research. In fact, during the last decade, many researchers focused their attention studying  
15 innovative composites materials, such as fiber-reinforced polymers (FRP) and fiber-reinforced  
16 cementitious matrix (FRCM) composites, for the strengthening of existing masonry structures.  
17 This research has focused on aspects such as the bond behavior between the substrate and the  
18 composite materials, the structural behavior of the strengthened masonry and concrete  
19 structures, and the compatibility and reversibility of these materials when bonded to existing  
20 substrates. In this study, the bond behavior of a composite material known as steel fiber-  
21 reinforced mortar (SFRM), recently used as for the strengthening of existing structures, applied  
22 onto masonry structures is analyzed experimentally and numerically. First, the material is  
23 characterized experimentally with the aim of getting insight on its behavior and applicability  
24 when applied as an innovative technique for the strengthening of masonry and to obtain  
25 mechanical parameters required for the numerical models. Mechanical properties of the SFRM

26 studied included flexural and compressive strength, tensile strength, and residual flexural  
27 strength. The SFRM bond behavior on masonry substrates was evaluated by means of double  
28 shear lap tests. In addition, the experimental tensile and bond behavior of the SFRM is studied  
29 numerically through finite element models validated using the results obtained during the  
30 experimental tests. Results show that if an adequate bonded length is provided, the SFRM can  
31 fully develop its tensile strength as detachment from the substrate is not observed.

32 **Keywords:** steel fiber reinforced mortar (SFRM); masonry; strengthening; mechanical  
33 characterization; bond behavior, tensile test, numerical modelling.

34

## 35 1. INTRODUCTION

36 The interest to preserve old masonry structures has caught the attention of the scientific  
37 community and civil engineering industry. This interest has led to the development of many  
38 techniques used to improve the structural safety level of masonry structures and reduce their  
39 structural vulnerability. One of the first techniques employed consisted in the use of steel  
40 applied to masonry structural elements with the aim of increasing their compression, flexural,  
41 and shear strength [1]. However, with the gain in knowledge regarding the behavior of  
42 strengthened masonry structures, such traditional techniques have been replaced by the use of  
43 externally bonded composite materials, such as fiber reinforced polymers (FRP) [2-5], and fiber  
44 reinforced cementitious matrix (FRCM) composites [6-10].

45 These composite materials can also improve the confinement, flexural and shear strengths of  
46 the masonry structural elements with a low weight increment. In addition, their application to  
47 straight and curved surfaces is easily performed due to its mode of application [11]. However,  
48 some disadvantages deserve to be considered. For FRP composites, the vapor permeability of  
49 the masonry structures can be compromised due to the epoxy resin used for the adhesion of the  
50 fibers to masonry substrates. Other disadvantages are related to the inability to apply the FRP

51 at low temperatures or on wet surfaces [12]. Instead, FRCM composites are able to overcome  
52 some of these disadvantages. In fact, during the last decade, the epoxy resin has started to be  
53 substituted with the cementitious matrix that is more compatible with masonry materials [10,  
54 13]. However, a recent study has pointed out that the application of FRCM has a lower increase  
55 in the load-carrying capacity when compared to FRP, but it promotes a higher increase in the  
56 ductility [14, 15].

57 Recently, the interest in the use of fiber reinforced concrete (FRC) or mortar (FRM) composites,  
58 comprised of an ultra-high performance concrete or mortar and short fibers, as strengthening  
59 material is a growing research field but, due to its novelty, the available scientific literature on  
60 the topic is quite limited. In fact, the use of these materials has been generally studied as a  
61 construction material for the design of new structural elements [16,17] and the experimental  
62 and numerical research has focused on the evaluation of its mechanical properties (uniaxial  
63 tensile strength and tensile fracture properties [18], etc.), the behavior of new high performance  
64 reinforced concrete elements [19], the ultimate shear behavior of hybrid RC beam and steel  
65 columns [20], or its use on building applications such as non-structural elements, for instance.  
66 In these cases, the presence of the fibers improves the mechanical properties of the building  
67 material and allows decreasing the area of steel reinforcement.

68 As strengthening material, FRC or FRM has been studied as an externally bonded strengthening  
69 system applied onto concrete bridge piers [21], masonry walls [22, 23], or at the intrados of  
70 masonry arches [24], with promising results. Among the advantages of FRC or FRM, it can be  
71 noticed that the use of high performance cementitious matrix guarantees an adequate vapor  
72 permeability with considerable abrasion resistance and high durability [25]. Furthermore, its  
73 high compressive strength can provide an increase in the compressive resistance of the  
74 structural element, which is not achieved when FRP or FRCM composites are used. In addition,

75 the flowability and self-compacting properties of the material allow filling simple traditional  
76 formwork which facilitates its application on the elements to be strengthened.

77 As for the case of another available externally bonded strengthened systems, such as FRCM  
78 and FRP composite materials, in which those issues have been more extensively discussed and  
79 studied, knowledge on the bond behavior of these materials when applied onto existing  
80 substrates issues is crucial for the understanding of the overall behavior of FRC/FRM  
81 strengthened structures. Available literature in the topic has focused mainly on the study of such  
82 materials applied onto normal compressive strength substrates for either repair or strengthening  
83 applications. As repair material, the bond behavior has been studied by means of slant shear,  
84 splitting tensile, and direct tensile tests, which do not replicate exactly the conditions expected  
85 when the material is externally bonded as a strengthening solution [26, 27]. As for strengthening  
86 material, Zhang et al 2020 [28] have recently investigated the shear bond strength of FRC  
87 applied onto concrete by means of double-sided direct shear tests. The test results showed that  
88 the interface between the FRC and the substrate exhibited an excellent bond behavior, which  
89 verifies the feasibility of the use of these materials for the strengthening of existing structures.

90 In their research, the most common failure mode of the specimens was associated with partial  
91 interface failure with partial or complete failure in shear of the substrate. However, on the  
92 authors' knowledge, there is no experimental evidence on the study of the bond behavior of  
93 these materials when applied to masonry substrates.

94 Based on this requirement, this paper is aimed to provide an exhaustive experimental and  
95 numerical analysis of the bond behavior of a type of FRM comprised of a high performance  
96 mortar and short steel fibers, known as steel fiber-reinforced mortar (SFRM), when applied  
97 onto masonry substrates. The bond behavior was investigated through double shear lap tests  
98 (conducted with two different bonded lengths) and observations on peak load and failure mode  
99 are highlighted. The material is also mechanically characterized by means of flexural,

100 compressive, direct tensile, and residual flexural tests with the aim of obtaining the parameters  
101 required for the numerical modelling presented in the paper.

102

103

## 104 2. MASONRY EXPERIMENTAL CHARACTERIZATION

### 105 2.1. Masonry mortar characterization

106 An M5 class mortar (according to UNI EN 998–2\_2016 [29]) was used for the realization of  
107 the masonry specimens used for the shear lap tests and experimentally characterized. This  
108 mortar consists in a Portland cementitious matrix with hydrated lime. The water required for  
109 the mortar hydration was of around 18% of the mortar weight while the maximum aggregate  
110 size is lower than 3 mm. The mixing procedure was carried out by means of a mixer machine  
111 for three minutes. According to the manufacturer, the workability time of the mortar matrix is  
112 of around two hours. Before the application of mortars, the clay bricks were wetted. After  
113 casting of the joints, the samples were left to dry under environmental conditions.

114 For the mortar characterization, six mortar prismatic elements with 40 x 40 mm of cross-section  
115 and 160 mm length were built in order to evaluate the flexural ( $f_{fm}$ ) and compressive ( $f_m$ )  
116 strength, and the elastic modulus ( $E_m$ ) of the mortar according to standards UNI EN 1015-11  
117 [30] and EN 13412 [31], respectively. In Table 1, the corresponding mean values and  
118 coefficient of variations (CoV) of these parameters are shown.

119 **Table 1.** Mortar mechanical properties.

Material	Density	Compressive strength ( $f_m$ )		Flexural strength ( $f_{fm}$ )		Elastic Modulus ( $E_m$ )	
	[kg/m <sup>3</sup> ]	[MPa]	CoV [%]	[MPa]	CoV [%]	[MPa]	CoV [%]
Masonry joint mortar (28 days)	1807	7.22	9.88	2.22	4.61	3706	16.33
SFRM matrix mortar (28 days)	2402	91.02	1.59	15.43	11.98	24040	22.01

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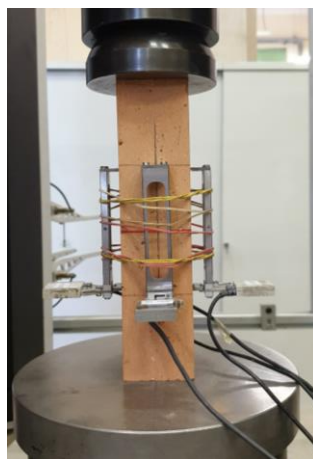
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122           **2.1. Clay bricks characterization**

123 Solid clay bricks (Euroformat type) fired in a furnace near Venice (Italy) were used in the  
124 experimental campaign and were tested to evaluate their compressive and flexural strengths.

125 Three bricks (named A, B, and C) with length ( $l$ ), width ( $b$ ) and height ( $d$ ) shown in Table 2  
126 were tested following the requirements reported in BS EN 771-1:2011 [32]. Before testing, the  
127 clay bricks were subjected to geometrical preparation in order to eliminate any geometrical  
128 imperfection caused by the fired process. With this aim, the specimens were cut to create planar  
129 faces with a circular saw. After cutting, the specimens were leveled again with an abrasion  
130 process aiming to obtain an adequate dimension accuracy.

131 The elastic modulus was evaluated considering three specimens with dimensions 58 x 58 x 233  
132 mm<sup>3</sup> (see Fig. 1). The load was applied in three load cycles considering maximum amplitudes  
133 equal to 7.82, 11.24, and 14.67 N/mm<sup>2</sup>. The elastic modulus was then defined during the last  
134 cycle using four DD1 strain transducers applied in the middle of the four faces of the specimens.  
135 The values of weight, compressive and flexural strengths, and elastic modulus for the specimens  
136 tested and the corresponding mean values and coefficient of variations (CoV) are reported in  
137 Table 2.



138  
139 **Fig. 1.** Elastic modulus for clay bricks.

140 **Table 2.** Brick mechanical properties.

