

1 **Mantle flow entrained by the Hindu Kush continental**
2 **subduction inferred from source-side seismic anisotropy**

3
4 **Cheng-Chien Peng¹, Ban-Yuan Kuo², Manuele Faccenda³,**
5 **and Ling-Yun Chiao¹**
6

7 ¹ Institute of Oceanography, National Taiwan University, Taipei, Taiwan

8 ² Institute of Earth Sciences, Academia Sinica, Taipei, Taiwan

9 ³ Dipartimento di Geoscienze, Università di Padova, Padova, Italy

10
11 Corresponding author: Ban-Yuan Kuo (byk@earth.sinica.edu.tw)
12

13 **Hightlights:**

- 14 • Circular pattern of shear wave splitting was found around the Hindu Kush slab
- 15 • Such pattern can be induced by either slab rollback or subduction entrainment
- 16 • The subduction entrainment is likely the primary cause
- 17 • A-type olivine with strong orthorhombic anisotropy is needed in the entrainment model

18
19 **Keywords:**

20 Continental subduction, sub-slab mantle, slab breakoff, subduction entrainment, seismic
21 anisotropy, Hindu Kush

22
23 **Abstract**
24

25 The intermediate-depth seismicity below the Hindu-Kush orogen is thought to mark the Indian-
26 plate subduction with the bottom half of the slab currently breaking off. Unique features of this
27 continental subduction are the near-vertical slab and the roughly stationary convergence boundary.
28 How this subduction affects the mantle flow patterns remains to be understood. In this study we
29 measured source-side shear wave splitting on the S waves from Hindu Kush intraslab events to
30 sample the surrounding mantle. The observed fast polarization directions exhibit a circular pattern
31 around the slab resembling that predicted for the toroidal flow driven by slab rollback. However,
32 the rollback scenario is not favored because it hardly sustains in dynamic models without a
33 considerable retreat of convergence boundary. We propose that the observed pattern is produced
34 by the sub-vertical shear flow entrained by the steep descent of the slab and the ongoing breakoff.
35 This scenario requires the existence of A-type or AG-type olivine fabrics with strong orthorhombic
36 anisotropy in mid- to lower upper mantle, which is consistent with the global models of azimuthal
37 and radial anisotropy. This interpretation circumvents the debate on the cause of trench-parallel
38 anisotropy in some oceanic subduction zones where slab entrainment and rollback may coexist,
39 and supports the notion that orthorhombic anisotropy of olivine may play an important role in
40 shaping mantle anisotropy.

41

42 **1. Introduction**

43

44 1.1 The Hindu Kush-Pamir mountain belt

45 The collision of the Indian sub-continent with the Eurasian plate created the Himalaya and Tibetan
46 plateau with a well-illuminated underthrusting of the Indian crust and lithosphere (Schulte-Pelkum,
47 2005; Nábelek, et al., 2009). In the eastern Himalayan syntaxis, the Indian indentation produced

48 large-scale lateral extrusion of the Eurasian crust and lithosphere without an obvious trace of deep
49 subduction. Around the western edge of the Indian indenter lies the Hindu Kush (HK) and Pamir
50 mountain belt, where intermediate-depth earthquakes extend to 250 km depth (Fig. 1). This seismic
51 zone has been linked to the subduction of either of the two continental plates, as geological and
52 geophysical evidence has ruled out the involvement of the Tethyan oceanic lithosphere (Burtman
53 and Molnar, 1993; Sippl et al., 2013; Schnieder et al., 2013; Li et al., 2018).

54
55 The seismicity-depicted slabs are near-vertical beneath the Hindu Kush (Sippl et al., 2013) and
56 dipping southward beneath the Pamir (Schneider et al., 2013). Whether the seismicity arises from
57 subduction of the Indian or the Eurasian plate has been debated (e.g., Burtman and Molnar, 1993;
58 Pavlis and Das, 2000; Sippl et al., 2013). Up to date, the Pamir's Eurasian origin has become
59 widely accepted (Schnieder et al., 2013) because of the apparent southward dipping. The steep
60 geometry of the HK slab, however, has rendered its provenance less certain. Recent tomographic
61 imaging (Kufner et al., 2016) suggests the association of the HK slab with the Indian plate based
62 on the spatial relationship between the high velocity anomalies and the seismicity. P wave images
63 reveal that the Hindu Kush slab reaches 600 km depth, much deeper than the terminal depth of the
64 seismicity at 250 km. The shape of the velocity anomalies, together with the kinematics of the
65 earthquake sources, suggest that the aseismic part of the slab is in the process of breaking off
66 (Kufner et al., 2017).

67
68 Previous studies have suggested a wide range of evolution models for the HK-Pamir double
69 verging system. The Pamir subduction might have commenced at 15-25 Ma (Sobel et al., 2013)
70 with a northward retreating plate boundary over a distance of 300 km, now at the Main Pamir

71 Thrust (Fig. 1). The Indian subduction in the Hindu Kush has been thought to start either at 8 Ma
72 (Negredo et al., 2007) or slightly predating 11 Ma (Kufner et al., 2016). In contrast to the Pamir,
73 the HK convergence boundary has remained roughly stationary (Replumaz and Tapponnier, 2003).
74 However, the straightening of the slab may be partially caused by the “trench” (hereafter we use
75 trench to represent the convergence plate boundary in the HK region) advancing pushed by the
76 Indian indentation, implying that the boundary might have even migrated northward over a short
77 distance (Liao et al., 2017). The continental subduction in general, and the HK-Pamir two-slab
78 system specifically, have attracted modeling efforts mainly on the dynamic evolution of the slab
79 or its impact on the orogen evolution (e.g., Duretz et al., 2012; Duretz and Gerya, 2013;
80 Krystopowicz and Currie, 2013; Liao et al., 2017). How the continental subduction together with
81 the breakoff may shape the mantle dynamics in the region has remained poorly understood.

82

83 1.2 Shear wave splitting and sub-slab dynamics

84 Compared to continental subduction, the mantle response to oceanic subduction has been widely
85 investigated primarily using the observations of seismic anisotropy. Seismic anisotropy is a
86 phenomenon resulting from systematic alignment of intrinsically anisotropic minerals through
87 crystal viscous deformation. One of the most direct forms of anisotropy is shear wave splitting
88 (SWS), which involves separation of an S-wave phase into two quasi phases polarized in planes
89 parallel to the directions of fast and slow velocity of the anisotropic medium. For vertically incident
90 S waves, SWS observations map the anisotropy in planform. SKS is the most commonly utilized
91 phase for SWS observations due to its advantage that the observed anisotropy is known to be
92 associated with the upswing path. The provenance of anisotropy can be further narrowed down to
93 upper mantle according to SKS sensitivity kernels computed for different anisotropic parameters

94 (Sieminski et al., 2007). In principle, teleseismic direct S phase can be used as long as the path is
95 sufficiently vertical. In the source-side anisotropy approach using direct S wave, receiver-side
96 anisotropy is usually constrained by SKS splitting and removed (e.g., Russo and Mocanu, 2009;
97 Long, 2013). Both SKS and source-side anisotropy studies have helped to delineate the structures
98 of the mantle disturbed by oceanic subduction zones (e.g., Long, 2013).

99

100 In sub-slab mantle, slab entrainment and rollback together generate a 3D flow. Observed
101 anisotropy with fast directions perpendicular to subduction zone trenches is often attributed to the
102 slab entrainment or the poloidal component of the 3D flow, whereas trench-parallel splitting is
103 thought to result from the rollback-induced toroidal flow (e.g., Long, 2013; Faccenda and
104 Capitanio, 2012; 2013). This interpretation in which each flow component is responsible for one
105 particular anisotropy pattern has been appealing because it involves only one type of deformation
106 pattern for olivine (the most abundant mineral in the upper mantle), i.e., A-type lattice preferred
107 orientation (LPO), which is characterized by the easy slip system [100](010), in which olivine a-
108 axis [100] is parallel to the shear direction and b-axis perpendicular to, or the b-plane (010) parallel
109 to, the shear plane (e.g., Karato, 2008). However, the association of trench-parallel anisotropy
110 solely with the toroidal flow has recently been challenged. Song and Kawakatsu (2012; 2013)
111 argued that some of the trench-parallel anisotropy observations can be explained instead by
112 subduction entrainment of the asthenosphere if the slab is sufficiently steep. Walpole et al. (2017)
113 proposed a similar model with the term of “tilted transverse isotropy (TTI)” to explain the trench-
114 parallel pattern in the sub-slab mantle. Lynner and Long (2014) asserted that the trench-parallel
115 splitting tends to occur in old subduction zones where toroidal flow dominates while the trench-
116 normal splitting characterizing most of the young subduction zones are driven by slab entrainment.

117 Different LPOs of olivine, such as C-type with [001](100) and E-type with [100](001) (e.g., Karato,
118 2008), may also play important roles in shaping anisotropy patterns in the sub-slab mantle (Lynner
119 et al., 2017). The sub-vertical slab of HK could serve as a continental test site on the controversies
120 inherited from oceanic subduction zones.

121

122 In this study we conduct source-side shear wave splitting analysis for the HK region, which allows
123 mapping of the deformation structure surrounding the subduction zone (e.g., Russo and Silver,
124 1994; Long, 2013). An earlier attempt of this kind in this region (Schoenecker et al., 1997)
125 employed limited data and provided preliminary interpretations. In a recent study using SKS across
126 the HK-Pamir orogenic belt (Kufner et al., 2018), the splitting exhibits mainly ENE trending fast
127 polarization directions suggesting an indentation-escape process in the lithosphere and
128 asthenosphere. Here we analyze a large set of source-side SWS data in the HK subduction zone to
129 constrain the dynamics in mid- to lower upper mantle surrounding the HK slab that is independent
130 of the lithospheric processes related to the development of the orogen.

131

132 **2. Data and method**

133

134 Our data set consists of 58 new measurements of source-side anisotropy for 32 events in the HK
135 subduction zone in a depth range of 70-240 km with sources primarily concentrated at 100 and
136 200 km depths. We assume that the down-going S waves from the HK subduction zone sample
137 the anisotropy mainly in the depth range from the source to 410 km, because in the transition zone
138 single crystal wadsleyite has much lower anisotropy than olivine (Zhang et al., 2018). The event
139 magnitudes range from Mw 5.5 to 7.3, and epicentral distances from 41 to 74° (Details of events

140 and stations used can be found in Supplementary Table S1). The most common practice in the
141 receiver-side correction is to remove the anisotropy constrained by the SKS splitting. It is thus
142 critical that the SKS splitting data represent properly the overall upper mantle properties beneath
143 the station, which can be azimuthally dependent and even varying with depth. In their studies,
144 Lynner and Long (2014) and Mohiuddin et al. (2015) have selected stations that show SKS
145 splitting reasonably uniform under sufficient azimuthal coverage such that the upper mantle
146 anisotropy beneath the station can be well characterized by one set of splitting parameters,
147 including the null solutions. This ensures that the SKS-based receiver-side correction is unbiased
148 for direct S waves from all azimuths. In this study, we used 11 stations, which are all noted in these
149 two previous studies as having either null or simple form of azimuthal anisotropy that can provide
150 proper receiver-side correction (see Table S1).

151
152 Another issue about receiver-side correction is the possible bias by neglecting the effect of radial
153 anisotropy in the upper mantle beneath the station. As the incidence angle increases, direct S is
154 more sensitive to the radial anisotropy than SKS. Our past experience indicates that the sensitivity
155 is a complex function of backazimuth and polarization direction, and that, even though when
156 individual measurements differ substantially with and without radial anisotropy in the receiver-
157 side correction, the overall pattern of SWS largely remains. This is because, in the case we
158 examined, the multiple sources and paths used render random scatters from the original splitting
159 that together do not shift the pattern in any systematic way. Moreover, radial anisotropy models
160 themselves carry uncertainties. In this study, we do not consider the effect of radial anisotropy in
161 the receiver-side correction.