Test	Brick weight [kg]	$l$ [mm]	$d$ [mm]	$h$ [mm]	Compressive strength		Flexural strength		Elastic Modulus	
					[MPa]	CoV [%]	[MPa]	CoV [%]	[MPa]	CoV [%]
A	2.71	245	111	57	46.2		3.69		8850	
B	2.68	243	110	58	40.7		2.76		8750	
C	2.72	245	111	58	45.1		5.73		8500	
Mean value					44.0	6.61	4.06	37.4	8700	2.07

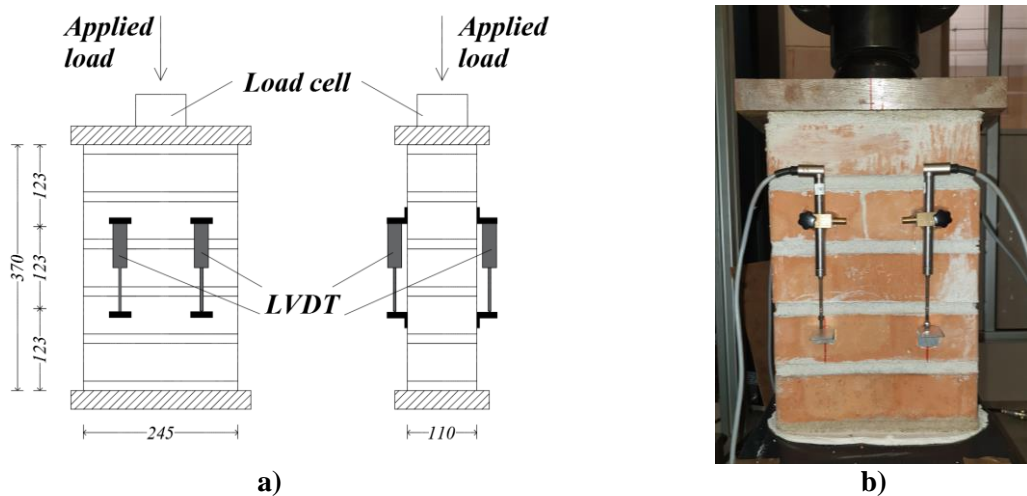
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143  
144

## 2.2. Masonry characterization

145 Three masonry prisms (named MPT), with cross-section dimensions  $l=245$  mm and  $d=110$  mm  
146 and a total height of 370 mm, were built to evaluate the masonry compressive strength ( $f_{c,p}$ ) and  
147 elastic modulus ( $E_p$ ). The prisms included five rows of clay bricks and six mortar joints with an  
148 average thickness of 12 mm, as shown in Fig. 2a.

149 For the masonry prisms, the tests were conducted (according BS EN 1052-1-1999 [33]) using a  
150 uniaxial machine with a cell with a maximum capacity of around 60 tons. The stress was  
151 obtained dividing the applied load by the average cross-section area of the specimen. The strains  
152 were computed as the average value obtained using four linear transducers (LVDTs) placed  
153 onto the masonry and fixed by dowels (Figs. 2a and 2b). The gage length of the LVDTs was  
154 around 1/3 of the specimens' height (Figs. 2a and 2b).

155



156 **Fig. 2.** Masonry uniaxial compression: a) test setup, b) specimen being tested.

157 The masonry prism compressive strength ( $f_{c,p}$ ) was evaluated using following equation:

$$158 \quad f_{c,p} = P_{max}/(l \cdot d) \quad (1)$$

159 where  $P_{max}$  is the maximum applied load recorded during the tests. The elastic modulus ( $E_p$ )  
160 was computed as:

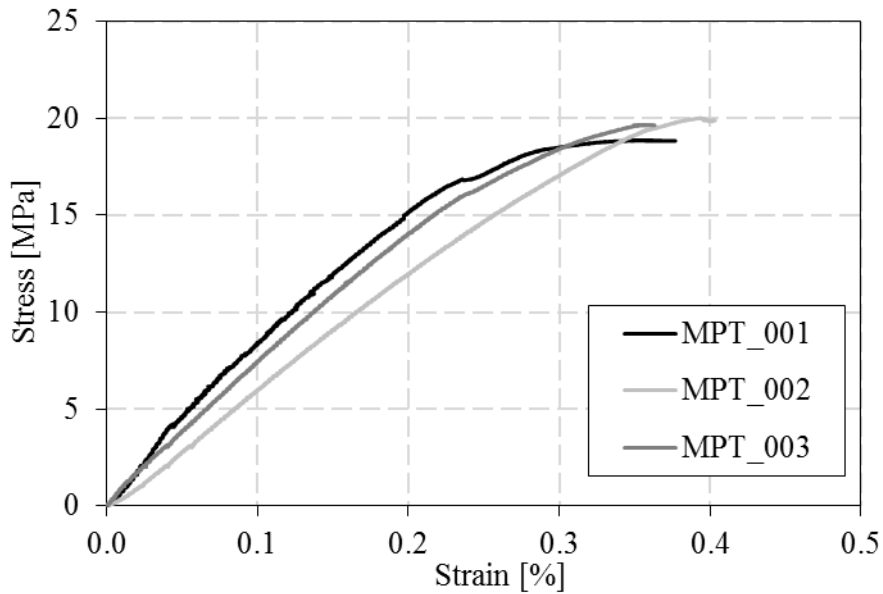
$$161 \quad E_p = \frac{P_{max}/3}{[l \cdot d \cdot \varepsilon(\frac{P_{max}}{3})]} \quad (2)$$

162 Where  $\varepsilon(P_{max}/3)$  is the strain measured at  $P_{max}/3$ . Values of  $f_{c,p}$ , ultimate compressive strain ( $\varepsilon_{u,p}$ ),  
163 and  $E_p$  for the three masonry prisms and the corresponding mean value and coefficient of  
164 variation (CoV) are presented in Table 3. In Fig. 3, the normal stress-strain curves obtained  
165 from the compressive tests are shown.

166 **Table 3.** Masonry prism mechanical properties

	Compressive Strength ( $f_{c,p}$ )		Ultimate compressive strain ( $\varepsilon_{u,p}$ )		Elastic Modulus ( $E_p$ )	
	[MPa]	CoV [%]	[%]	CoV [%]	[MPa]	CoV [%]
MPT_001	18.9		0.377		8800	
MPT_002	20.0		0.403		6100	
MPT_003	19.7		0.363		7500	
Mean value	19.5	2.91	0.381	5.33	7500	18.08

167



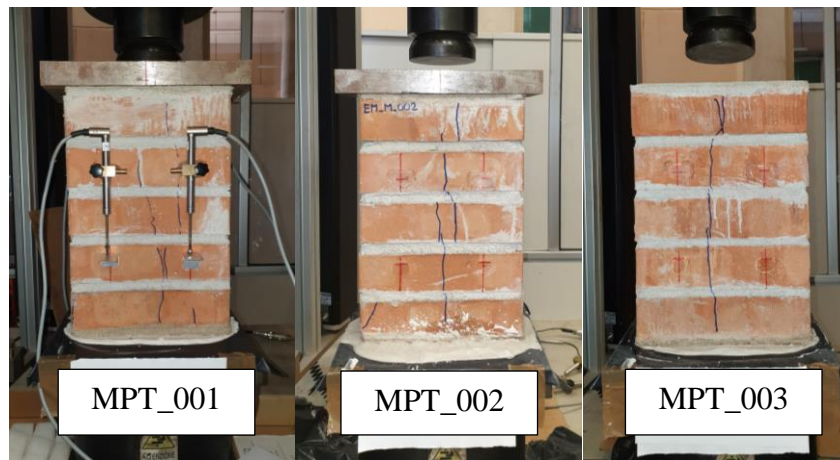
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169

**Fig. 3.** Normal compressive Stress - Strain curves of masonry prisms.



170 As shown in Fig. 4, cracks running parallel to the vertical axis of the specimens and  
171 concentrated mainly at the center of the elements were observed at the end of the test.



172

173

**Fig. 4.** Failure modes of the masonry prisms.

174 The characteristic masonry compressive strength ( $f_{ck,p}$ ) derived from compressive experimental  
175 tests is compared with that found using the analytical formulation (named  $f_{ck,e}$ ) proposed by  
176 Eurocode 6 [34] considering the brick and the mortar compressive strengths experimentally  
177 evaluated. From the analytical formulation proposed by Eurocode 6 [34], the characteristic  
178 masonry compressive strength ( $f_{ck,e}$ ) and the elastic modulus ( $E_e$ ) are obtained from the  
179 following equations:

180 
$$f_{ck,e} = K \cdot f_b^{0.7} \cdot f_m^{0.3} \quad (3)$$

181 
$$E_e = 1000 \cdot f_{ck,e} \quad (4)$$

182 where the coefficient  $K$ , the mortar compressive strength ( $f_m$ ) and the compressive strength of  
183 the brick ( $f_b$ ) are assumed equal to 0.44, 7.22, and 44.0 MPa, respectively. However, the  
184 experimental determination of the masonry characteristic compressive strength (namely  $f_{ck,p}$ )  
185 proposed by standard BS EN 1052-1:1999-[33] includes masonry specimens with vertical joints  
186 (i.e., wallets). Considering that the prisms tested do not include vertical joints (see Fig. 4) the  
187 characteristic masonry compressive strength ( $f_k$ ) is derived from the formulation proposed by  
188 Thamboo et al. 2019 [35]. They found that the masonry characteristic compressive strength of  
189 specimens without vertical joints (prisms) can be considered as 75% of the wallet characteristic

190 masonry compressive strength obtained using specimens with vertical joints. The characteristic  
 191 masonry compressive strength ( $f_{ck,p}=f_{c,p} / 1.2$ ) obtained by prism specimens is equal to 16.3  
 192 MPa, and using the Thamboo et al. 2019 [35] correlation, it is possible to define the wallet  
 193 characteristic masonry compressive strength equal to 12.2 MPa. Moreover, the analytical  
 194 formulation (3) proposed by Eurocode 6 [34] evaluates a masonry characteristic compressive  
 195 strength ( $f_{ck,e}$ ) equal to 11.3 MPa, which is 7.5% lower than the wallet characteristic masonry  
 196 compressive strength.

197

### 198 3. SFRM EXPERIMENTAL CHARACTERIZATION

199 The SFRM material is composed of cement, aggregates, water, superplasticizer and steel fibers  
 200 (see Fig. 5.) with the proportions reported in Table 4 [19]. The steel hooked-end fibers have a  
 201 length  $L_s=30$  mm, nominal thickness  $t_s=0.55$  mm and the mechanical properties reported in  
 202 Table 5.



203

204

**Fig. 5.** SFRM components.

205

**Table 4.** Mix details of SFRM material

Cement	48 % v/v
Water	12 % v/v
Superplasticizer	1 % v/v
Steel fiber	2 % v/v
Aggregates (0 – 3.2 mm)	37% v/v

206

207

**Table 5.** Steel fiber properties

	Standard	Steel fiber length $L_s$ [mm]	Steel fiber nominal thickness $t_s$ [mm]	Steel fiber Elastic modulus [MPa]	Steel fiber tensile strength $f_{fsu}$ [MPa]
Steel fiber (Hooked Ends shape)	EN-14889-1:2006	30	0.55	210000	1345

208

209 The preparation of the SFRM required a rotary mixer that contains 25 kg of the material. The  
 210 cementitious matrix, the steel fibers, and water were placed in the mixer and the mixing  
 211 procedure was held for two minutes. At that point, the superplasticizer was added and the mixing  
 212 was carried out for one more minute. During the mixture process, through visual inspection, it  
 213 was possible to observe that the steel fibers were distributed homogeneously. Vibration of the  
 214 specimens was not needed due to the self-compacting property of the material. In fact, when  
 215 applied to existing structures, vibration of the formwork should be avoided as it can cause  
 216 sedimentation/precipitation of the fibers.

### 217 3.1. Flexural and compressive strength of the SFRM mortar

218 The flexural and compressive strength of the SFRM mortar (i.e., without fibers) was carried out  
 219 following the procedure described in section 2.1 and the results are shown in Table 6. In  
 220 addition, the flexural and compressive strengths of the mortar used for SFRM were evaluated  
 221 at 1, 7, 14, and 21 days after casting. Fig. 6 shows the development of the strengths in terms of  
 222 the percentage of maximum strength obtained at 28 days. Results show that after seven days of  
 223 casting, the evaluated mechanical properties of the mortar are about 80% of the maximum value  
 224 attained at 28 days after casting.

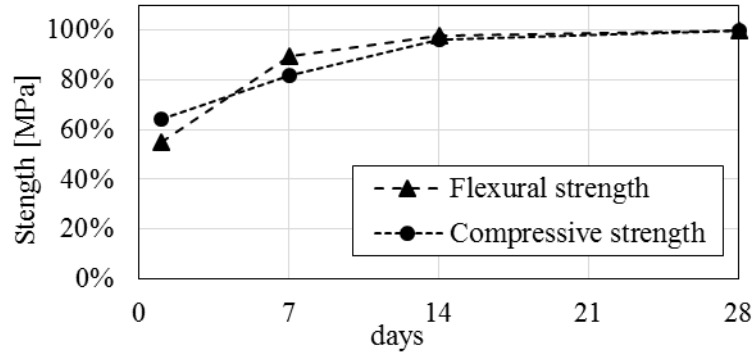


Fig. 6. SFRM mortar Strengths - days.

Table 6. SFRM mortar mechanical properties.

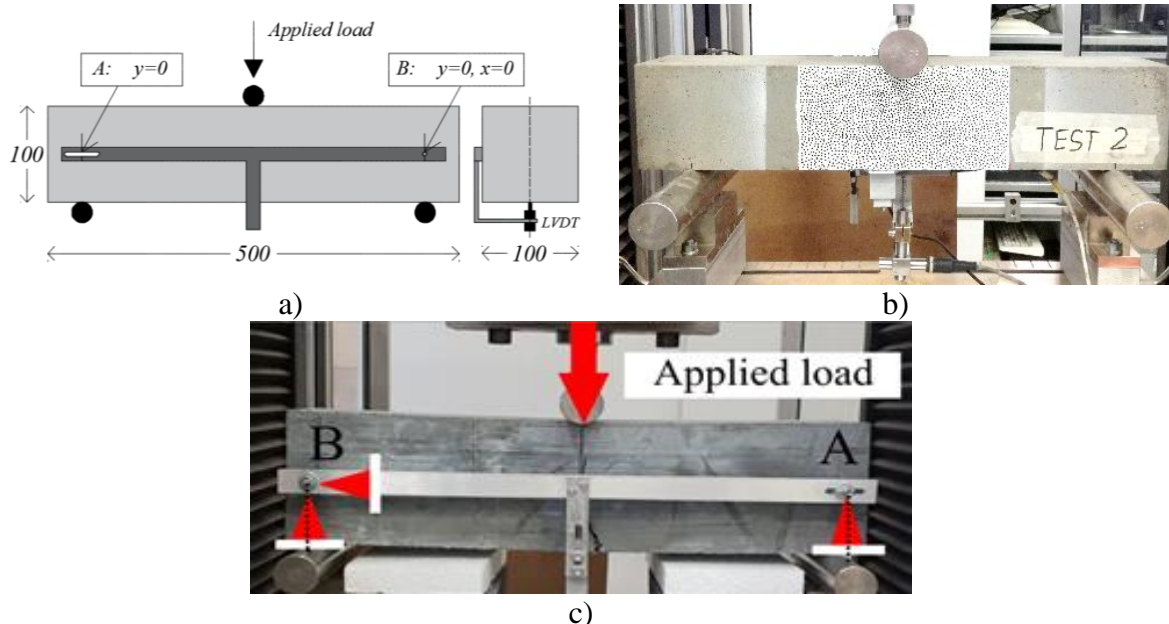
Material	Density [kg/m <sup>3</sup> ]	Compressive strength ( $f_m$ )		Flexural strength ( $f_{fm}$ )		Elastic Modulus ( $E_m$ )	
		[MPa]	CoV [%]	[MPa]	CoV [%]	[MPa]	CoV [%]
SFRM Mortar (28 days)	2402	91.02	1.59	15.43	11.98	24040	22.01

### 3.2. SFRM residual flexural tensile test

As reported in the BS EN 14651-2005 [36], steel fiber reinforced mortars can have different flexural post-elastic behavior (hardening or softening). The SFRM flexural post-elastic behavior depends on the percentage in volume of the steel fibers and it can show a hardening or a softening behavior if the fiber percentage is greater or lower than 2% (CNR-DT 204/2006 [37]), respectively. The SFRM used in this experimental campaign has a fiber volume of around 2% of mortar.

In order to evaluate the SFRM flexural behavior, three-point bending tests were carried out using specimens with dimensions 100 x 100 x 500 mm and shown in Fig. 7. The specimens were cast using a formwork that was removed after 24 hours. The specimens were then covered with a plastic film for 28 days.

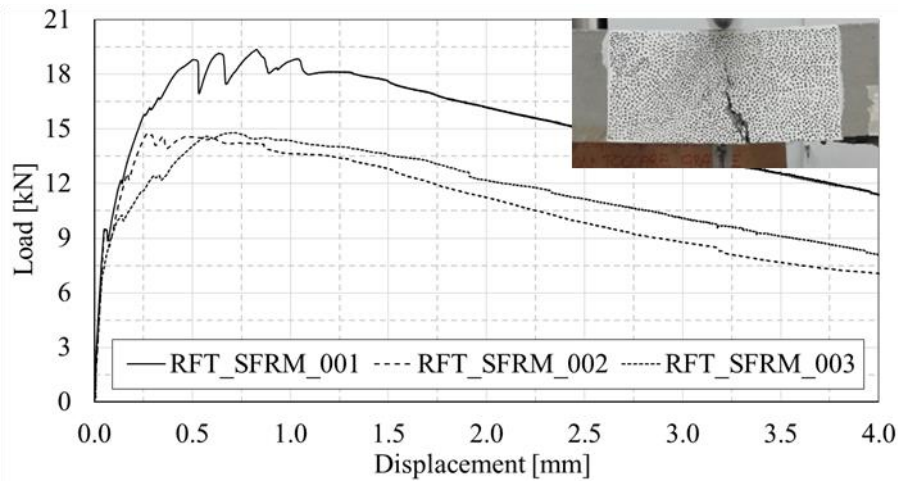
The test set-up used to evaluate the deflection of the specimen consists of a rigid frame with a sliding fixture (“A”,  $y = 0$ ) and a rotating fixture (“B”,  $y = x = 0$ ), as seen in Fig. 7a and Fig. 7c.



244 **Fig. 7.** Residual flexural strength: a) Test setup SFRM; b) Specimen being tested. c) Specimen after  
 245 testing.

246 In Fig. 8, the Load-Displacement curves obtained from the three tests are reported. The  
 247 displacement shown in Fig. 8 corresponds to the mid-span displacement obtained using the  
 248 measurement system represented in Fig. 7b. Fig. 8 also includes the typical crack witnessed at  
 249 the end of the descending branch.

250 From the analysis of the fracture surface, it was observed that the fibers are evenly distributed  
 251 and orthogonal to the fracture. It is possible to conclude that the steel fibers contributed to the  
 252 flexural strength of the specimens because the behavior of SFRM is similar to that observed on  
 253 similar materials with the same amount of fiber volume [19]. In addition, the fracture plane  
 254 spread to the top of the specimen offering residual flexural strength. In the absence of fibers,  
 255 this behavior could not be observed. Furthermore, during the test, after the maximum load is  
 256 attained, it is also possible to observe in Fig.8 the presence of instantaneous load reductions  
 257 with subsequent recovery, which can be associated to the rupture or debonding of the steel  
 258 fibers.

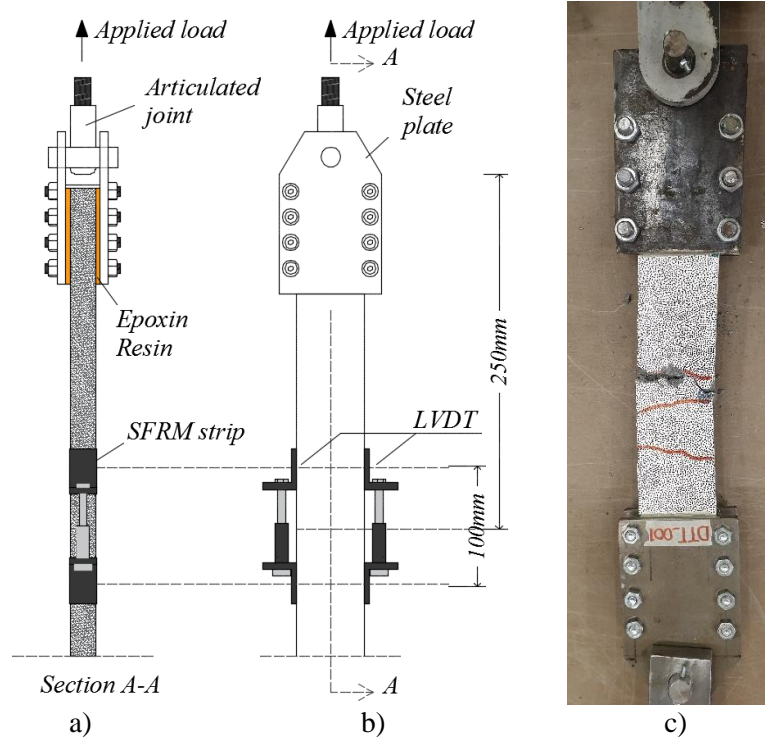


259  
260 **Fig. 8.** Load-Displacement curves for SFRM specimens.

261 **3.3. SFRM direct tensile test**

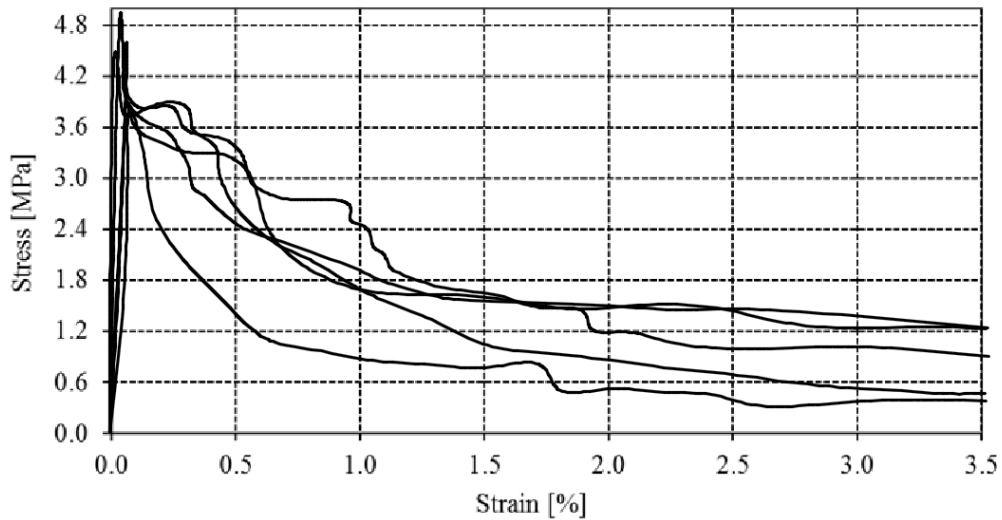
262 In order to investigate the direct tensile strength of the SFRM, direct tensile tests were carried  
263 out. The specimens were cast using a formwork with the following dimensions: 500mm of  
264 height, 80 mm of width, and 30 mm of thickness. The SFRM composite material was cast  
265 considering the direction of the fibers where the principal direction coincides with the direction  
266 of the applied load. After casting, the specimens were covered with a plastic film in order to  
267 maintain the humidity constant for 28 days and tested using a non-standard test setup showed  
268 in Fig. 9.