162

163 The standard routine of receiver-side correction involves rotating the NS and EW components of
164 S wave to the fast and slow directions at the station determined from SKS anisotropy
165 measurements, closing the time shift (δt) between the two phases, and rotating the waveforms
166 back to the NS and EW directions. After the correction is finished, we apply our SWS measurement
167 routine (e.g., Kuo et al., 2012; Kuo et al., 2018; details to be discussed below and in Supplementary)
168 to obtain the splitting parameters ($\phi_r, \delta t$), where ϕ_r is the fast direction on the receiver side. One
169 unique step in the source-side splitting approach is the geometrical correction that translates ϕ_r
170 in the station frame to ϕ in the source frame using $\phi = \alpha + \beta - \phi_r$ (Nowacki et al., 2015),
171 where α is the azimuth of the S wave at the source and β is the backazimuth at the receiver.
172 Examples of measurement are shown in Fig. 2. The quality control criteria follow that practiced
173 by Kuo et al. (2018) for SKS, which includes a comparison between results from rotation-
174 correlation and minimum Eigenvalue methods (details in Supplementary). In this study, the
175 splitting parameters from the minimum eigenvalue method are reported. The last step of the quality
176 control in Kuo et al. (2018) is to require small deviation of the recovered particle motion from the
177 SKS great-circle path. For source-side anisotropy, this step is replaced by comparing the final
178 particle motion against that calculated from centroid-moment tensor (CMT) solution of the source
179 (e.g., Ekström et al., 2012). We abandoned those with the difference greater than 15° (Fig. 2; Fig.
180 S1 in Supplementary). We also determined the null solutions following the approach of Wüstefeld
181 and Bokelmann (2007) (Supplementary). The comparison with the nulls are explained below.

182

183 **3. Pattern of source-side splitting**

184

185 Fig. 3 shows the pattern of shear wave splitting plotted at locations 200 km down dip from
186 respective earthquakes along the S wave paths traced in iasp91 global velocity model (Kennett and
187 Engdahl, 1991) using the TauP program (Crotwell et al., 1999). The eight measurements from
188 Schoenecker et al. (1997) were included in this figure. Measurement results are summarized in
189 Table S2. The prominent features are the consistent alignment of fast polarization direction ϕ in
190 parallel with the general trend of the trench on the Indian side in group A and a clustering of ϕ
191 oblique to the trench northwest of the HK on the Asian side in group B. Group C consists of a
192 small number of measurements with paths crossing the back of the Pamir subduction zone
193 (northern side), yielding scattered results although with an apparent EEW majority. Group D
194 samples the east of HK and the south of the Pamir. From D1 to D2, ϕ exhibits a rotation from
195 normal to oblique with respect to the strike of the Pamir slab.

196
197 The patterns of ϕ in groups A, B, D1 and D2 are in general compatible with that of the null
198 solutions, which is an independent constraint on the reliability of the measurements (Fig. S2).
199 Furthermore, group A consists of three stations of null anisotropy straddling from oceanic hotspot
200 (RER) to the margin of the craton in southern Africa (LSZ), yet the observed splitting directions
201 are highly consistent as shown in the rose diagram in Fig. 3, implying that the observed splitting
202 originates from near-source structures. In other groups, stations do not spread in space like in group
203 A so that this argument does not apply. Nonetheless, the stringent quality control, the general
204 agreement with the nulls, the selection of stations from Lynner and Long (2014) and Mohiuddin
205 et al. (2015), and the implication from group A together lend us confidence that our measurements
206 are reliable and their source-side origin is valid.

207

208 Three-dimensional visualization shows that the S waves sample the upper mantle surrounding the
209 steep HK seismic zone (Fig. 4). The delay times are 1 – 3 s (Fig. S3), which would need an S wave
210 traveling for 100-400 km long in a 3-4% anisotropy domain. To estimate how slab anisotropy may
211 contribute to the final results, we calculate the path length of the S wave traveling inside the slab
212 compared with the total length from the source to the 410 km depth. We use 1, 1.5, and 2% velocity
213 perturbations in Kufner et al.'s (2016) tomographic model to define the outer boundary of the slab.
214 As this threshold increases, the path length through the slab decreases. Low threshold pushes the
215 boundary towards the surrounding mantle where fossil anisotropy may not sustain. Overall, there
216 is no correlation of splitting parameters with the slab path length. For 1.5 and 2%, the S waves in
217 groups A and B rarely travel through any slabs, while group D still has high percentage of paths
218 in the Pamir slab (Fig. S4). There is no direct evidence for the presence of frozen-in anisotropy in
219 the HK or Pamir subduction zones. If it is any hint, Kufner et al.'s (2018) local-event and
220 teleseismic SKS anisotropy measurements show ESE- and ENE-oriented ϕ for crust and
221 lithosphere, respectively, north of the plate boundary. If these fabrics remain frozen-in after the
222 Pamir subduction, then this hypothetical fossil ϕ are at odds with the observations of D group.
223 Details of possible slab effect is discussed in Supplementary (Fig. S4). We assume that groups A,
224 B, and D primarily detect the deformation in the mid- to lower upper mantle surrounding the HK
225 subduction zone.

226

227 Groups A and D exhibit little depth dependence of splitting parameters, while in B, ϕ rotates
228 roughly from NS to NE-SW and δt slightly decreases with event depth (Fig. S1). While groups
229 A and D agree well with the null solution, in B, one peak of ϕ is consistent with the majority of
230 the null solutions and the other peak deviates from the nulls by about 30° . Group B probably

231 samples more complex mantle structures than A and D. Nevertheless, the overall orientations of
232 ϕ in the NE-SW quadrants is believed to be a robust feature. In comparison, group C is composed
233 of much fewer data than other groups, and we defer the interpretation of the pattern presented by
234 group C until more data are available.

235

236 **4. Interpretations**

237

238 4.1 Slab rollback

239 Different mechanisms may be involved in producing the observed anisotropy pattern. First, **groups**
240 **A and B** together are consistent with that expected for A-type LPO of olivine aligned by the
241 toroidal flow from sub-slab to supraslab mantle (Fig. 5a). This would require a southward rollback
242 of the HK slab probably throughout its relatively short subduction history (scenario 1). The model
243 of Faccenda and Capitanio (2012, 2013) predicts that olivine LPO develops in two domains in sub-
244 slab mantle giving different anisotropy: trench-normal right beneath the slab in the entrained
245 mantle, and trench-parallel at greater depth where rollback imposes toroidal flow. The strength of
246 the trench-parallel anisotropy within the latter domain increases progressively toward the slab
247 lateral margins where the divergence of the toroidal flow (and deformation) is larger. Their models
248 therefore predict strong trench-parallel SKS splitting in that domain as observed in many studies
249 (e.g., Baccheschi et al., 2007; Foley and Long, 2011; Lynner and Long, 2013). The source-side
250 anisotropy in this study may result from the toroidal flow in the deeper part of the sub-slab mantle.

251

252 Group D covers the region where the two slabs are close to each other, with the wave paths grazing
253 the high velocity core of the lower part of the westernmost Pamir slab (Fig. 4). The apparent

254 rotation in ϕ from D2 to D1 may be related to the same toroidal flow associated with the HK slab
255 that turns counter-clockwise around the eastern edge. On the other hand, the possible northward
256 rollback of the Pamir slab may induce its own toroidal flow that wraps both slab edges. Once
257 turning to the Pamir wedge side (south), both toroidal branches may join the corner flow there to
258 form trench-normal anisotropy (Faccenda and Capitanio, 2012, 2013). Although this is consistent
259 with D1, it should occur inside the mantle wedge, not much beneath it. The rollback of the Pamir
260 slab may also drive material around the slab tip, but this poloidal type of flow seems difficult to
261 provide large scale, consistent deformation fabrics over depths (e.g. MacDougall et al., 2017)
262 detectable by SWS.

263

264 4.2 Subduction entrainment

265 Another possible mechanism to cause the observed anisotropy pattern is the alignment of A-type
266 olivine with strong orthorhombic anisotropy by vertical flow entrained by the subduction (Scenario
267 2) (Fig. 5b). Strong orthorhombic anisotropy for both P and S waves is produced by combining
268 azimuthal anisotropy (Aa) with a significant, positive radial anisotropy (Ra) $\xi > 1$, where $\xi =$
269 $(V_{SH}/V_{SV})^2$. In oceanic regions, global models often shows Ra larger than or comparable to Aa
270 (Kustowski et al., 2008; Auer et al., 2014). $\xi > 1$ is equivalent to the transverse isotropy with a
271 vertical slow symmetry axis and a horizontal, fast polarization plane (010) (perpendicular to
272 olivine b-axis). Along with subduction, the slow symmetry axis is progressively tilted, and
273 becomes sub-horizontal in steep subduction zones with the fast polarization plane (010) sub-
274 vertical and slab-parallel (Fig. 5) (e.g., Walpole et al., 2017). This would explain group A and
275 potentially group B and D if the vertical flow surrounds the slab. This mechanism was initially
276 proposed by Song and Kawakatsu (2012; 2013) to explain the observed trench-parallel ϕ in

277 oceanic subduction zones with large dip angles. They demonstrated that, for A-type orthorhombic
278 anisotropy of olivine, when the slab progressively steepens, ϕ for a sub-vertically propagating S
279 wave switches from trench-normal to trench-parallel. The near-vertical slab in the HK stands as a
280 vertical end-member of the models tested by Song and Kawakatsu (2012).

281
282 The orthorhombic anisotropy compatible with scenario 2 can be realized by the relationship
283 between the three distinct shear moduli in three respective crystal planes as $C55 > C66 > C44$,
284 where C44 is associated with the (100) plane, C55 with the (010) plane, and C66 with the (001)
285 plane. The above terminology is based on the mineralogy coordinates in which index 1 corresponds
286 to a-axis, index 2 to b-axis, and index 3 to c-axis (Table 1, bottom half). If the LPO is determined
287 in the deformation experiment, usually 1 refers to the lineation or shear direction, 3 refers to the
288 foliation or the shear plane, and 2 refers to that in the shear plane perpendicular to 1. (Table 1,
289 upper half). Fig. 6 illustrates the vertical flow scenario in terms of these 3 shear moduli in
290 mineralogy coordinates (see Fig. S5 for crystal configurations in deformation coordinates). The
291 orthorhombic anisotropy used by Song and Kawakatsu (2012) (SK12) has 2% Aa and 3% Ra for
292 shear waves (Table 1). In contrast, for single crystal olivine (Zhang et al., 2018) (Z18) Ra is
293 relatively reduced compared to Aa if deformed as A-type in horizontal flow, because the difference
294 between the horizontally aligned C55 and the average of C66 and C44 is smaller than the difference
295 between C66 and C44 (Fig. 6). We conducted a synthetic waveform experiment (details in
296 Supplementary) to evaluate how different fabrics listed in Table 1 contribute to scenario 2. Because
297 single crystal olivine anisotropy is the building block of mantle anisotropy, Z18 is also tested. The
298 setting of the model is to mimic A-type deformation in an NS-oriented horizontal flow and an EW-
299 striking vertical flow. These two settings can be viewed together as the flow before and after a

300 vertical subduction along a trench striking at an azimuth of 90° . Recently, Lynner and Long (2014)
301 and Lynner et al. (2017) proposed that E- and C-type olivine LPO better explain the pattern of
302 anisotropy in sub-slab mantle than A-type in a suit of subduction zones. We also include E- and
303 C-type olivine in our examination. Their corresponding crystal configurations in deformation
304 coordinates can be found in Fig. S5.