269 The SFRM specimens were anchored on both sides with steel plates. Epoxy resin was applied  
270 between the specimen and the steel plates to avoid any slip phenomenon (Fig. 9a). The tensile  
271 force was applied to the specimen through two articulated joints that avoid the presence of  
272 bending moments in the SFRM strip during testing (Fig. 9b). Two LVDTs placed at the middle  
273 height of the lateral sides of the specimen were used to investigate the strain of the SFRM strip  
274 (Fig. 9a-b). The measuring length of the instruments is equal to 100 mm.



275 **Fig. 9.** Direct tensile test: a) Anchorage system with epoxyn resin and steel plates; b) testing setup, c)  
 276 failure mode.

277 In Fig. 10 the stress-strain curves of the five direct tensile experimental tests carried out are  
 278 reported. To obtain the stress-strain curves, only the specimens which shown a fracture within  
 279 the gage length (equal to 100 mm as shown in Fig. 9) were considered. The material shows a  
 280 first elastic branch on the stress-strain curve due to the matrix and steel fibers working together.  
 281 After the peak of stress is attained, the subsequent strain is due only to the tensile steel fiber  
 282 strength. As a simplification, the stress is calculated considering the entire section area instead  
 283 of the steel fiber. The mean stress peak value of the direct tensile test corresponds to 3.98 MPa  
 284 (see Table 7) with a strain of around 0.078%.



285

286

**Fig. 10.** Stress-Strain curves derived from direct tensile tests.

287

**Table 7.** SFRM direct tensile test.

Specimen	Tensile strength		Corresponding Strain	
	[MPa]	CoV [%]	[%]	CoV [%]
DTT_SFRM_001	3.43		0.0781	
DTT_SFRM_002	4.15		0.0861	
DTT_SFRM_003	3.08		0.0612	
DTT_SFRM_004	3.83		0.0793	
DTT_SFRM_005	4.51		0.0862	
Mean value	3.98	14.23	0.0782	13.05

288

289

### 3.4. Smooth and simplified tensile strength curves

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The mean smooth stress-strain curve derived from direct tensile tests is compared with the

291

simplified mean curve obtained from the analysis of the residual flexural tensile test results

292

(Fig. 11). The average tensile stress-strain curve derived from the results of the residual flexural

293

tests was evaluated according to the BS EN 14651-2005 [36] and it is shown in Fig. 11. This

294

curve also includes values of tensile strength  $f_{Fi}$ , serviceability tensile residual strength  $f_{Fts}$ , and

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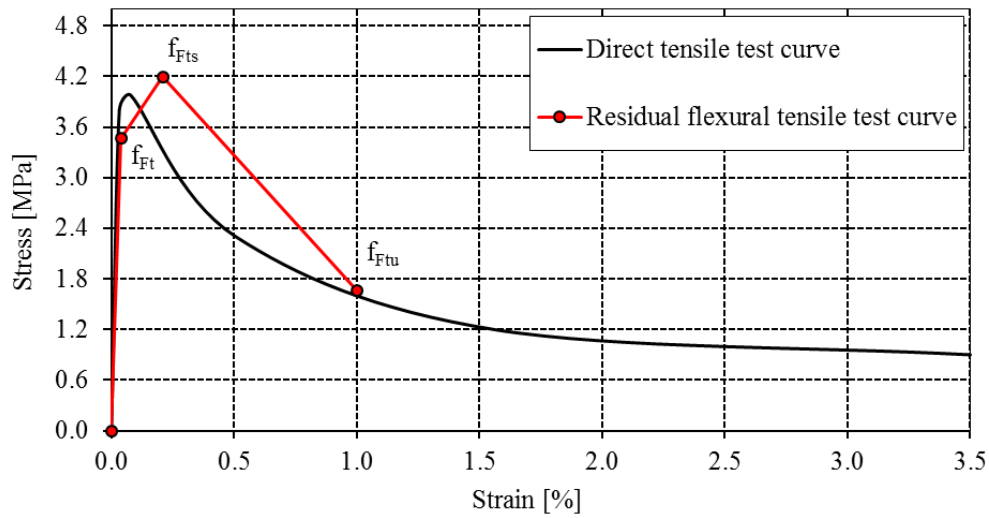
ultimate tensile residual strength  $f_{Ftu}$  (see Table 8). As can be seen in Fig. 11, the first and third

296

points of that curve are closer to the direct tensile stress-strain curve than the second point.



297 Finally, it is important to underline that the SFRM material shows a tensile strength reduction  
 298 around 50% after a large strain (around 1%).



299  
 300 **Fig. 11.** Stress-Strain smooth mean curves derived from direct tensile tests and residual flexural tensile  
 301 tests.

302 **Table 8.** SFRM Residual flexural strength test results.

Material	$f_{Ft}$		$f_{Fts}$		$f_{Ftu}$	
	[MPa]	CoV [%]	[MPa]	CoV [%]	[MPa]	CoV [%]
RFT_SFRM_001	3.79		4.82		2.28	
RFT_SFRM_002	3.79		3.93		1.14	
RFT_SFRM_003	2.81		3.84		1.58	
	3.46	16.34	4.20	12.91	1.66	34.49

303  
 304 As can be seen in Table 8, the dispersion of the results (tensile strength  $f_{Ft}$ , serviceability tensile  
 305 residual strength  $f_{Fts}$ , and ultimate tensile residual strength  $f_{Ftu}$ ) carried out from the three points  
 306 bending tests (according to the BS EN 14651-2005 [36]) is quite high with respect to the CoV  
 307 obtained from the masonry mortar tests (Table 6). This result depends on the randomness of the  
 308 SFRM materials that is a consequence of the random distribution of the steel fibers within the  
 309 mortar matrix [38, 39].

310

311

312 **4. SFRM-MASONRY BOND BEHAVIOR**

313 The results reported in section 3 show the SFRM material has high compressive and tensile  
314 strength with respect to a masonry material and shows a ductile tensile behavior. The  
315 effectiveness of this strengthening system is intrinsically dependent on the bond performance  
316 between the SFRM material and the masonry substrate and this issue requires further  
317 investigation.

318 Considering a masonry cross-section with a bottom or a top layer of SFRM strengthening, the  
319 bond actions depend on the type of forces applied to the SFRM and on the curvature of the  
320 masonry element. In general, such bond actions are tangential (i.e., shear) and normal stresses  
321 applied at the masonry-SFRM interface [40]. In this experimental campaign, double shear lap  
322 tests were performed in order to investigate the existence of an effective bond length ( $L_b$ ), the  
323 failure mode, and the shear bond stress developed at the masonry-SFRM- interface. Due to the  
324 test set-up, the presence of normal stresses is not expected.

325 In this article, the effective bonded length ( $L_b$ ) is defined as it has been reported for other types  
326 of composites externally bonded to concrete or masonry (concrete structures strengthened with  
327 FRP [40, 41], FRCM [42-44], and masonry structures strengthened with FRP [45, 46], FRCM  
328 [47-49]). The double shear lap tests performed in this experimental campaign were developed  
329 using the specimens shown in Fig. 12.



330

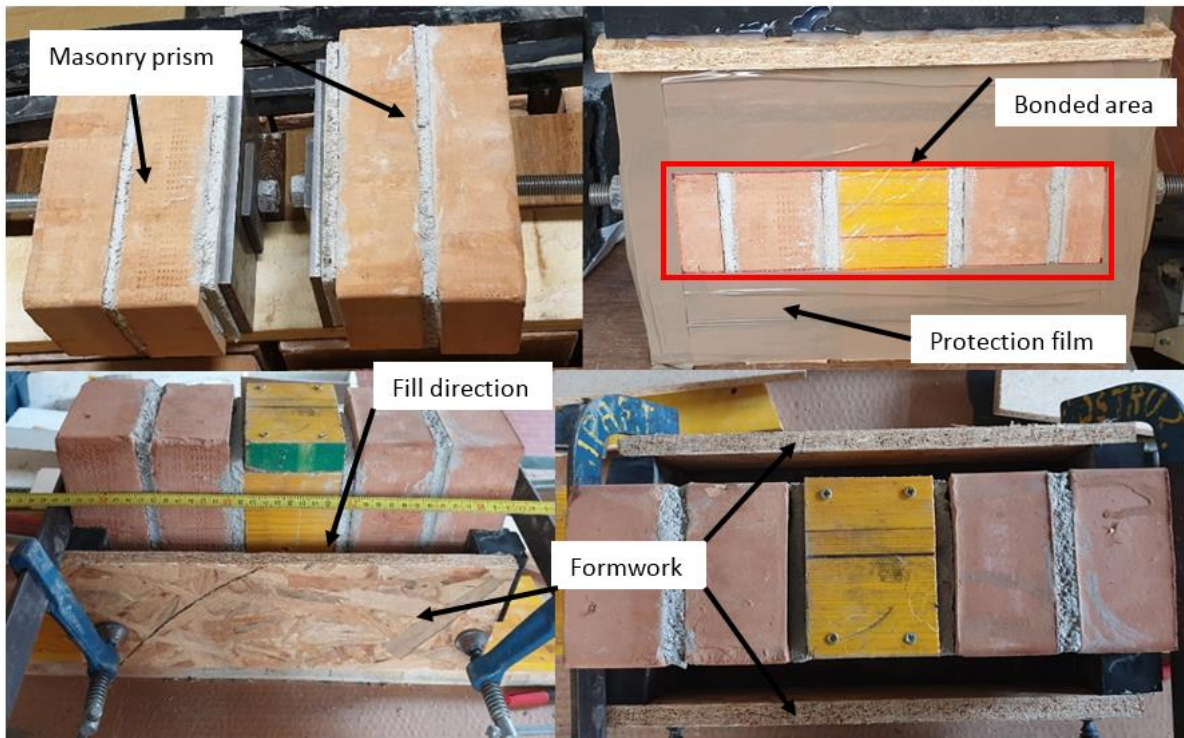
331

**Fig. 12.** Double shear lap test specimens.

332 Considering a strip of SFRM with bonded width ( $b$ ) and bonded length ( $L$ ), the effective bonded  
333 length ( $L_b$ ) can be defined as a length where the forces in the SFRM strip are transferred to the  
334 masonry substrate through shear stresses in the interface between two materials. If the bonded  
335 length is greater than  $L_b$  the composite material is able to transfer the maximum load to the  
336 masonry. This maximum load, as will be shown in the following, depends on the shear failure  
337 mode of the bonded material.

338 The specimens were prepared in three different phases. First, two masonry prisms were made  
339 over a horizontal steel plane parallel to the mortar joints. Then, a timber element was used to  
340 keep the two prisms 100 mm apart (Figure 13a). A protection film was applied to the specimens'  
341 surface, with the exception of the bonded area. In this way, the area in which the SFRM strip  
342 was applied was delimited. Two formworks were built and then positioned laterally as shown  
343 in Figure 13. The thickness of the SFRM strip was guaranteed by means of hard rubber elements  
344 with a thickness of 30 mm located between the wood formwork and the specimen. The SFRM  
345 matrix was then cast and the formworks were removed after 14 days. The tests were performed  
346 after 28 days of casting. The application of the SFRM to the masonry substrate was carried out  
347 without any previous surface preparation as former experimental evidence [24] demonstrated  
348 that an adequate bond between the SFRM and the substrate was obtained in that condition.

349



350

351

**Fig. 13.** Double shear lap test specimens' preparation.

352

The two-masonry prisms, connected by two SFRM strips placed on the two sides of the masonry element, have a hole (Fig. 13) where a steel bar is inserted and connected to a steel plate at the bottom of the masonry specimen (Fig. 13). In this manner, it is possible to apply the load as a pressure to the steel plate connected to the steel bar and then to the masonry specimen (Fig. 14).

355

356

The test was conducted in displacement control defined with a rate equal to 0.5 mm/min. Four

357

LVDTs were used to define the displacement between the two ends of the masonry prisms, as

358

can be seen in Fig. 12. The LVDTs record the variation of the distance  $c$  with the application

359

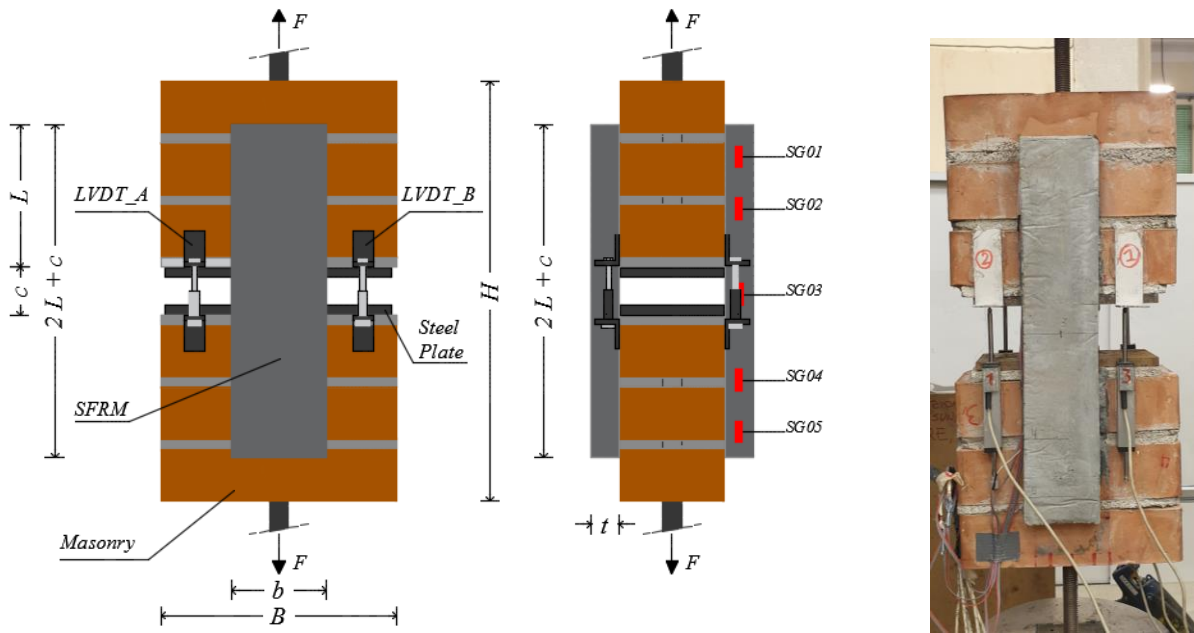
of the imposed displacement. In addition, five strain gauges were applied to the middle

360

thickness of the strip in order to evaluate the variation of strain along with the composite layer

361

for each value of imposed displacement (see Fig. 14a).



**Fig. 14.** Double shear lap tests: a) Test setup, b) specimen being tested.

362

363

364 The SFRM strip has 30 mm of thickness ( $t$ ) and 80 mm of width ( $b$ ), and two different bond

365 lengths ( $L$ ) are considered (100 mm and 150 mm). The entire specimen has 540 mm of total

366 height ( $H$ ), and the distance ( $c$ ) between the masonry triplets connected with SFRM strip is 100

367 mm. The masonry specimens have a cross-section equal to the brick dimensions (245 mm x

368 110 mm). The tests are named following the convention  $DSL\_SFRM\_X\_Z$  where DSL

369 represents the test type considered (double shear lap test), SFRM is referred to the composite

370 material investigated,  $X$  is the bonded length considered, and  $Z$  is the numbering of the test. For

371 the bonded lengths ( $L$ ) 100 mm and 150 mm three and six specimens were tested, respectively.

372 In Table 9, the values of maximum load attained during testing ( $F_{max}$ ), the maximum global

373 shear stress ( $\tau_{g,max} = F_{max} / (2 \cdot L \cdot b)$ ) and the failure mode observed for each test are reported.

374 Three failure modes were observed (see Fig. 15):  $D$ , detachment of the SFRM strip to the

375 masonry substrate (Fig. 15a);  $C$ , cracking of the SFRM strip (Fig. 15b); and  $CD$ , cracking of

376 the SFRM with cracks that running parallel to the interface and SFRM detachment (Fig. 15c).

377

378

379

**Table 9.** SFRM Double shear lap test

Specimen	$L$ [mm]	$F_{max}$ [kN]	$\tau_{g,max}$ [MPa]	Failure mode
DSL_SFRM_100_001	100	9.01	0.56	<i>D</i>
DSL_SFRM_100_002	100	10.50	0.66	<i>D</i>
DSL_SFRM_100_003	100	12.13	0.76	<i>D</i>
DSL_SFRM_150_001	150	18.14	0.76	<i>C</i>
DSL_SFRM_150_002	150	7.67	0.32	<i>D</i>
DSL_SFRM_150_003	150	19.86	0.83	<i>CD</i>
DSL_SFRM_150_004	150	17.85	0.74	<i>C</i>
DSL_SFRM_150_005	150	17.93	0.75	<i>C</i>
DSL_SFRM_150_006	150	19.72	0.82	<i>C</i>

380

381 Experimental results show that the bonded length of 100 mm is insufficient to develop the shear  
382 stress necessary to guarantee the transfer of the maximum force from the SFRM to the masonry  
383 substrate. In fact, the average value of the maximum global shear stress ( $\tau_{g,max}$ ) reached for 100  
384 mm bond length is equal to 0.66 MPa (Table 9) which is lower than the value obtained from  
385 the tests with 150 mm of bond length (0.78 MPa). With this last bonded length, the specimens  
386 showed cracking failure, and a perfect shear stress transfer was observed (with the exclusion of  
387 specimen *DSL\_SFRM\_150\_002* that shows an early detachment). The mean maximum load  
388 reached for the specimens with  $L=150$ mm (with exclusion of *DSL\_SFRM\_150\_002*) is equal  
389 to 18.70 kN. The corresponding average normal stress in the strip cross-section is equal to 3.89  
390 MPa which is only 2.2% lower than the average tensile strength (evaluated by direct tensile  
391 tests and reported in Table 7). This result means that if the bonded length is equal to or greater  
392 than effective bonded length, there is a perfect force transfer from SFRM to masonry because  
393 the observed failure mode involves in the tensile rupture of the strengthening and detachment  
394 is not observed (Fig. 15).

395

396

397

398           **4.1. Shear lap test failure modes**

399   The failure mode registered for the bonded length equal to 100 mm is the detachment of the  
400   SFRM strip from the masonry substrate (Failure mode “*D*”), as shown in Fig. 15a. Therefore,  
401   the bonded length of 100 mm is considered insufficient to have the perfect transfer of the stress  
402   from SFRM to masonry.

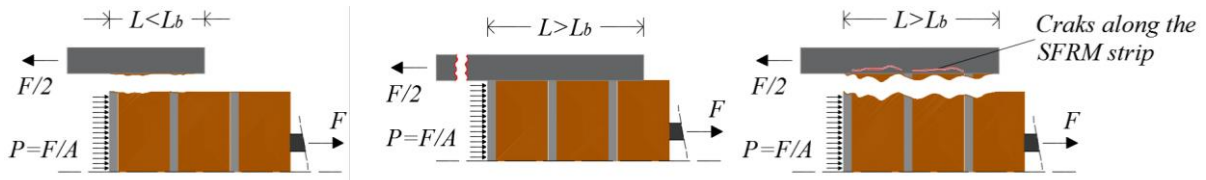
403   For the bonded length equal to 150 mm, results show three different failure modes: four  
404   specimens show cracking of SFRM in the unbonded region until the tensile rupture of the  
405   SFRM without detachment of the composite from the substrate (Failure mode “*C*”, Fig. 15b);  
406   one specimen (test DSL\_SFRM\_150\_003) shows cracking along the SFRM strip in the bonded  
407   and unbonded area cracks until the detachment of the composite material from the masonry  
408   (Failure mode “*CD*”, Fig. 15c); one specimen (test DSL\_SFRM\_150\_002) shows an early  
409   detachment of the SFRM from the masonry (Failure mode “*D*” , Fig.15a).

410   Test DSL\_SFRM\_150\_002 was not considered in the results analysis because it showed an  
411   early detachment corresponding to an applied load of 7.67 kN (see Table 6) which is lower than  
412   the average maximum load (18.70 kN) registered for the other specimens with  $L=150$  mm. This  
413   could be justified because after a visual inspection of the specimen, it was observed that the  
414   strip surface was not completely bonded to the masonry surface. In addition, the reason for the  
415   type of failure witnessed for specimen DSL\_SFRM\_150\_002 can also be attributed to a small  
416   misalignment (i.e., eccentricity with respect to the machine axis) of the sample that might have  
417   caused a concentration of stresses on one of the strips causing its earlier detachment.

418   Test DSL\_SFRM\_150\_003 reached a maximum load (19.86 kN, see Table 9) which is similar  
419   to the results obtained for the remaining specimens, even if it shows a different failure mode  
420   (see Table 9).



421



a)



b)



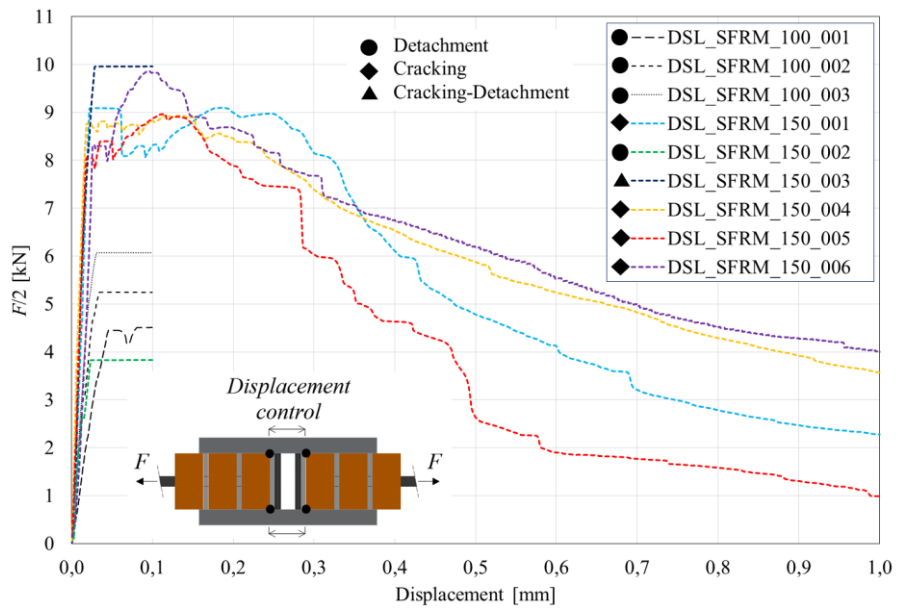
c)

422 **Fig. 15.** Failure modes obtained from the double shear lap tests: a) DSL\_SFRM\_100 failure mode  
 423 “D”; b) DSL\_SFRM\_150\_ (001, 004, 005, 006) failure mode “C”; c) DSL\_SFRM\_150\_003 failure  
 424 mode “CD”.