305
306 For both horizontal and vertical flow cases, we generate synthetic waveforms with incidence
307 angles j of 5° and 30° (roughly the case of this study), and for S wave propagating azimuths from
308 90 to 270° (see Supplementary). At each azimuth, two polarization angles of S wave were tested:
309 0 (SV) and 35° from the propagation direction. We measure SWS on the synthetic waveforms as
310 for the real data. No noise is added to the synthetics, but the same quality control as for the real
311 data is applied. In Figs. 7 and 8, only the results for azimuth of 200° , i.e., the azimuth for most of
312 the rays in group A, is displayed. A-, E- and C-type olivine is the focus of this section, and the
313 effects of B-type fabrics will be discussed later.

314
315 Fig. 7 shows that for j of 5° , A-type SK12 and Z18, C-type J06C, and E-type J06E (see Table 1
316 for model names) all produce trench-normal ϕ for horizontal flow as expected. For vertical flow,
317 ϕ parallel the trench (or slab) for SK12, but could be off for some non-SV polarizations for Z18.
318 Splitting is minimal for Z18, because C55 (71.74) is almost equal to C66 (71.16) (Fig. 6) and Aa
319 $> Ra$, as explained above. C- and E-type LPOs yield splitting perpendicular and oblique to the
320 trench, respectively. For $j = 30^\circ$, scatter increases. For horizontal flow, ϕ still cluster roughly in
321 the trench-normal regime ($<40^\circ$). In the case of vertical flow, SK12 stably produce splitting in

322 parallel to the trench. An incidence angle of 30° yields enhanced splitting for Z18, but ϕ is no
323 longer trench-parallel. Splitting for both J06C and J06E is more of trench-normal than of trench-
324 parallel, and thus both C- and E-type fabrics fail to explain our observations. This could be
325 understood intuitively from the fact that C55 (trench-normal) is larger than C66 (trench-parallel)
326 for both C- and E-type olivine in vertical flow environment (Fig. S5). These synthetic experiments
327 demonstrate that the vertical flow model is valid if the dominant mantle mineral olivine deforms
328 as A-type and has orthorhombic anisotropy with a strong radial component that makes $C55 > C66$
329 $> C44$ (in mineralogy frame). This configuration is compatible with the AG-type olivine fabrics
330 documented by Mainprice (2007).

331

332 **5. Preferred mechanism**

333

334 We have simplified the mechanisms behind the observed anisotropy pattern around the HK to two
335 scenarios. While a full understanding of the dynamics of the double-verging HK-Pamir system
336 relies on a detailed simulation yet to be available, critical issues pertaining to each scenario can be
337 assessed to help discriminate which one is more favored than the other.

338

339 We first examine whether each scenario is realistic in providing sufficient anisotropy. For the
340 vertical flow scenario, assuming a 150 km wide deformation domain from the vertical slab laterally
341 into the ambient mantle (corresponding to an S traveling distance of roughly 300 km), it takes a
342 vertical distance of 150 km, or 4.3 My with a 35 km/My descending rate, to assemble a finite strain
343 of one ($\gamma = 1$), a deformation sufficient for strong alignment. Strain accumulation may have started
344 before subduction, but even though it starts at 100 km depth, γ of 2 can be achieved at 400 km

345 depth. The additional stretching of the lower half of the slab (Kufner et al., 2018) since the breakoff
346 inception accelerates the deformation accumulation. In contrast, trench-parallel anisotropy is
347 aligned by pure shear that results from stretching of the minerals in parallel with the trench when
348 they are pushed away by the retreating slab; it is not straightforward to parameterize the strength
349 of the pure shear. Nonetheless, we note that the slab in HK is short in length, i.e., at 380 km depth
350 before breakoff (Kufner et al., 2016) and only 100 km in half width. As a reference, strong trench-
351 parallel anisotropy is accumulated in subduction models with slabs 300-1000 km in half width
352 continuously extending to and resting on the bottom of the transition zone (Faccenda and Capitanio,
353 2012; 2013). A robust “core” of toroidal flow as witnessed in the numerical models may not easily
354 be formed due to HK’s small dimension, and a weak alignment may be overwhelmed by the later,
355 breakoff-driven accelerated shear flow. The rollback scenario seems to be difficult in producing
356 sufficient amount of anisotropy.

357

358 Another challenge for the rollback scenario comes from the constraint that the convergence
359 boundary of the HK is nearly motionless. Recent dynamic models (e.g., Duretz and Gerya, 2013;
360 Krystopowicz and Currie, 2013) show that continental subduction occurs in different styles
361 depending on the rheology structure of crust and mantle, often characterized by lithospheric
362 delamination and slab breakoff. In the case of lower crust subduction, either the slab is short-lived
363 due to frequent, complete breakoff or the delamination of mantle lithosphere rapidly retreats to
364 maintain its entirety. The prominent model feature of “trench retreat” is in contradiction with the
365 non-retreating of the plate boundary along the HK (Replumaz and Tapponnier, 2003; Liao et al.,
366 2017). A case model in Krystopowicz and Currie (2013) that might mimic the HK with a stationary
367 trench and a steep slab before complete breakoff is made of increased strength of lower crust and

368 mantle lithosphere so that the delaminated lithosphere does not retreat and detach easily. In all the
369 cases tested in Duretz and Gerya (2013) and Krystopowicz and Currie (2013), rollback with a fixed
370 hinge at the surface is hardly achievable. In the conceptual rollback orogeny model proposed by
371 Kissling and Schlunegger (2017), trench retreat is a central feature. In the oceanic counterpart,
372 Faccenda and Capitanio (2012) shows that, without hundreds of km of trench retreat, trench-
373 parallel delay times are likely negligible.

374
375 A point concerning the vertical entrainment scenario is whether the shear flow is disrupted by the
376 breakoff. If the lower slablet is completely detached, the flow around it can be complicated and
377 systematic anisotropy would be difficult to build. The breakoff models tested in Lin and Kuo (2016)
378 for the Taiwan orogen show that the descending of the slab fragment severely destroys the toroidal
379 flow in the vicinity originating from the adjacent slabs. In Confal et al.' (2018) simulation of
380 eastern Mediterranean subduction, complete slab breakoff induces flow across the slab window
381 that significantly influences the pattern of anisotropy. However, tomography on semi-global
382 (Koulakov, 2011; Van der Voo et al., 1999) and regional (Kufner et al., 2016) scales all portrays
383 the HK slab as a vertical structure continuing to the lower transition zone, which is preferable in
384 harnessing large-scale, vertical shear and align the olivine consistently in the surrounding mantle.

385
386 The analyses described above strongly favor vertical entrainment, as opposed to rollback, as the
387 primary mechanism for the observed circular pattern of anisotropy around the HK. If the stationary
388 trench does not permit much changes in subduction trajectory, the near-vertical subduction or
389 delamination entails no toroidal flow. This thereby avoids the debate centered at some oceanic
390 subduction zones where toroidal flow may dominate. Our observations thus demonstrate that slab

391 entrainment is a viable mechanism for trench-parallel anisotropy. The vertical slab in the HK can
392 be regarded as the end-member case of the steep subduction scenario where orthorhombic
393 anisotropy of olivine contributes to the trench-parallel anisotropy.

394

395 **6. Discussion**

396

397 6.1 The role of B-type olivine

398 Since positive radial anisotropy ($\xi > 1$) together with $Ra > Aa$ (observed in horizontal flow regions)
399 are critical factors to the vertical flow scenario, questions may arise as to whether the radial
400 anisotropy commonly observed in asthenosphere beneath oceanic plates (e.g., Kustowski et al.,
401 2008; Auer et al., 2014) persists along subduction zones to deep upper mantle. It has been proposed
402 that radial anisotropy may result from petrological fabrics, such as elongated melt pockets, that
403 would not be entrained with subduction to depth (e.g., Kawakatsu and Utada, 2017). Recent global
404 anisotropy model, however, shows primarily negative radial anisotropy ($\xi < 1$) in the lower upper
405 mantle and transition zone around subduction zones (Ferreira et al., 2019), which can be readily
406 explained as caused by the rotation of the same deformation fabrics from horizontal to vertical
407 during subduction.

408

409 Despite the global model of Ferreira et al. (2019) suggests a form of radial anisotropy compatible
410 with our deep entrainment interpretation, it is always desirable to examine other mechanisms that
411 could explain the observations too. One type of olivine fabric may enhance the trench-parallel
412 anisotropy without external mechanisms to maintain large radial anisotropy. Jung (2009) reported
413 that A-type olivine fabric transforms to B-type with [001](010) (the same as A-type except c-axis

414 aligns with the shear direction) by increasing pressure to 3 GPa or 100 km depth. Ohuchi and
415 Irifune (2014) demonstrated more complex transformations of A-type dry olivine at about 220 km
416 to either a mix of B- and C-type at high temperatures similar to oceanic mantle conditions or a B-
417 type alike fabric at temperatures akin to continental environment. Moreover, strong B-type LPO
418 is found in rock samples exhumed from pressure conditions greater than 4 GPa (Lee and Jung,
419 2015).

420

421 We tested the effect of B-type fabrics in the same way as for A-, C- and E-types. Fig. 8 shows that
422 Z18B (Z18, but assuming B-type) and LJ15 (Lee and Jung, 2015) provide strong trench-parallel
423 splitting especially for vertical flow. Both O11 (Ohuchi et al., 2011) and J06B (Jung et al. 2006)
424 are computed from weakly aligned samples and thus produce weak and polarization-dependent
425 anisotropy, but some of them may be marginally detectable. An investigation of Z18 reveals how
426 the vertical flow scenario benefits from B-type fabric: For A-type, the trench-parallel and trench-
427 normal directions are dominated by C55 and C66, respectively, which are almost equal in
428 magnitude in most mineral physics reports (e.g., Zhang et al., 2018); for B-type, the moduli in play
429 are C55 and C44 (see Fig. 6) with C44 (trench-normal) being the smallest shear modulus of single
430 crystal olivine (Table 1). While some of the early experiments of pressure-induced fabric
431 transformation was challenged (e.g., Karato, 2008) and B-type olivine predicts anisotropy at odds
432 with seismology observations in most of oceanic asthenosphere, the HK subduction with an
433 accelerated descent during breakoff may facilitate high shear stress in a dry environment where B-
434 type alike transformation may occur in deeper upper mantle. B-type fabric is characterized by $\xi >$
435 1 in both horizontal and vertical flow, which may increase the heterogeneity of radial anisotropy
436 portrayed in global models like Ferreira et al. (2019).

437

438 6.2 Orogenic processes vs. mantle dynamics

439 The SKS splitting measurements with nearly consistent ENE trending ϕ by Kufner et al. (2018)
440 (Fig. S6) covers mainly the north of the HK-Pamir convergence boundary and barely overlap
441 groups A, B, and D. They proposed a collision-induced escape process in the mantle that produce
442 the anisotropy in parallel with the general trend of the convergence boundary in the HK-Pamir
443 mountain belt. Schoenecker et al. (1997) suggested that the strain field in the upper mantle is
444 induced by collision and indentation of the continental plates. **These interpretations are in**
445 **accordance with the conception of coherent deformation over the depth of large mountain belts**
446 **(Silver, 1996). In contrast, group A, on the Indian side, is sub-parallel to the trend of the**
447 **convergence boundary in the HK segment alone, and is attributed to subduction processes below**
448 **the lithosphere.** Our source-side anisotropy shows little direct correlation with the geometry of the
449 HK-Pamir convergence boundary (Fig. 2), nor with the major tectonic structures in the region. For
450 instance, groups A and D strike at high angles with the Chaman fault and the Shyok suture zone,
451 respectively (see Fig. 1).