425 **4.2. Shear lap test behavior**

426 In Fig. 16a, the Applied load in the strip ( $F/2$ )–Displacement diagram obtained from all the  
 427 double shear tests are reported. The displacement evaluated during the experimental test  
 428 represents the variation of the distance ( $c$ ) between the two masonry prisms ends that in the  
 429 unloaded condition is equal to 100 mm (see Fig. 16a). The tests with  $L=100$  mm were stopped  
 430 after the detachment of SFRM (Fig. 16a). Tests with  $L=150$  mm show an initial elastic branch  
 431 before the cracking of SFRM (see Fig. 16a). Then, a non-linear branch, similar to that witnessed  
 432 during the direct tensile tests and reported in Fig. 10, is observed. In Fig. 16b the Applied load  
 433 -Global slip curves are presented until the failure mode. The slip value reported in Fig. 16b is  
 434 equal to half of the mean displacement evaluated by LVDTs minus the SFRM strip elongation  
 435 (evaluated considering the strain registered by the strain gauge in the middle of the strip).

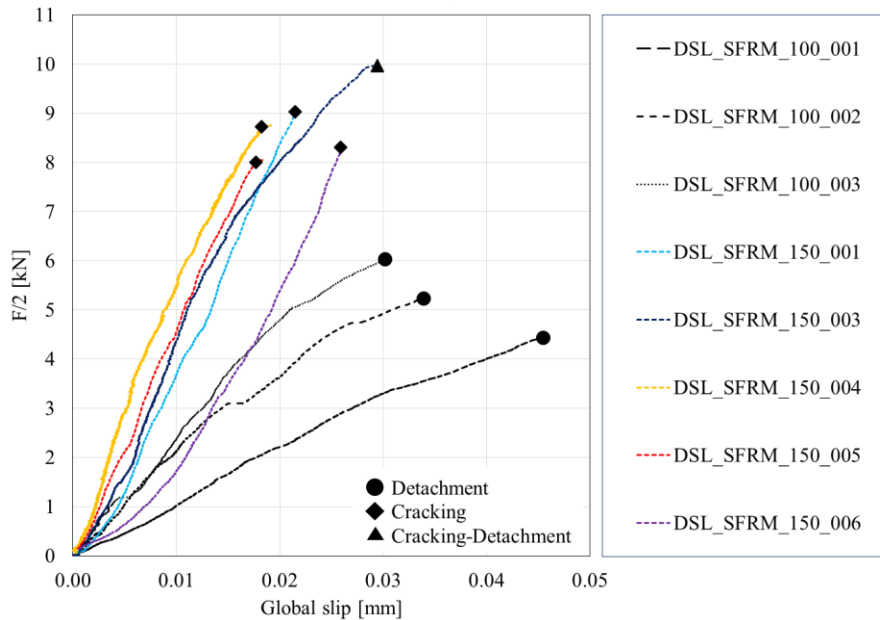




436

437

a)



b)

438

439

440

**Fig. 16.** Double shear lap test results: Applied load - Displacement diagrams a) Entire experimental

441

curves b) Load-Global slip curve until specimen failure.

442

Results in Fig. 16b show that the curves with (C) failure mode present a mean global slip of

443

around 0.022 mm while the (D) failure mode of around 0.037 mm. In Fig.16b, it is possible to

444

see that specimens with 150 mm of bonded length have a higher initial stiffness compared to

445

that of specimens with 100 mm of bonded length, i.e., specimens with 100 mm of bonded length

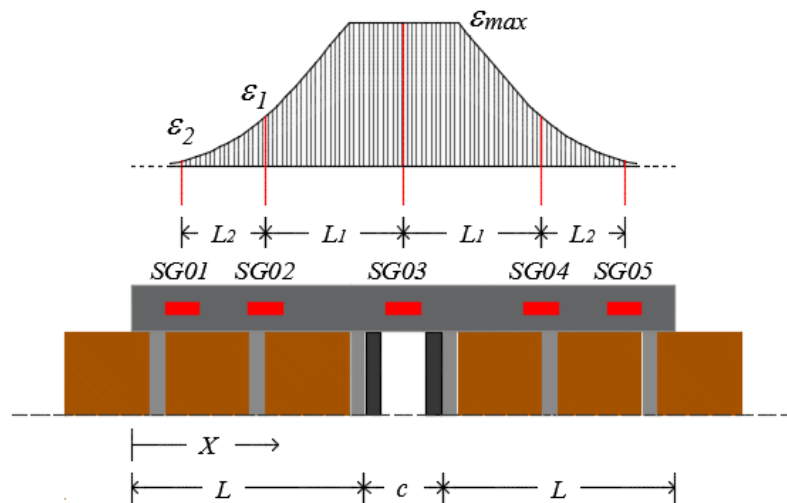
446

show higher global slip displacements for the same amount of applied load when compared to

447 specimens with 150 mm of bonded length. This behavior is explained when it is considered that  
 448 for specimens with lower values of bonded length, the tangential stress reaches its maximum  
 449 value for a lower applied load, and the global slip increases more rapidly.

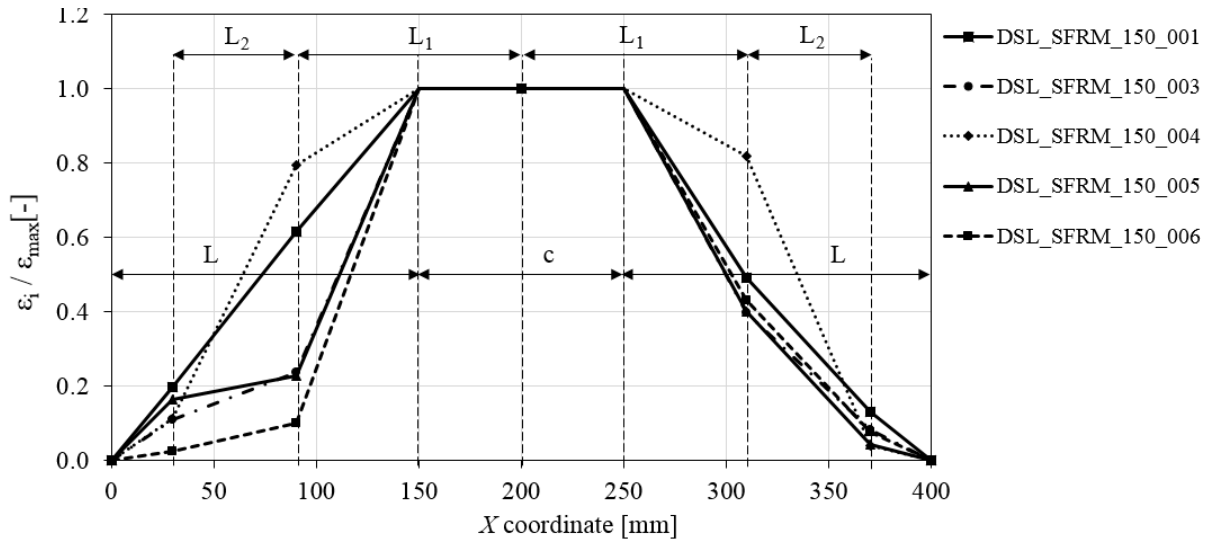
#### 450 4.3. Stress – Strain development along the SFRM strip

451 Five strain gauges were used with the aim to determinate the strain distribution along the bond  
 452 length of the SFRM strip during tests DSL\_SFRM\_150 (001, 003, 004, 005, and 006). The  
 453 strain gauges were applied to the middle thickness of the strip (Fig. 17): one at the middle span  
 454 of the strip (SG03), SG02 and SG01 were respectively applied at  $L_1$  (110 mm) and at  $L_1+L_2$   
 455 (170 mm) from the SG03. SG04 and SG05 were applied in the symmetrical position with  
 456 respect to SG02 and SG01.



457  
 458 **Fig. 17.** Disposition of the strain gauges used in tests DLS\_SFRM\_150.

459 The results in terms of strain from tests with a bonded length ( $L$ ) equal to 150 mm are reported  
 460 in Fig. 18. The strain distribution from test DSL\_SFRM\_150\_002 was not included since results  
 461 from this test were disregarded. The strain values ( $\epsilon_i$ ) at the maximum load reached during the  
 462 experimental test are normalized with respect to the maximum strain ( $\epsilon_{max}$ ) reached in the  
 463 middle of the strip of the corresponding test.



464

465

**Fig. 18.** Normalized strain distribution carried out from the DSL\_SFRM\_150 tests.

466

As it can be seen in Fig. 18, maximum values of the strain are observed in the unbonded region and decrease to the bonded strip ends.

467

## 468 5. NUMERICAL CALIBRATION

469

In this section, a detailed numerical investigation is presented with the aim of simulating the experimental results described above. Numerical analyses were developed through finite element models considering the non-linear behavior of the materials. In the following, the different numerical strategies used to reproduce the compressive tests of the masonry prism, the SFRM tensile tests, and the double shear lap tests are discussed.

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474

The numerical model were made using CQ16M 2D plane stress elements. This type of elements were used for the masonry mesh and also for the SFRM material mesh. The quadratic interpolation and Gauss integration type were adopted for the eight-node quadrilateral isoperimetric plane stress elements. The nonlinear system was solved with iteration type and for the iteration scheme a modified Newton-Raphson algorithm with 0.01 energy norm was used. The elements have an average area of around 250mm<sup>2</sup> (with the exclusion of the elements used for the discretization of the masonry mortar joints reported in Fig. 19a).