452

453 Evidence has mounted in support of a deep origin for the observed anisotropy along mountain
454 belts. In western Alps, while the SKS pattern apparently tracks the Alps curvature, Barruol et al.
455 (2011) proposed that the source of anisotropy resides in the asthenosphere around the Eurasian
456 continental slab. Kuo et al. (2018) demonstrated quantitatively that ϕ 's of SKS in parallel with
457 the structures of the Taiwan orogen are better explained by the interaction between the double
458 verging Ryukyu-Manila subduction zones underlying the broad collision zone. We argue that,
459 whereas collision directly imposes deformation in the lithosphere and builds the mountain,

460 subduction-related dynamics dominates the strain field across the depth of the upper mantle that
461 may lead to patterns of anisotropy coincidentally correlated with the trend of the mountain structure
462 or convergence boundary.

463

464 **7. Conclusions**

465

466 We measured source-side shear wave splitting for the Hindu Kush region to isolate the mid- to
467 lower upper mantle from the collision processes that built the orogen. The results reflect the
468 dynamics in the mantle dictated by the subduction of the Indian lithosphere. We observed a circular
469 pattern of fast polarization direction surrounding the HK slab, which is similar to that found in
470 many oceanic subduction zones where slab rollback is suggested to drive the toroidal flow and the
471 trench-parallel anisotropy. However, because continental slab rollback is difficult to maintain with
472 a fixed convergence boundary as in the case of Hindu Kush, we interpret the anisotropy pattern as
473 resulting from sub-vertical shear flow in the ambient mantle driven by the steep and probably
474 accelerated descent in the detaching segment of the continental lithosphere beneath the Hindu
475 Kush. This scenario necessitates A-type or AG-type olivine characterized by stronger radial than
476 azimuthal component. Whereas this is our main conclusion, in the case that the orthorhombic
477 anisotropy diminishes with depth we speculate that B-type olivine in dry, deep upper mantle, as
478 has been documented in both laboratory and natural rocks, may potentially contribute to the
479 pronounced trench-parallel anisotropy in this region.

480

481 Acknowledgment. We thank three anonymous reviewers for their constructive comments. The
482 research was supported by the Ministry of Science and Technology of Taiwan, Republic of China,
483 under grant MOST 107-2116-M-001-020-MY3.

484

485 **References**

486

487 Auer, L., Boschi, L., Becker, T. W., Nissen-Meyer, T., & Giardini, D. (2014). Savani: A variable
488 resolution whole-mantle model of anisotropic shear velocity variations based on multiple
489 data sets. *Journal of Geophysical Research: Solid Earth*, 119(4), 3006–
490 3034.[doi:10.1002/2013jb010773](https://doi.org/10.1002/2013jb010773)

491 Baccheschi, P., Margheriti, L., Steckler, M.S., 2007. Sesmic anisotropy reveals focused mantle
492 flow around the Calabrian slab (Southern Italy). *Geophys. Res. Lett.* 34, L05302.
493 <https://doi.org/10.1029/2006GL028899>

494 Barruol, G., Bonnín, M., Pedersen, H., Bokelmann, G. H. R., Tiberi, C., 2011. Belt-parallel
495 mantle flow beneath a halted continental collision: The Western Alps. *Earth Planet. Sci.*
496 *Lett.* 302, 429–438. <https://doi.org/10.1016/j.epsl.2010.12.040>

497 Burtman, V.S., Molnar, P., 1993. Geological and geophysical evidence for deep subduction of
498 continental crust beneath the Pamir. *Spec. Pap., Geol. Soc. Am.* 281, 1–76.
499 <https://doi.org/10.1130/SPE281-p1>

500 Confal, J.M., Faccenda, M., Eken, T., Taymaz, T., 2018. Numerical simulation of 3-D mantle
501 flow evolution in subduction zone environments in relation to seismic anisotropy beneath

502 the eastern Mediterranean region. *Earth Planet. Sci. Lett.* 497, 50-
503 61. <https://doi.org/10.1016/j.epsl.2018.06.005>

504 Crotwell, H.P., Owens, T.J., Ritsema, J., 1999. The TauP Toolkit: Flexible seismic travel-time
505 and ray-path utilities. *Seismol. Res. Lett.* 70, 154–160. doi:10.1785/gssrl.70.2.154.

506 Duretz, T., Schmalholz, S.M., Gerya, T.V., 2012. Dynamics of slab detachment. *Geochem.*
507 *Geophys. Geosyst* 13(3), Q03020. <http://dx.doi.org/10.1029/2011GC004024>

508 Duretz, T., Gerya, T.V., 2013. Slab detachment during continental collision: Influence of crustal
509 rheology and interaction with lithospheric delamination. *Tectonophysics* 602, 124–140.
510 <https://doi.org/10.1016/j.tecto.2012.12.024>

511 Ekström, G., Nettles, M., Dziewonski, A. M., 2012. The global CMT project 2004-2010:
512 Centroid-moment tensors for 13,017 earthquakes. *Phys. Earth Planet. Inter.* 200-201, 1-9.
513 doi:10.1016/j.pepi.2012.04.002

514 Faccenda, M., Capitanio, F.A., 2012. Development of mantle seismic anisotropy during
515 subduction-induced 3-D flow. *Geophys. Res. Lett.* 39, 11. doi:10.1029/2012GL051988

516 Faccenda, M., Capitanio, F.A., 2013. Seismic anisotropy around subduction zones: insights from
517 three-dimensional modeling of upper mantle deformation and SKS splitting calculations.
518 *Geochem. Geophys. Geosyst.* 14. <http://dx.doi.org/10.1029/2012GC004451>

519 Foley, B.J., Long, M.D., 2011. Upper and mid-mantle anisotropy beneath the Tonga slab.
520 *Geophys. Res. Lett.*, 38, L02303. doi:10.1029/2010GL046021

521 Ferreira, A.M.G., Faccenda, M., Sturgeon, W., Chang, S.-J., Schardong, L. 2019. Ubiquitous
522 lower-mantle anisotropy beneath subduction zones. *Nat. Geosci.* 12, 301-
523 306. <https://doi.org/10.1038/s41561-019-0325-7>

524 Jung, H., Katayama, I., Jiang, Z., Hiraga, T., and Karato, S., 2006. Effect of water and stress on
525 the lattice-preferred orientation of olivine. *Tectonophysics*, 421, 1-22.
526 doi:10.1016/j.tecto.2006.02.011.

527 Jung, H., Mo, W., Green, H.E., 2009. Upper mantle seismic anisotropy resulting from pressure-
528 induced slip transition in olivine. *Nat. Geosci.* 2, 73–77. <https://doi.org/10.1038/ngeo389>

529 Karato, S.-I., Jung, H., Katayama, I., Skemer, P., 2008. Geodynamic significance of seismic
530 anisotropy of the upper mantle: New insights from laboratory studies. *Annu. Rev. Earth*
531 *Planet. Sci.* 36, 59–95. doi:[10.1146/annurev.earth.36.031207.124120](https://doi.org/10.1146/annurev.earth.36.031207.124120)

532 Kawakatsu, H., Utada, H. 2017. Seismic and electrical signatures of the lithosphere-
533 asthenosphere system of the normal oceanic mantle. *Annu. Rev. Earth Planet. Sci.* 45, 139-
534 67. <https://doi.org/10.1146/annurev-earth-063016-020319>

535 Kennett, B.L.N., Engdahl, E.R., 1991. Traveltimes for global earthquake location and phase
536 identification. *Geophys. J. Int.* 105, 429–465. doi:10.1111/j.1365-246X.1991.tb06724.x.

537 Kissling, E., Schlunegger, F., 2018. Rollback Orogeny Model for the Evolution of the Swiss
538 Alps. *Tectonics* 37, 1097-1115. <https://doi.org/10.1002/2017TC004762>

539 Koulakov, I., 2011. High-frequency P and S velocity anomalies in the upper mantle beneath Asia
540 from inversion of worldwide traveltime data. *J. Geophys. Res.* 116(B4), 1–22.
541 doi:10.1029/2010JB007938

542 Krystopowicz, N. J., Currie, C.A., 2013. Crustal eclogitization and lithosphere delamination in
543 orogens. *Earth Planet. Sci. Lett.* 361, 195-207. <https://doi.org/10.1016/j.epsl.2012.09.056>

544 Kufner, S.-K., Schurr, B., Sippl, C., Yuan, X., Ratschbacher, L., Mohammad Akbar, A., et al.,
545 2016. Deep India meets deep Asia: Lithospheric indentation, delamination and break-off
546 under Pamir and Hindu Kush (Central Asia). *Earth Planet. Sci. Lett.* 435, 171–184.
547 <https://doi.org/10.1016/j.epsl.2015.11.046>

548 Kufner, S.-K., Schurr, B., Haberland, C., Zhang, Y., Saul, J., Ischuk, A., & Oimahmadov, I.,
549 2017. Zooming into the Hindu Kush slab break-off: A rare glimpse on the terminal stage of
550 subduction. *Earth Planet. Sci. Lett.* 461, 127–140. <https://doi.org/10.1016/j.epsl.2016.12.043>

551 Kufner, S.-K., Eken, T., Tilmann, F., Schurr, B., Yuan, X., Mechie, J., et al., 2018. Seismic
552 anisotropy beneath the Pamir and the Hindu Kush: Evidence for contributions from crust,
553 mantle lithosphere, and asthenosphere. *J. Geophys. Res., Solid Earth* 123.
554 <https://doi.org/10.1029/2018JB015926>

555 Kuo, B.-Y., Wang, C.-C., Lin, S.-C., Lin, C.-R., Chen, P.-C., Jang, J.-P., Chang, H.-K., 2012,
556 Shear-wave splitting at the edge of the Ryukyu subduction zone, *Earth Planet. Sci. Lett.*,
557 355-356, 262-270, doi:10.1016/j.epsl.2012.08.005.

558 Kuo, B.-Y., Lin, S.-C., Lin, Y.-W., 2018. SKS splitting and the scale of vertical coherence of the
559 Taiwan mountain belt. *J. Geophys. Res., Solid Earth* 123, 1366–1380.
560 <https://doi.org/10.1002/2017JB014803>

561 Kustowski, B., Ekstrom, G., Dziewonski, A.M., 2008. Anisotropic shear-wave velocity structure
562 of the Earth's mantle: a global model. *J. Geophys. Res.* 113, (B06306).
563 [doi:10.1029/2007JB005169](https://doi.org/10.1029/2007JB005169).

564 Lee, J., Jung, H., 2015. Lattice-preferred orientation of olivine found in diamond-bearing garnet
565 peridotites in Finsch, South Africa and implications for seismic anisotropy. *J. Struct. Geol.*
566 70, 12-22. <https://doi.org/10.1016/j.jsg.2014.10.015>

567 Li, W., Chen, Y., Yuan, X., Schurr, B., Mechie, J., Oimahmadov, I., Fu, B., 2018. Continental
568 lithospheric subduction and intermediate-depth seismicity: Constraints from S-wave velocity
569 structures in the Pamir and Hindu Kush. *Earth Planet. Sci. Lett.* 482, 478–489.
570 <https://doi.org/10.1016/j.epsl.2017.11.031>

571 Liao, J., Gerya, T., Thielmann, M., Webb, A., Kufner, S.K., Yin, A., 2017. 3D geodynamic
572 models for the development of opposing continental subduction zones: The Hindu Kush-
573 Pamir example. *Earth Planet. Sci. Lett.* 480, 133-146.
574 <https://doi.org/10.1016/j.epsl.2017.10.005>

575 Lin, S.-C., Kuo, B.-Y., 2016. Dynamics of the opposite-verging subduction zones in the Taiwan
576 region: Insights from numerical models. *J. Geophys. Res., Solid Earth* 121, 2174–2192.
577 <https://doi.org/10.1002/2015JB012784>

578 Long, M. D., 2013. Constraints on subduction geodynamics from seismic anisotropy. *Rev.*
579 *Geophys.* 51, 76-112. <https://doi.org/10.1002/rog.20008>

580 Lynner, C., Long, M.D., 2013. Sub-slab seismic anisotropy and mantle flow beneath the
581 Caribbean and Scotia subduction zones: Effects of slab morphology and kinematics. *Earth*
582 *Plant. Sci. Lett.*, 361, 367-378. <https://doi.org/10.1016/j.epsl.2012.11.007>

583 Lynner, C., Long, M.D., 2014. Sub-slab anisotropy beneath the Sumatra and circum-Pacific
584 subduction zones from source-side shear wave splitting observations. *Geochem. Geophys.*
585 *Geosyst.* 15, 2262–2281. <https://doi.org/10.1002/2014GC005239>

586 Lynner, C., Long, M.D., Thissen, C.J., Paczkowski, K., Montesi, L.G.J., 2017. Evaluating
587 geodynamic models for sub-slab anisotropy: Effects of olivine fabric type. *Geosphere*.
588 13,247-259. <https://doi.org/10.1130/GES01395.1>

589 MacDougall, J. G., Jadamec, M. A., Fischer, K. M., 2017. The zone of influence of the
590 subducting slab in the asthenospheric mantle. *J. Geophys. Res., Solid Earth* 122, 6599–6624.
591 <https://doi.org/10.1002/2017JB014445>

592 Mainprice, D., 2007. Seismic anisotropy of the deep earth from a mineral and rock physics
593 perspective. In *Treatise on Geophysics*, 2, 437-491.

594 Mohiuddin, A., Long, M.D., Lynner, C., 2015. Mid-mantle seismic anisotropy beneath
595 southwestern Pacific subduction systems and implications for mid-mantle deformation.
596 *Phys. Earth Planet. Inter.* 245, 1–14.

597 Nábelek, J., Hetényi, G., Vergne, J., Sapkota, S., Kafle, B., Jiang, M., Su, H., Chen, J., Huang,
598 B.-S., 2009. Underplating in the Himalaya-Tibet collision zone revealed by the Hi-CLIMB
599 experiment. *Science*, 325, 1371–1374. doi:10.1126/science.1167719

600 Negrodo, A. M., Replumaz, A., Willaseñor, A., Guillot, S., 2007. Modeling the evolution of
601 continental subduction processes in the Pamir-Hindu Kush region. *Earth and Planet. Sci.*
602 *Lett.* 259, 202-225. Doi:10.1016/j.epsl.2007.04.043

603 Nowacki, A., Kendall, J.-M., Wookey, J., Pemberton, A., 2015. Mid-mantle anisotropy in
604 subduction zones and deep water transport. *Geochem. Geophys. Geosyst.* 16(3), 764–784.
605 doi:10.1002/2014GC005667

606 Ohuchi, T., Irifune, T., 2014. Crystallographic preferred orientation of olivine in the Earth's deep
607 upper mantle. *Phy. Earth Planet. Inter.* 228, 220-231.
608 <http://dx.doi.org/10.1016/j.pepi.2013.11.013>

609 Ohuchi, T., Kawazoe, T., Nishihara, Y., Nishiyama, N., Irifune, T., 2011. High pressure and
610 temperature fabric transitions in olivine and variations in upper mantle seismic anisotropy.
611 *Earth Planet. Sci. Lett.* 304, 55-63, doi:10.1016/j.epsl.2011.01.015

612 Pavlis, G. L., Das, S., 2000. The Pamir-Hindu Kush seismic zone as a strain marker for flow in
613 the upper mantle. *Tectonics* 19(1), 103–115. <https://doi.org/10.1029/1999tc900062>

614 Replumaz, A., Tapponnier, P., 2003. Reconstruction of the deformed collision zone between
615 India and Asia by backward motion of lithospheric blocks. *J. Geophys. Res.* 108(B6), 2285,
616 doi:10.1029/2001JB000661.

617 Russo, R.M., Silver, P.G., 1994. Trench-Parallel Flow Beneath the Nazca Plate from Seismic
618 Anisotropy. *Science* 263(5150), 1105-1111. DOI: 10.1126/science.263.5150.1105

619 Russo, R.M., Mocanu, V.I., 2009. Source-side shear wave splitting and upper mantle flow in the
620 Romanian Carpathians and surroundings. *Earth Planet. Sci. Lett.* 287, 205-216.
621 <https://doi.org/10.1016/j.epsl.2009.08.028>

622 Schneider, F., Yuan, X., Schurr, B., Mechie, J., Sippl, C., Haberland, C., et al., GIPP, 2013.
623 Seismic imaging of subducting continental lower crust beneath the Pamir. *Earth Planet. Sci.*
624 *Lett.* 375(1), 101–112. <https://doi.org/10.1016/j.epsl.2013.05.015>

625 Schoenecker, S.C., Russo, R.M., Silver, P.G., 1997. Source-side splitting of S waves from Hindu
626 Kush-Pamir earthquakes. *Tectonophysics* 279, 149–159. [https://doi.org/10.1016/S0040-](https://doi.org/10.1016/S0040-1951(97)00130-3)
627 [1951\(97\)00130-3](https://doi.org/10.1016/S0040-1951(97)00130-3)

628 Schulte-Pelkum, V., Monsalve, G., Sheehan, A., Pandey, M. R., Saptota, S., Bilham, R., and Wu,
629 F., 2005. Imaging the Indian subcontinent beneath the Himalaya. *Nature* 435, 1222-1225,
630 doi:10.1038/nature03678.

631 Sieminski, A., Liu, Q., Trampert, J., Tromp, J., 2007. Finite-frequency sensitivity of body waves
632 to anisotropy based upon adjoint methods, *Geophys. J. Int.*, 171, 368–389.
633 <https://doi.org/10.1111/j.1365-246X.2007.03528.x>

634 Silver, P. G., 1996. Seismic anisotropy beneath the continents: Probing the depths of geology.
635 *Annu. Rev. Earth Planet. Sci.* 24(1), 385–432.
636 <https://doi.org/10.1146/annurev.earth.24.1.385>

637 Sippl, C., Schurr, B., Yuan, X., Mechie, J., Schneider, F. M., Gadoev, M., et al., 2013. Geometry
638 of the Pamir-Hindu Kush intermediate-depth earthquake zone from local seismic data. *J.*
639 *Geophys. Res., Solid Earth* 118(4), 1438–1457. <https://doi.org/10.1002/jgrb.50128>

640 Sobel, E., Chen, J., Schoenbohm, L., Thiede, R., Stockli, D., Sudo, M., Strecker, M., 2013.
641 Oceanic-style subduction controls late Cenozoic deformation of the Northern Pamir
642 orogeny. *Earth Planet. Sci. Lett.* 363, 204–218. doi:10.1016/j.epsl.2012.12.009

643 Song, T.-R. A., Kawakatsu, H., 2012. Subduction of oceanic asthenosphere: evidence from sub-
644 slab seismic anisotropy. *Geophys. Res. Lett.*, 39,
645 L17301. <https://doi.org/10.1029/2012GL052639>

646 Song, T.-R. A., Kawakatsu, H., 2013. Subduction of oceanic asthenosphere: a critical appraisal
647 in central Alaska. *Earth Planet. Sci. Lett.* 367, 82-
648 94. <https://doi.org/10.1016/j.epsl.2013.02.010>

649 van der Voo, R., Spakman, W., Bijwaard, H., 1999. Mesozoic subducted slabs under Siberia.
650 Nature 397, 246–249. <https://doi.org/10.1038/16686>

651 Walpole, J., Wookey, J., Kendall, J.-M., Masters, T.-G., 2017. Seismic anisotropy and mantle
652 flow below subducting slabs. Earth Planet. Sci. Lett., 465, 155-167.
653 <https://doi.org/10.1016/j.epsl.2017.02.023>

654 Wüstefeld, A., Bokelmann, G., 2007. Null detection in shear wave splitting measurements. Bull.
655 Seismol. Soc. Am. 97, 1204–1211. <https://doi.org/10.1785/0120060190>

656 Zhang, J. S., Bass, J.D., Schmandt, B., 2018. The Elastic Anisotropy Change Near the 410-km
657 Discontinuity: Predictions From Single-Crystal Elasticity Measurements of Olivine and
658 Wadsleyite. J. Geophys. Res., Solid Earth 123, 2674-
659 2684. <https://doi.org/10.1002/2017JB015339>

660
661
662
663

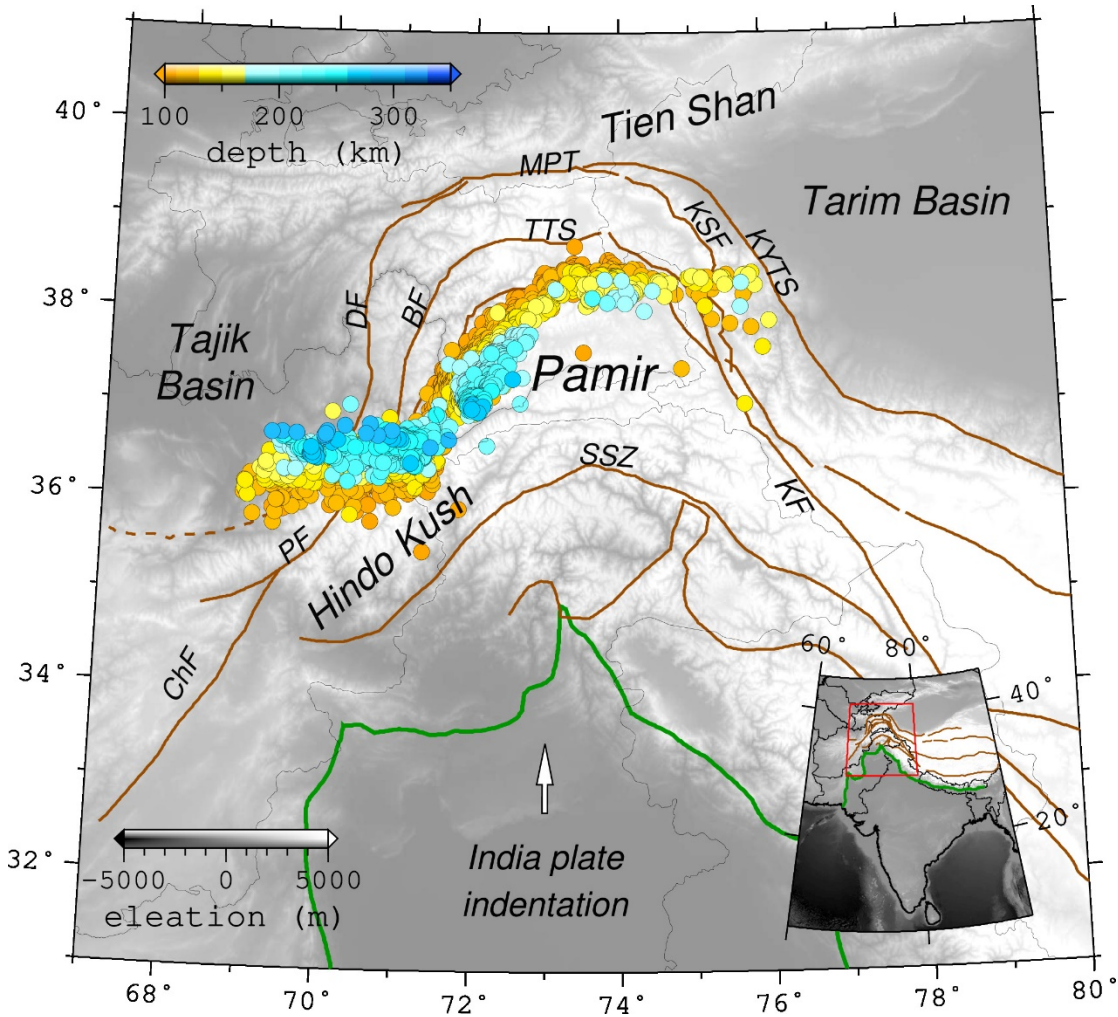
664 Table 1. Shear moduli, azimuthal anisotropy (A_a), and radial anisotropy (R_a) of olivine provided
 665 from literature in deformation coordinates (top half) and mineralogy coordinates (bottom half).