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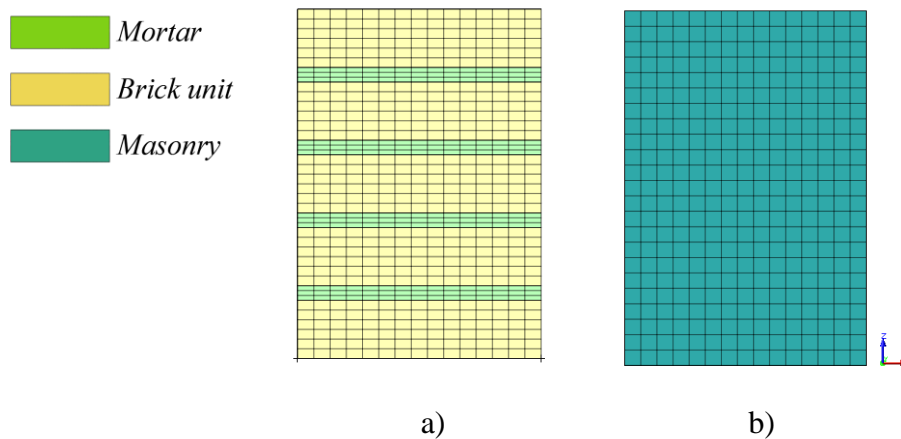
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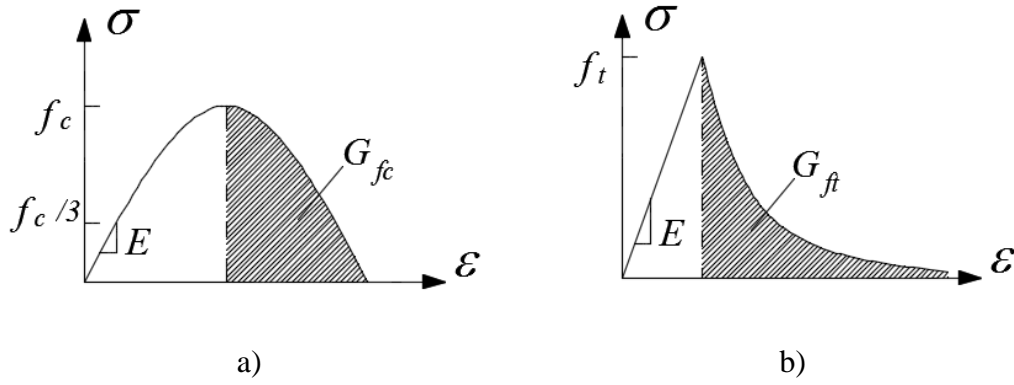
481

The FE model used in the numerical analysis is mesh depending. For this reason, different numerical models with different mesh sizes were developed with the aim of obtaining reliable

483 results. The mesh dimension was chosen considering a compromise between a good agreement  
484 with the experimental test and computational time. Moreover, the average mesh dimension was  
485 calibrated on the base of experimental test results in order to avoid results localizations [50].  
486 The masonry compressive tests were numerically studied considering the simplified micro-  
487 modelling approach shown in Fig. 19a where mortar and bricks were separately discretized and  
488 the “Total Strain Crack Model” (TSCM) was used as non-linear constitutive law of the  
489 materials. Parabolic stress-strain diagrams (see Fig. 20a) were used to consider the compressive  
490 behavior of mortar and bricks and linear elastic with exponential softening laws (Fig. 20b) were  
491 used for modelling the tensile behavior of the materials.  
492 These stress-strain relationships, shown in Fig. 20b, were defined according to the parameters  
493 in Table 10: Elastic Modulus ( $E$ ), material compressive strength ( $f_c$ ), material tensile strength  
494 ( $f_t$ ), compressive fracture energy ( $G_{fc}$ ) and tensile fracture energy ( $G_{ft}$ ). Results from the  
495 simplified micro-modelling approach were compared with the experimental results and with  
496 those of a macro-modelling approach (Fig. 19b) where masonry was considering as continuum  
497 material.



498 **Fig. 19.** Masonry prism models: a) simplified micro-modelling approach; b) macro-modelling  
499 approach.

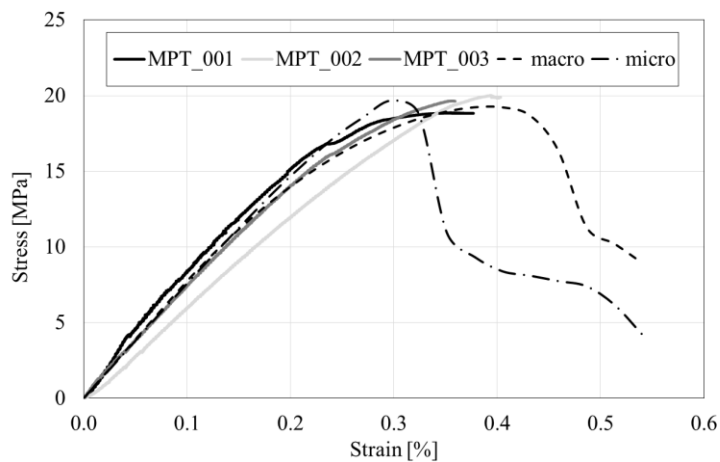


500 **Fig. 20.** Stress-strain curves used for the numerical analysis a) parabolic function; b) linear with  
 501 exponential softening function.

502 **Table 10.** Material mechanical properties of masonry numerical models.

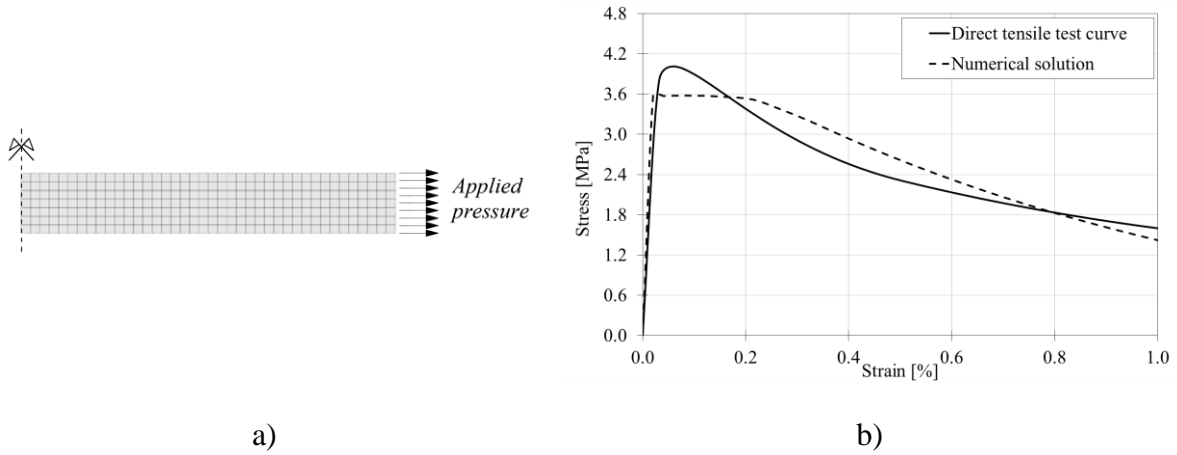
Material	Density [kg/m <sup>3</sup> ]	$E$ [MPa]	Compression			Tension		
			$f_c$ [MPa]	$G_{fc}$ [N/mm]	Function type	$f_t$ [MPa]	$G_{ft}$ [N/mm]	Function Type
Brick unit	1700	8700	44.0	8	parabolic	3.00	0.01	exponential
Masonry joint mortar	1770	3700	7.22	8	parabolic	2.22	0.01	exponential
Masonry SFRM matrix mortar	1714	7500	19.5	-	parabolic	4.06	3.00	exponential
SFRM matrix mortar	2400	24000	91.0	-	E-P	3.6	9.00	exponential

503  
 504 From Fig. 21, it is possible to observe that the initial stiffness corresponding to the elastic branch  
 505 is similar for the micro and macro model curves and those obtained experimentally. In addition,  
 506 the macro model shows a descending branch more ductile respect to the micro model.



507  
 508 **Fig. 21.** Stress strain result of the masonry prisms, numerical analysis - experimental test results.

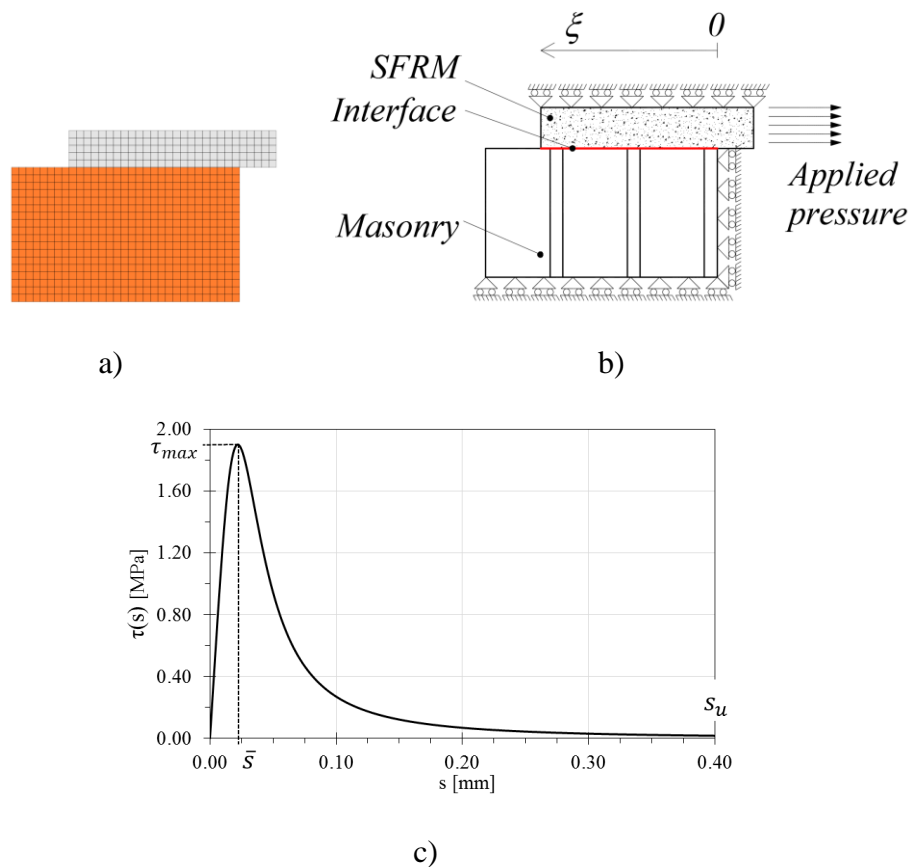
509 The SFRM was discretized with finite elements (Fig. 22a) and its tensile stress-strain curve  
510 (assumed in the TCSM) was calibrated considering a linear elastic branch with an exponential  
511 softening curve (Fig. 20b). The tensile fracture energy ( $G_f=9 N/mm$ , Table 10) was calibrated  
512 in order to obtain a good correspondence between numerical and experimental stress-strain  
513 curves of the tensile behavior of SFRM strip as reported in Fig. 22b. This calibration analysis  
514 has considered a strain range between 0% and 1% that is defined from the stress-strain reported  
515 in Fig. 8 and obtained from residual flexural tests. The SFRM compressive stress-strain law  
516 used is an elasto perfectly plastic (E-P) curve defined considering the experimental values of  
517 the elastic modulus and the compressive strength ( $E$  and  $f_c$ ) reported in Table 10.