Ref	C44	C55 ¹	C66 ¹	A_a	R_a	Note
SK12	63.33	65.95	68.64	2.0%	3.0%	Deformation coordinates: 1: lineation (shear direction) 2: perpendicular to 1 in foliation plane 3: normal to foliation (shear plane)
Z18 ²	59.94	71.16	71.74	8.6%	4.7%	
J06C ³	67.9	71.1	66.6	2.3%	-2.1%	
J06E ³	65.0	71.1	68.5	4.5%	0.4%	
Z18B	71.16	59.94	71.74	8.6%	4.7%	
J06B ³	68.9	67.4	69.4	1.1%	0.1%	
LJ15	73.26	67.26	86.45	4.3%	11.0%	
O11 ³	72.50	71.80	74.30	0.5%	1.5%	
SK12	63.33	68.64	65.95	-	-	Mineralogy coordinates: 1: a-axis 2: b-axis 3: c-axis
Z18	59.94	71.74	71.16	-	-	
Z18B	59.94	71.74	71.16	-	-	
LJ15	67.26	86.45	73.26	-	-	

666
 667 Ref: SK12: Song and Kawakatsu (2012); Z18: Zhang et al. (2018); J06B, J06C, and J06E: Jung
 668 et al. (2006) for B-type, C-type and E-type olivine, respectively; Z18B: the same as Z18 but
 669 assumed to deform as B-type; LJ15: Lee and Jung (2015); O11: Ohuchi et al. (2011). SK12 and
 670 Z18 are assumed to deform as A-type. Z18B, LJ15, and O11 deform as B-type.

- 671 1. The difference between deformation and mineralogy coordinates is the switches between the 3
 672 shear moduli. Take A-type for instance, the switch is between C55 and C66.
 673 2. Shear moduli calculated for 4 GPa and 1273 K, the same condition as in LJ2015.
 674 3. The elastic moduli measured from deformation experiment is referenced to the deformation
 675 geometry. For O11, J06C, J06E, and J06B, the concentrations of crystal exes with respective to
 676 lineation and foliation are weak and diffuse, and it is not appropriate to convert them to the
 677 intrinsic, mineralogy coordinates.

678
679
680
681
682
683
684
685
686
687
688
689
690
691
692



693 Fig. 1. Map of the Hindu Kush-Pamir region. Earthquakes deeper than 100 km depth depict the
694 geometry of the Hindu Kush slab and the Pamir slab (Kufner et al., 2017). Green line denotes the
695 Eurasian-Asian main thrust boundary and brown lines represent the faults and sutures, adopted
696 from Sippl et al. (2013). ChF: Chaman Fault; PF: Panjshir Fault; DF: Darvaz Fault; BF:
697 Badakhshan Fault; MPT: Main Pamir Fault; TTS: Tanymas Thrust System; KSF: Kongur Shan
698 Fault; KYTS: Kashgar-Yecheng Transfer system; KF: Karakorum Fault; and SSZ: Shyok Suture
699 Zone. The Hindu Kush-Pamir region is outlined in the map on the lower right.

700

701

(a) 1993.261.05.02 (36.45°, 71.60°, 117 km) GRA1

702

703

704

705

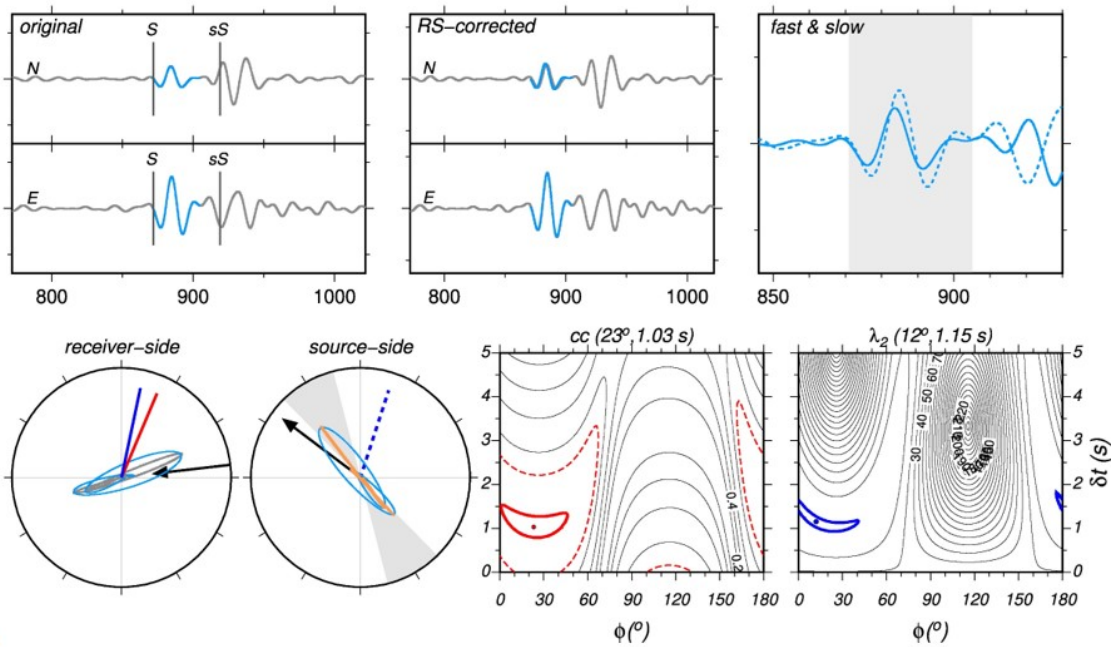
706

707

708

709

710



711

(b) 2000.019.07.09 (36.39°, 70.38°, 206 km) GRA1

712

713

714

715

716

717

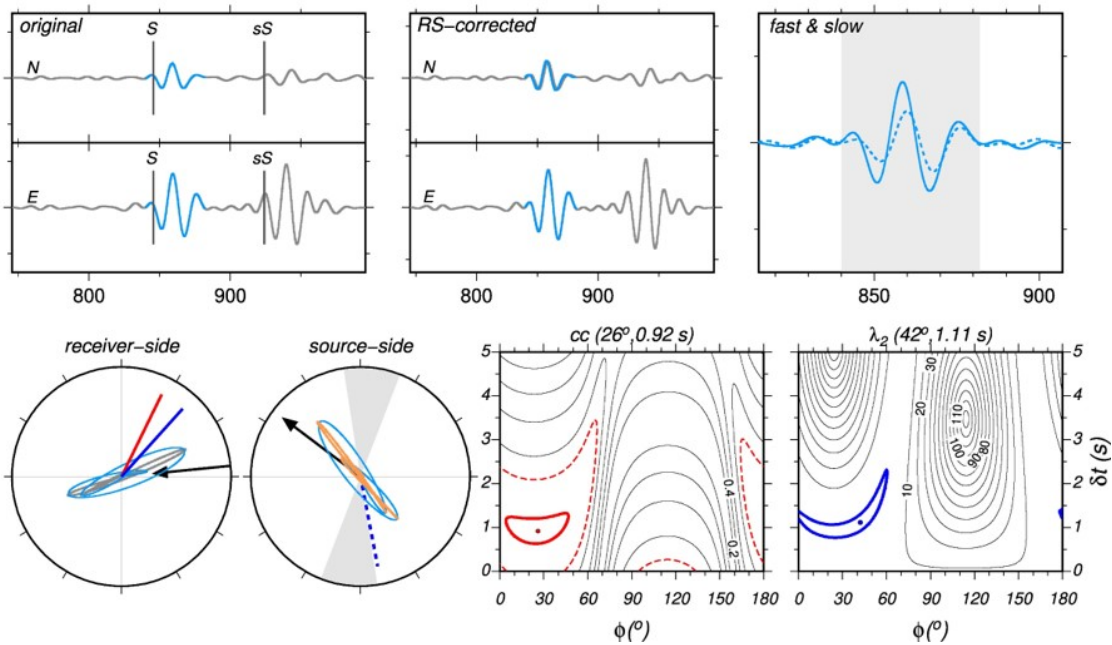
718

719

720

721

722

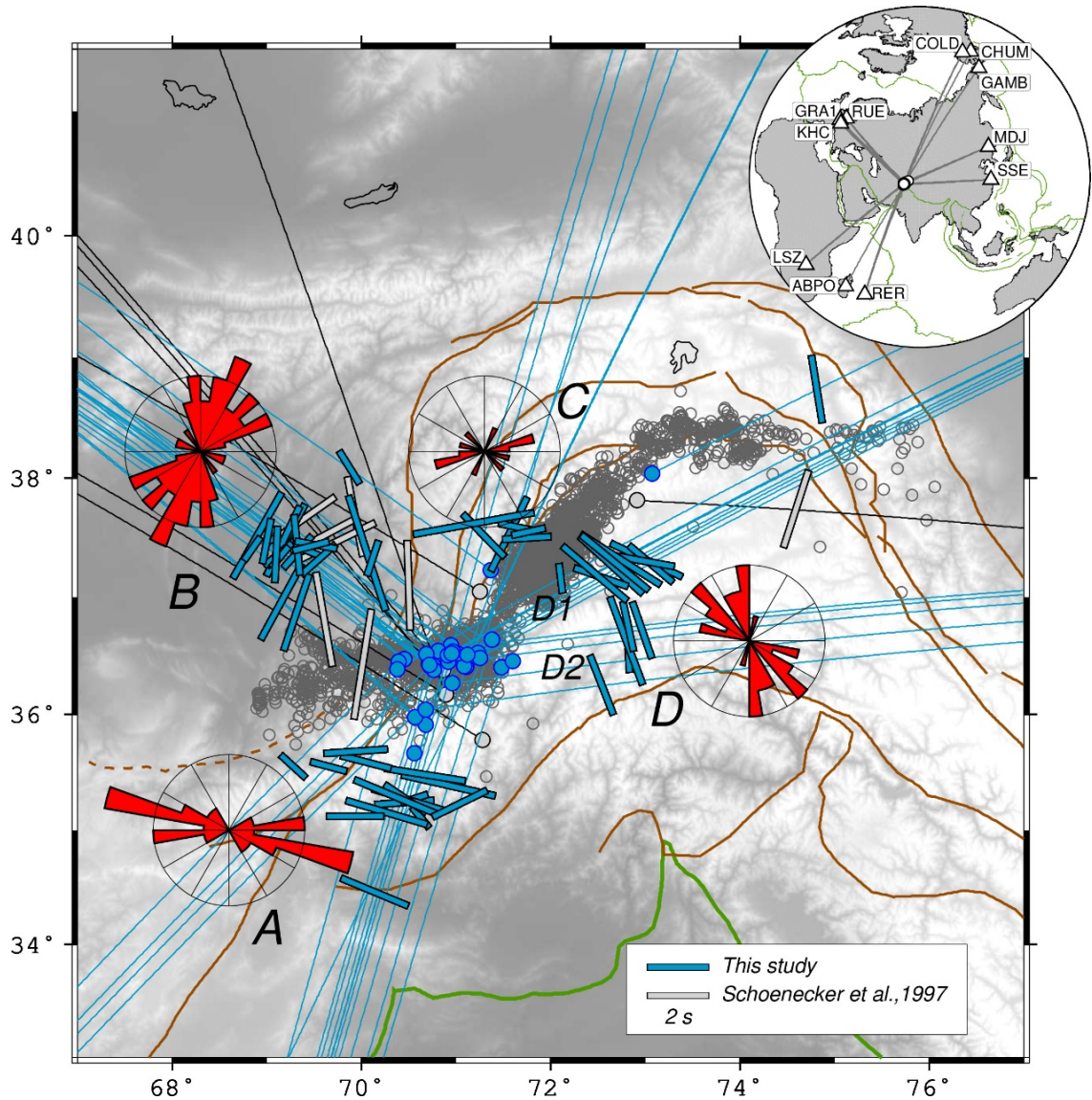


723 Fig. 2. Examples of source-side anisotropy measurement conducted in this study. The one-line
724 label on top of each figure shows date-time of the event (year, Julian day, hour, and minute),
725 location and depth of the event in the parenthesis, and the station name. On the top row, left panel:
726 Original waveforms in NS and EW components with S-wave in measurement window highlighted
727 in blue and the PREM predicted phase arrivals. Middle: Waveforms corrected for receiver-side
728 anisotropy. Right: Waveforms rotated to the fast (solid) and slow (dotted) directions of the source-
729 side anisotropy, with the measurement window in gray. On the lower row, left panel: Information
730 in station frame; S particle motion in gray for the original and light blue for that after receiver-side
731 anisotropy is removed. Two thick lines represent measured fast directions (red for rotation
732 correlation; blue for minimum eigenvalue method). Black arrow indicates where the S wave comes
733 from (at backazimuth). Second panel: Information in the source frame; Curve in light blue is the
734 same in the left panel but translated from the station frame to the source frame; curve in orange is
735 the recovered particle motion after source-side anisotropy is removed. Black arrow indicates the
736 azimuth of S wave. Blue dashed line denotes the ϕ determined from the minimum eigenvalue
737 method. The shaded region represents $\pm 15^\circ$ of the CMT predicted polarization orientation. The
738 CMT solution diagram is shown in Fig. S1. The third and forth panels: Grid search diagrams for
739 rotation correlation method (third; in red) and the minimum eigenvalue method (forth; in blue),
740 respectively, with the best solution denoted by dot, encircled by the contours of the 95%
741 confidence region (solid-line in respective colors) and the contours corresponding to the cross-
742 correlation coefficient of 0.9 (dotted line). (a) Solution accepted. (b) Solution rejected because the
743 recovered particle motion (orange curve) is outside of the CMT prediction region (shade).

744

745

746
747
748
749
750
751
752
753
754
755
756
757
758
759
760
761



762 Fig. 3. Source-side anisotropy measurement results. Individual splitting parameters (blue bars) are
763 plotted at locations 200 km down dip along the S raypath from the respective earthquakes (blue
764 dots). The orientation and length of each bar indicate measured ϕ and δt with the 2 s scale in
765 the legend box. Gray bars are the data from Schoenecker et al. (1997). Rose diagram for ϕ is
766 constructed with a 10° bin and an outer rim of 3. The upper right inset shows the stations (triangle)
767 distribution. Group C is disregarded (see Section 3) for having too few measurements. Groups A,
768 B, and D form a circular pattern around the Hindu Kush subduction zone.

769
770
771
772
773
774
775
776
777
778
779
780
781
782
783
784
785
786
787
788
789
790

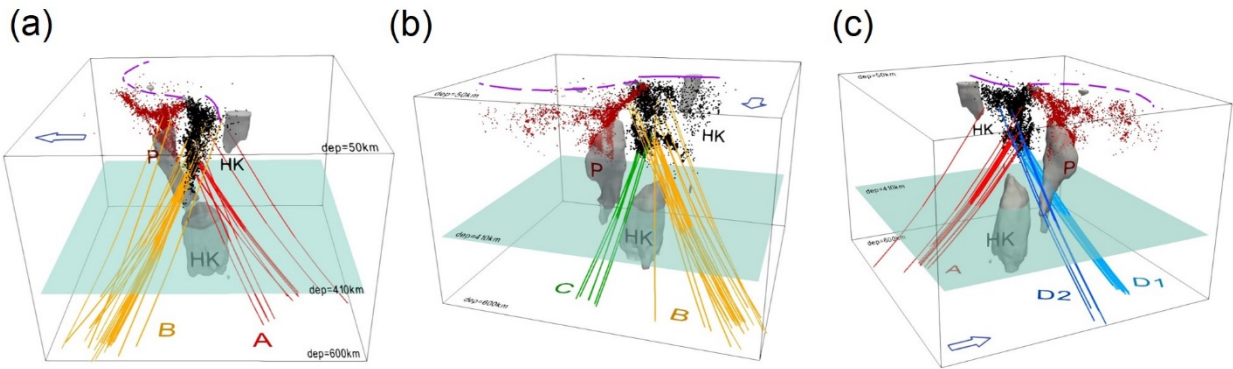


Fig. 4. 3D view of the ray path in three different perspectives. Arrow in each panel points to the north. Top and bottom surfaces of the box are at depths of 50 km and 600 km, respectively. A reference plane is placed at 410 km depth. On the top surface, solid and dashed lines in purple represent convergence boundary for Hindu Kush and Pamir subduction zones, respectively. Black and brown dots represent seismicity in the Hindu Kush and the Pamir slab, respectively. The 2.5% iso-surface of the positive anomalies from Kufner et al. (2016) is plotted to represent the core of the slabs, labeled with HK and P (Pamir). Rays in groups A, B, C, and D are marked in red, orange, green, and blue, respectively. (a) View from the west towards east to show sampling of the south (group A) and north (group B) sides of the HK slab. (b) View from nearly north to show groups B and C north of the HK. (c) View from ESE showing the paths of D1 and D2.

791
792
793
794
795
796
797
798
799
800
801
802
803
804
805
806
807
808
809
810
811
812
813

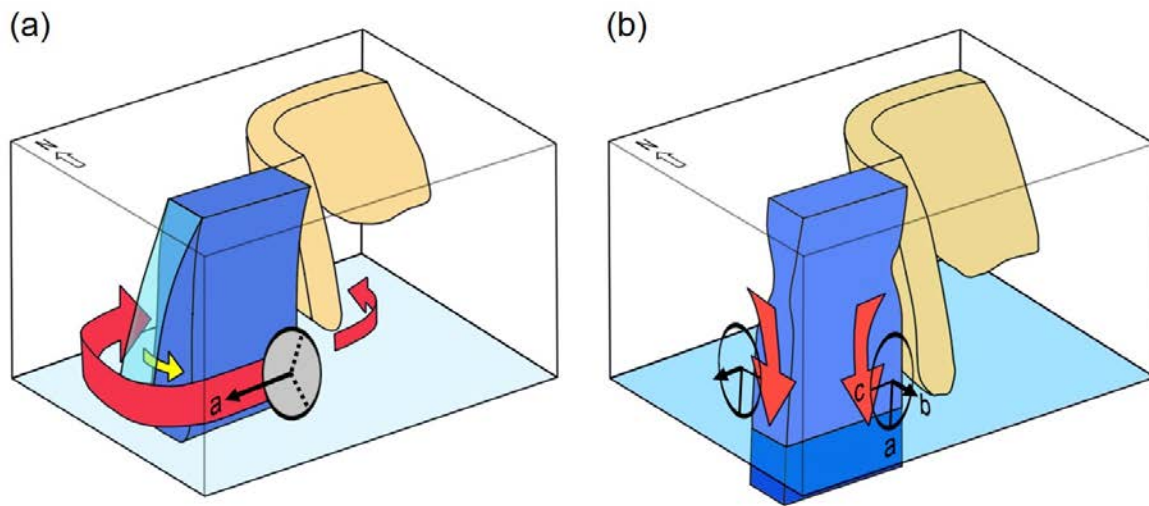
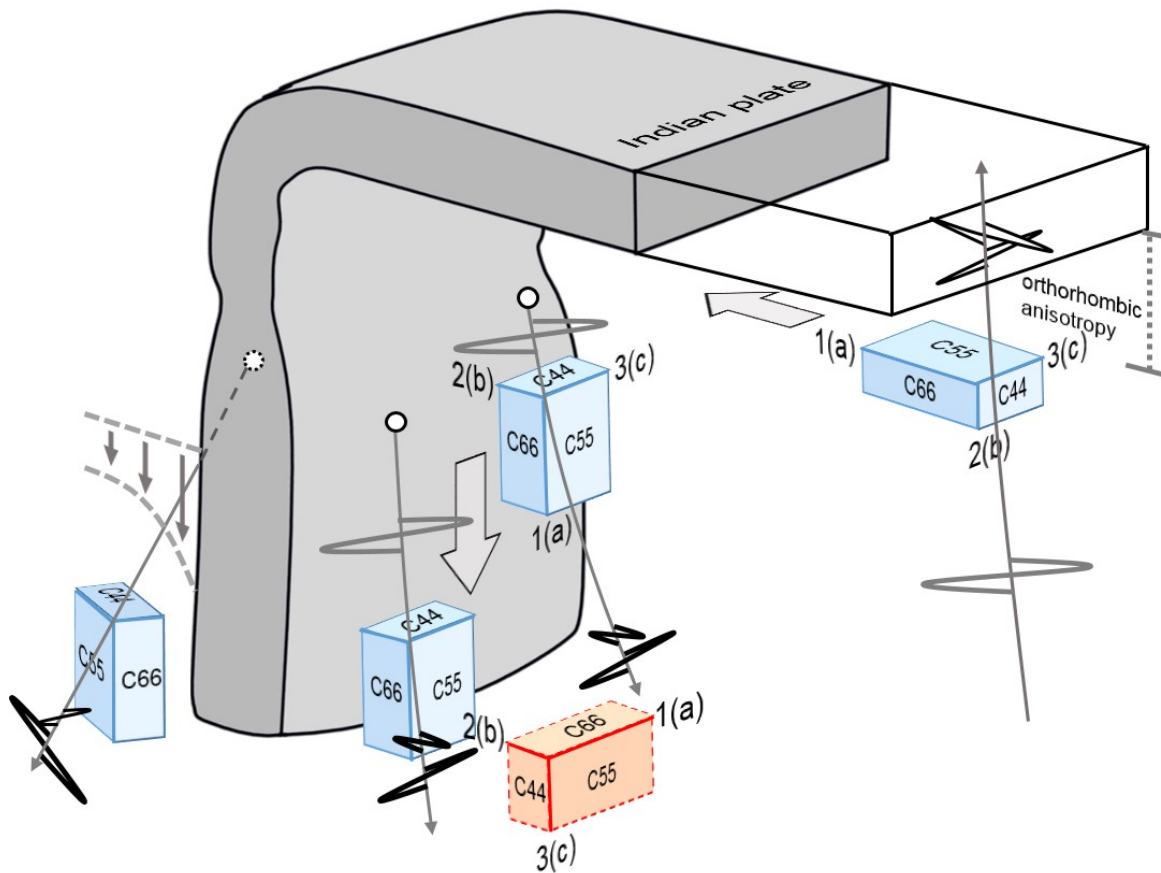


Fig. 5. Cartoons illustrating two mechanisms that are potentially responsible for the observed anisotropy around the HK of the HK (blue) - Parmir (Yellow) double subductions. The top and bottom surfaces of the box correspond to 100 and 410 km depths, respectively. (a) Rollback of the HK slab from a hypothetical north dipping position (transparent light blue) to the current near vertical position (blue), in the pre-breakoff time when the slab extends to 380 km depth (Kufner et al., 2016). Red arrows indicate toroidal flow induced by the rollback. The olivine a-axis is aligned by the pure shear along the toroidal flow, with b- and c-axis within the symmetry plane (shaded). (b) Vertical subduction and the incipient breakoff of the HK lower slab drives downward flow (red arrows) and vertical simple shear. For strong orthorhombic anisotropy, olivine fast plane (a-c plane) is aligned by vertical shear flow and the slow axis (b-axis) is perpendicular to the shear plane.