518 **Fig. 22.** Tensile tests modelling: a) Discretization of SFRM material with finite elements; b) Stress -  
519 Strain result for the numerical solution compared with the direct tensile test curve (experimental).  
520 Lastly, the bond behavior between SFRM and the masonry substrate was investigated using the  
521 finite element model illustrated in Fig. 23a. Fig. 23a shows the mesh used, the boundary  
522 conditions (Fig. 23b) and local stress ( $\tau(s)$ )-slip ( $s$ ) curve implemented in the bond-slip interface  
523 type inserted between masonry and SFRM composite material (Fig. 23c). In the bond-slip  
524 interface, a local tangential tress  $\tau(s)$ -slip ( $s$ ) curve to calibrate the parameter of the well-known  
525 equation proposed by Popovics et al. 1973 [51] was implemented:

$$526 \quad \tau(s) = \tau_{max} \frac{s_p}{s} \frac{n}{(n-1) + \left(\frac{s}{s}\right)^n} \quad (5)$$

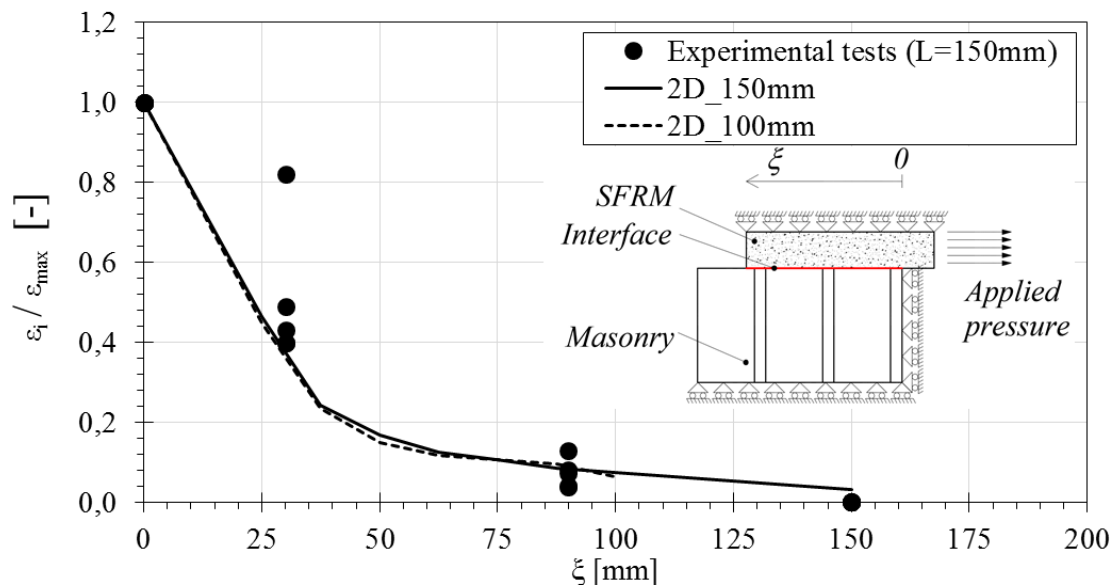
527 where the ultimate slip  $s_u$  is equal to 0.4 mm (according to CNR-DT 200 R1/2013 [52]),  $\bar{s}$   
 528 (0.022 mm) is the slip corresponding to the peak value of the tangential stress ( $\tau_{max}=1.9 \text{ N/mm}^2$ ),  
 529 finally the factor  $n$  in equation (5) is assumed equal to 3.  
 530 The interface element between SFRM and masonry has zero thickness [53] and the slip zone  
 531 was described with a bond-slip interface model, which has a constitutive law based on the  
 532 “Total Deformation Theory” [54]. This theory expresses the bond strength as a function of the  
 533 relative tangential displacement ( $s$ ) between the two materials. The normal tension ( $t_n$ )  
 534 parameter was considered rigid, while the relationship between the tangential stress ( $\tau$ ) and the  
 535 relative tangential displacement is assumed to be non-linear (Figure 22).



536 **Fig. 23.** a) Shear lap test model b) Boundary conditions and load applied to the F.E. model c) Local  
 537 bond–slip curve implemented in the bond-slip interface element.

538 Fig. 24 shows the dimensionless strain  $\varepsilon_i / \varepsilon_{max}$  in the middle thickness of the SFRM strip as a  
 539 function of the coordinate  $\zeta$  (from 0 mm to 150 mm). The numerical results obtained

540 considering a bonded length ( $L$ ) equal to 100 mm and 150 mm were compared with those  
 541 obtained from the strain gauges used in the DSL\_SFRM\_150 experimental tests (Fig. 24).  
 542 The dimensionless normal strain is maximum when for  $\xi = 0$  and is equal to zero for  $\xi \geq L_b$  as  
 543 reported in Fig. 24. The numerical simulation confirms that  $L=100$  mm is lower than the bonded  
 544 length because for  $\xi=100$  mm strain is different from zero. Moreover, it is possible to see from  
 545 Fig. 24 that the numerical strain distribution is comparable to the experimental one.

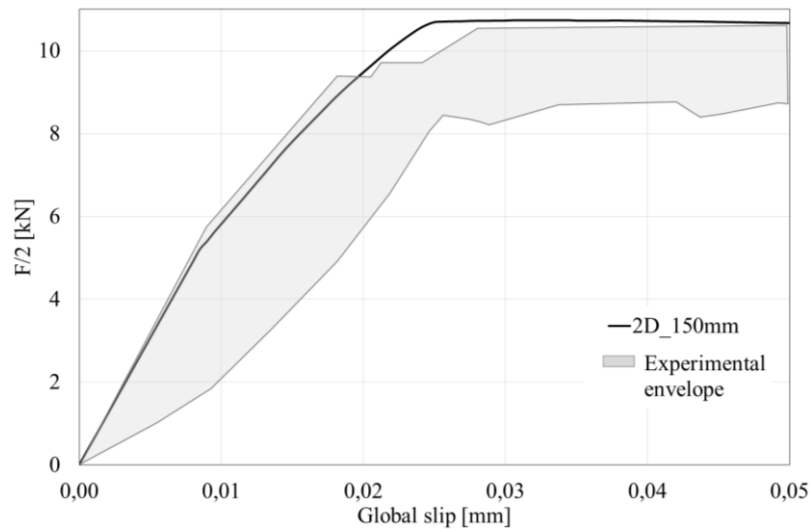


546  
 547 **Fig. 24.** Dimensionless strain –  $\xi$  coordinate. Experimental and numerical results.

548 The load – global slip curves have been compared with the numerical simulation results until  
 549 0.05 mm of global slip. Fig. 25 shows the experimental envelope for the tests with bonded  
 550 length equal to 150 mm, without considering the test DSL\_SFRM\_150\_002. The numerical  
 551 simulation has a good agreement with the envelope of experimental results. The value of the  
 552 maximum load obtained from the numerical analysis was equal to 10.73 kN while the average  
 553 maximum load for the experimental tests was 9.35 kN.

554





555

556 **Fig. 25.** Load – global slip curves Experimental envelope - Numerical results (2D\_150mm)

557

## 558 6. FURTHER DEVELOPMENTS

559 The results presented in this paper corresponds to a first attempt to gain knowledge on the bond  
 560 behavior of SFRM composites applied onto masonry substrates but need to be validated when  
 561 more experimental data become available, as they are strictly related to the mechanical and  
 562 geometric properties of the specimens tested. These results are intended to provide tools for  
 563 future practical applications of the material as strengthening system and to help researchers to  
 564 plan future experimental tests that focus on variables not studied here.

565 For instance, the presence of a bonded length, as demonstrated by the shear lap tests, implies  
 566 that the system can be applied to structural members with limited size. However, aspects such  
 567 a possible size effect and the influence of the thickness and width of the strips on the expected  
 568 values of effective bonded length need to be considered and investigated.

569 It is also worth noting that the most common type of failure mode observed for specimens with  
 570 bonded length equal to 150 mm (i.e., cracking of the SFRM strip without detachment) suggests  
 571 that the behavior of the material might be independent of the type of substrates onto which it is  
 572 applied. In this case, however, it is important to verify how the state of conservation of the  
 573 masonry or its strength will affect the final behavior.

574 Another interesting outcome of this work is related to the fact that it was possible to achieve  
575 the maximum tensile strength of the SFRM when it was applied onto a masonry surface without  
576 any previous preparation. These results suggest that a perfect bond between the two materials  
577 might be achieved even without the need of additional application procedures. From the point  
578 of view of the practical application of the SFRM as strengthening system, this characteristic of  
579 the material will significantly reduce its cost and time of application. However, future research  
580 on the topic should validate this finding by means of tests that investigate the effect that the  
581 surface substrate characteristics (age, irregularities, etc.) might have on the bond behavior  
582 between masonry and SFRM.

583 Finally, it is also hoped that the information included in this paper, that comprises the  
584 characterization of all the materials involved will allow researchers to plan their experimental  
585 campaigns based on the preliminary numerical analysis carried out using the parameters herein  
586 presented.

587 It is also important to underline that, considering a masonry cross-section with a bottom or a top  
588 layer of SFRM strengthening, the bond actions depend on the type of forces applied to the  
589 SFRM and on the curvature of the masonry element. In general, the bond actions are tangential  
590 and normal stresses applied at the masonry-SFRM interface.

591

## 592 **7. CONCLUSIONS**

593 In this paper, the behavior of steel fiber reinforced mortar (SFRM) strips applied onto masonry  
594 substrates was studied experimentally and numerically with the aim of gaining insight on the  
595 behavior of masonry structures strengthened with SFRM composites. In addition, a mechanical  
596 characterization of the material was performed. Mechanical properties studied included  
597 compressive, tensile, and residual flexural strength. The main conclusions that can be drawn  
598 from this study are as follows:

- 599       • Evolution of the compressive strength of the high-performance mortar used in SFRM  
600       shows that after 7 days, the compressive and flexural strength of the matrix attained is  
601       around 80% of that witnessed after 28 days of casting.
- 602       • Comparison of tensile stress-strain curves obtained from the direct tensile and residual  
603       tensile test performed on SFRM showed a similar behavior, with an initial elastic branch  
604       followed by a softening behavior after peak stress.
- 605       • The bond behavior between the masonry substrate and SFRM composite, investigated  
606       through double shear lap tests, showed three different failure modes: detachment of the  
607       SFRM strip from the masonry substrate; cracking of the SFRM strip; and a combination  
608       of both, depending on the used bonded length. Detachment from the substrate was  
609       observed for specimens with a bonded length equal to 100 mm, while for bonded lengths  
610       equal to 150 mm, cracking of the strip with or without detachment was witnessed.
- 611       • For a bonded length equal to 150 mm, values of the maximum applied load obtained  
612       during the shear lap tests are similar to those attained on direct tensile tests. This result  
613       and the observed failure mode suggest that 150 mm can be considered as the effective  
614       bonded length for the SFRM composite studied in this paper, as a full exploitation of  
615       the material is reached.
- 616       • The strain profile along the length of the SFRM strip, at the maximum applied load, for  
617       specimens with bonded length equal to 150 mm, shows that maximum values of strain  
618       are observed at the middle of the strip (unbonded area). An exponential decrease in the  
619       strain is then observed, with values close to zero reached at the end of the strip.
- 620       • The comparison between experimental and numerical shear lap test results show that  
621       the strain profile along the SFRM strip obtained from the numerical simulations is  
622       similar to the observed experimental behavior.

623

624 **8. CONFLICT OF INTEREST STATEMENT**

625 The authors declare that there is not conflict of interest

626 **9. ROLE OF THE FUNDING SOURCE**

627 This research was not supported by funding source

628 **10. ETHICAL APPROVAL**

629 The authors approve the ethical aims of the journal

630 **11. ACKNOWLEDGEMENTS**

631 Eng. P. Napolitano and Mr. L. Martin are gratefully acknowledged for providing the SFRM  
632 composite material.

633

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