814
815
816
817
818
819
820
821
822
823
824
825
826



827 Fig. 6. Schematic illustration of olivine LPO rotation from horizontal to vertical during the Indian
 828 plate (gray) subduction in the HK region. Each rectangular box represents olivine fabric with shear
 829 modulus labelled on the 3 orthogonal faces in mineralogy convention. In a horizontal flow
 830 (horizontal arrow) regime, the alignment of A-type olivine is typified by the box in the upper right
 831 corner beneath the Indian plate: Index 1 corresponds to a-axis, index 2 b-axis, and index 3 c-axis.
 832 When the A-type fabric is rotated to vertical, S waves traveling sub-vertically from intraslab events
 833 (circle) split into fast and slow phases in parallel and perpendicular to slab surface, respectively, if
 834 strong orthorhombic anisotropy is present, i.e., $C55 > C66 > C44$. B-type olivine (orange box) is
 835 speculated to form in mid- to lower upper mantle to enhance trench-parallel anisotropy with C55
 836 always significantly larger than C44.

837

838

839

840

841

842

843

844

845

846

847

848

849

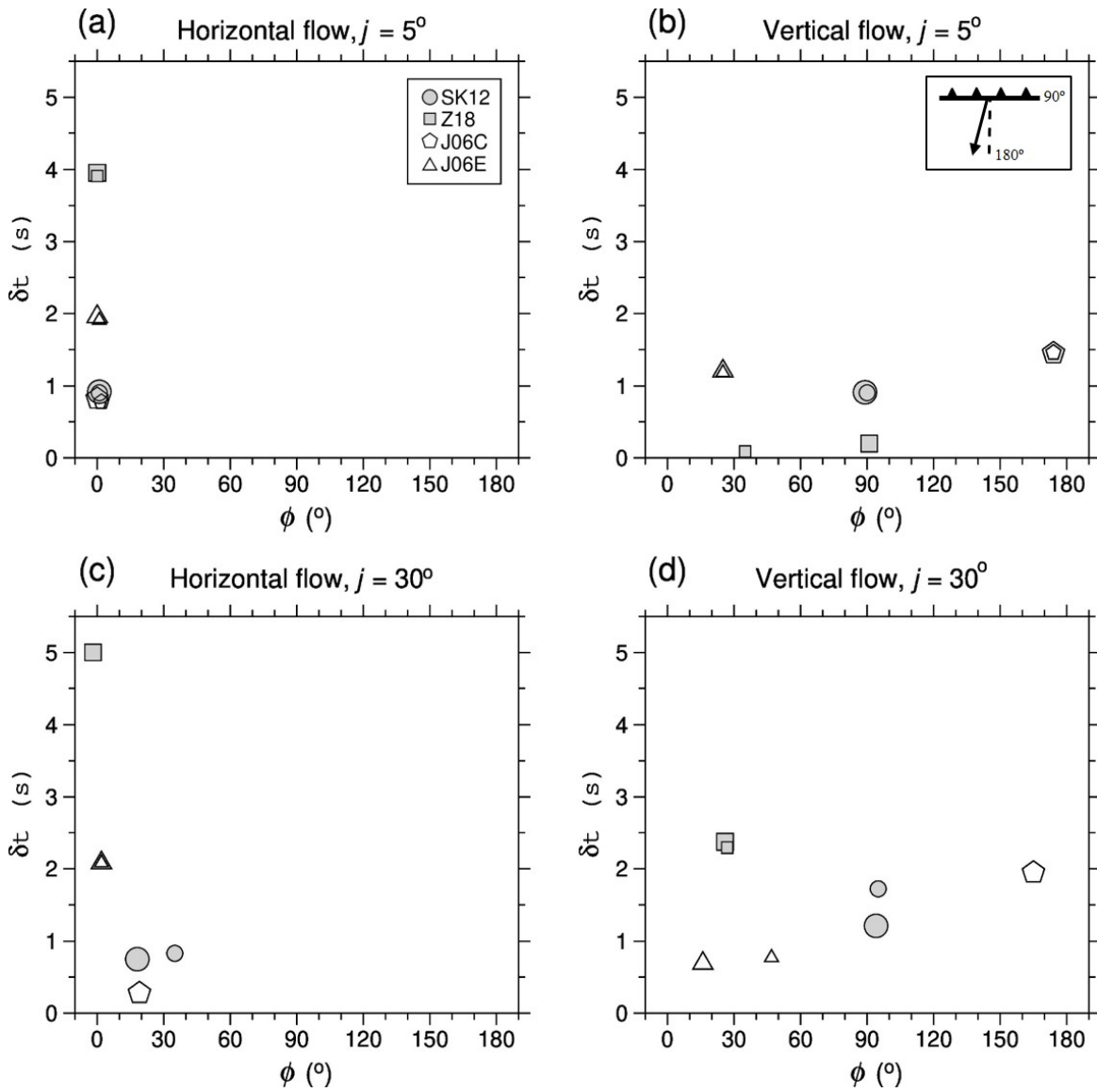
850

851

852

853

854



855 Fig. 7. SWS measurement results of synthetic experiments using elasticity models listed in Table

856 1 (Shaded symbols for A-type; open symbols for C- and E-type). Panels (a) and (b) with S-wave

857 incidence angle $j = 5^\circ$ provide a reference for an intuitive understanding of the splitting pattern.

858 Panels (c) and (d) represent $j = 30^\circ$. Symbol legend is shown in panel (a), and modeling setting

859 relative to the trench is shown in the inset in panel (b). Trench-normal direction corresponds to the

860 azimuth of 0 or 180° and trench-parallel (or slab-parallel) to 90° . Data shown are only the splitting
861 parameters for S wave at azimuth of 200° (the arrow in the inset in b) in order to simulate group
862 A. For each model, large-sized symbol denotes an initial polarization in parallel to the azimuth
863 (SV), and small-sized symbol denotes an initial polarization 35° from SV (SV:SH~0.82:0.57). A-
864 type olivine displays expected trench-normal ϕ for horizontal flow (a), and trench-parallel ϕ for
865 vertical flow (b), except for Z18 for which splitting is small and sensitive to initial polarization.
866 Splitting for C- and E-type olivine mimics that for A-type in horizontal flow, but becomes oblique
867 or perpendicular to the trench in the vertical flow scenario. Variability increases for $j = 30^\circ$ (c, d)
868 but general patterns remain.

869

870

871

872

873

874

875

876

877

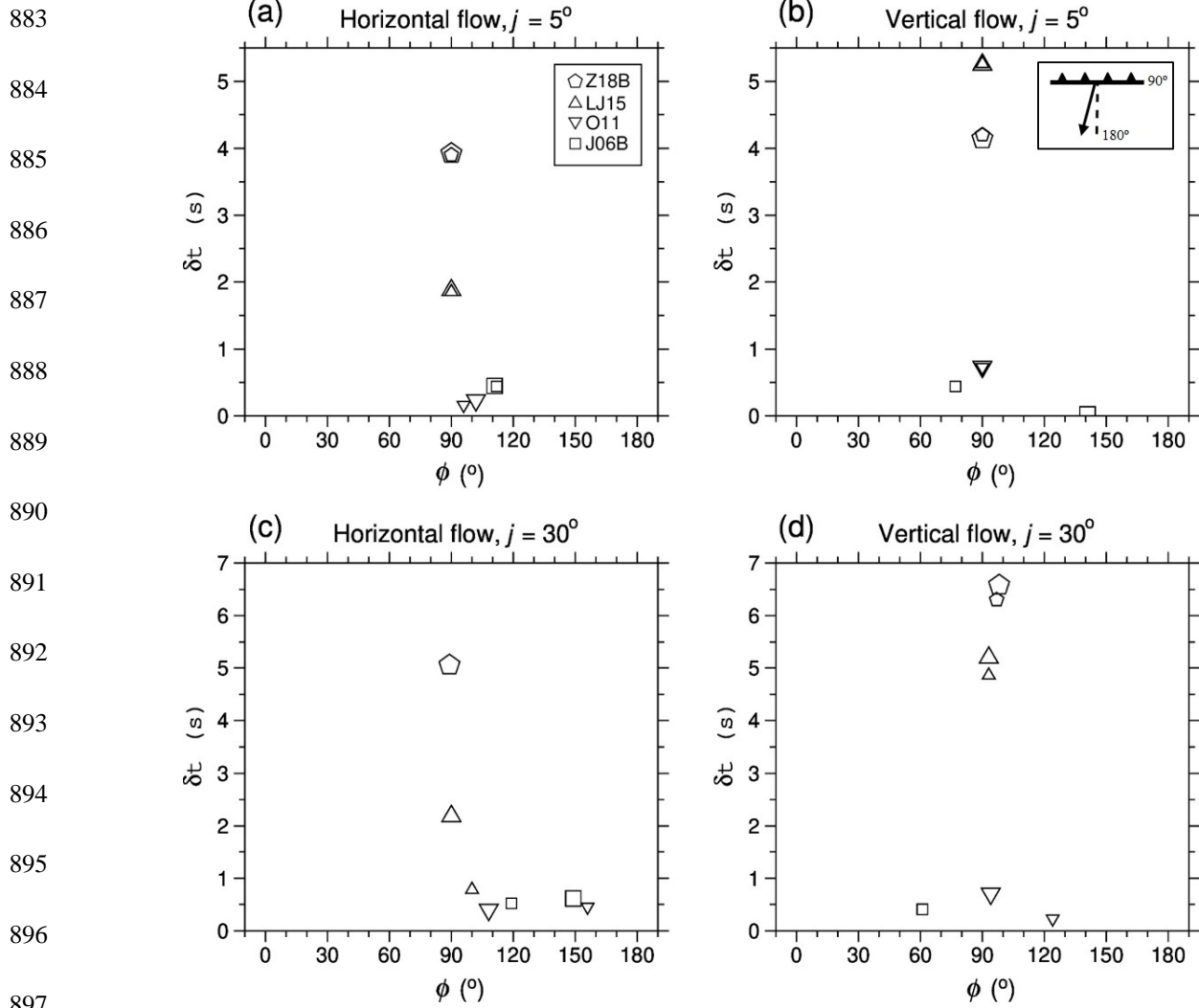
878

879

880

881

882



899 Fig. 8. The same as Figure 7 but for B-type olivine models. Z18B and LJ15 produce mostly trench-
 900 parallel ϕ for both horizontal and vertical flow with different incidence angles. For O11 and J06B
 901 whose anisotropy is weak, splitting can be polarization sensitive or unresolvable. B-type olivine
 902 with trench-parallel splitting is a viable contributor to the observed anisotropy.

903

904