

## **SEISMIC RELIABILITY OF RC BUILDINGS MADE WITH EAF CONCRETES**

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### **Abstract**

*The development of sustainable concretes is becoming an emerging issue in civil construction sector. The use of recycled aggregates is one way to fulfill sustainability goals in concrete industry, and among others, Electric Arc Furnace (EAF) slag aggregates has been proven to be promising. Past research demonstrated a significant increase of mechanical properties of EAF concretes when compared with ones made with natural aggregates (NA); however, at the same time, their use implies also an increase of self-weight loads. The present study aims therefore to investigate the seismic reliability of reinforced concrete frame buildings made with EAF, and compare it with the same structural configurations built with NA mixes, in order to show how the change in mechanical properties and self-weight can impact the seismic response of the analyzed case-studies.*

**Keywords:** EAF slag, reinforced concrete moment frames, seismic fragility, seismic reliability.

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## 1 INTRODUCTION

Construction waste reduction is one of the main goals construction industry has to face in the upcoming years [1]. Recycling and reuse are seen as the main policies for waste reduction disposal and a lot of studies and research has been done on achieving this objective. Recycled Aggregates (RAs) production is one of the main uses of Construction and Demolition Waste (C&DW) and their use is allowed in most countries around the world [3-5]. Among RAs from C&DW, recently, other kind of waste, mostly originating from industrial processes, have been object of research to evaluate their possible use to produce RAs or so-called industrial aggregates. Only in Europe, nearly 2.7 billion tonnes of natural aggregates are consumed each year [2]. Previous research has shown that among all industrial waste or by-products, those coming from steelmaking industry, particularly electric arc furnace (EAF) slag, offer the best performance when used in structural concrete. Particularly has been observed that EAF slag use enhances both mechanical strength [6-10] (i.e compressive strength, tensile strength and elastic properties) and durability [11-13] of concrete mixtures when compared to ordinary ones. Another difference worth highlighting is heavy-weight metals presence in the EAF slag composition which gives EAF concrete mixtures a higher specific weight with respect to NA mixtures. [14-15] have demonstrated that reinforced concrete (RC) elements with EAF slag aggregates manifest better flexural and shear capacity with respect to ordinary RC when tested to monotonic loading under four-point bending. Columns under uniaxial compression has shown a similar ductility to that of NA mixtures [17] while a higher shear strength of exterior beam-column joint is observed [18]. Experiments of EAF concrete joints under cyclic loading have shown a gain with respect to NA ones in terms of ductility, dissipated energy and reduced cracking patten. The same results were obtained even for a joint made with a minor cement amount [18]. Bond properties, between reinforcement and concrete, are also improved when using EAF slag aggregates [16]. Other beam-column joint conditions (i.e strong beam – weak column and strong column – weak beam situations) have been numerically investigated [19].

EAF concrete has found different applications, especially in gravity structures that require shielding from radiations where its high specific weight and high strength can be better exploited [20]. However, no studies have been made to investigate the efficacy of EAF slag concrete when applied in elevation RC structures, particularly, in seismic regions where an important change of the building mass can lead to a variation of the vibration modes and fundamental periods, impacting so the seismic loads acting in the structure elements.

Therefore, the present study aims to investigate this topic, analyzing the seismic response of code conforming RC frame buildings designed with ordinary NA concretes then replaced with three different EAF concrete classes characterized by different aggregates replacement ratios. For the mechanical properties' definition of EAF concrete mixtures a dataset of experimental tests based on two previous research works of some of the authors [21-22] is used. Mean mechanical properties, ratios of variation and self-weight were extracted via statistical processing for three EAF concrete classes (C1, C2, A) with respect to a benchmark mixture realized with NAs. For the purpose, three RC frame structures with three, six and nine stories were designed according to the current Italian Code for Constructions [5] for a medium-to-high seismic hazard site. From these an overall of 12 models resulting from the combinations of 3 structural configurations and 4 concrete mixes, were created. Fragility functions were then computed from the seismic responses of the analyzed configurations under a set of non-linear time history analysis (NLTHAs) and a seismic reliability assessment was carried out for all 12 combinations, investigating the variation of structural safety margins related to the use EAF concrete mixtures in replacement to a conventional NA concrete.

## 2 EAF SLAG AND ITS USE AS AGGREGATE IN STRUCTURAL CONCRETE

EAF slag properties depend on several factors, such as the type of steel to be produced, scrap composition, slag cooling method and speed, and further weathering process. Its composition includes mainly iron, calcium, silicon and aluminum oxides [23]. Usually, before the raw product is ready to be used as a recycled aggregate, it must pass through a weathering protocol [23] to reduce the volumetric instability of the matrix. The main properties of the slag for two size fractions compared, with a dolomitic aggregate, are reported in Table 1.

	Apparent density (kg/m <sup>3</sup> )	Water absorption (%)	Porosity (%)	shape
EAF slag 0-4 mm	3800	1.0 – 1.5	2.0	Crushed
EAF slag 4-16 mm	3950	<1.0	0.5 – 2-7	Crushed
NA 0-4 mm	2760	1.0 1.5	< 2.0	Roundish
NA 4-16 mm	2790	<0.5	0.9 – 1.8	Roundish

Table 1: Physical properties of EAF slag compared to dolomitic aggregate (NA).

The properties of the concrete matrix with EAF slag aggregates depends on type and amount of substitution. Generally coarse aggregates improve mechanical properties, while fine fraction affect is minor [12]. Workability of EAF concrete is highly reduced by high porosity and the crushed shape that characterizes the slag. Another important variation is observed on the specific weight of EAF concrete. Compared to a conventional NA concrete, the use of EAF slag can increase the specific weight of the matrix up to 15-20%. While gain in mechanical properties depends on slag type and fraction size, it seems that specific weight increase is almost constant and is not affected by these factors. Elastic modulus is also improved when using EAF slag. This is mainly because concrete elastic modulus depends mainly on the aggregates elastic modulus. The overall property improvements are also due to the interfacial transition zone between EAF aggregate and cementitious matrix. If a bad quality cementitious matrix or a high water/cement ratio is employed property enhancements are less important.

## 3 RC FRAME CODE-CONFORMING ANALYZED CASE STUDIES

To analyze the seismic response of different buildings built with EAF concrete three moment frame RC structures with 3-, 6-, and 9- stories were considered. The structures are characterized by a rectangular shape with five spans in the longitudinal direction and three in the transversal one. Span length is equal to 5 m in both directions.

The structures were designed in accordance with the Italian Building Code [5] considering a moderate-to-high seismic hazard site (Municipality of Pordenone, Northeast Italy) and a low ductility class (Class B). Seismic actions were computed from a dynamic linear analysis while beams and columns were designed accordingly using a C25/30 conventional concrete class.

## 4 THEORETICAL BACKGROUND ON SEISMIC RELIABILITY ANALYSIS

The occurrence of main shock events at a given site is assumed to be a Homogenous Poisson Process for the Performance-Based Earthquake Engineering (PBEE) framework [24]. So, the process of events causing structural failure is also a HPP and its unique parameter, failure rate  $\lambda_f$ , can be used for computing the failure probability at any time. The failure rate depends on the seismicity of the site (hazard curve  $\lambda_{im}$ ) and on the structural behavior (fragility curve  $P[f|im]$ ) [25-29].  $\lambda_f$  is computed by applying the Total Probability Theorem as:

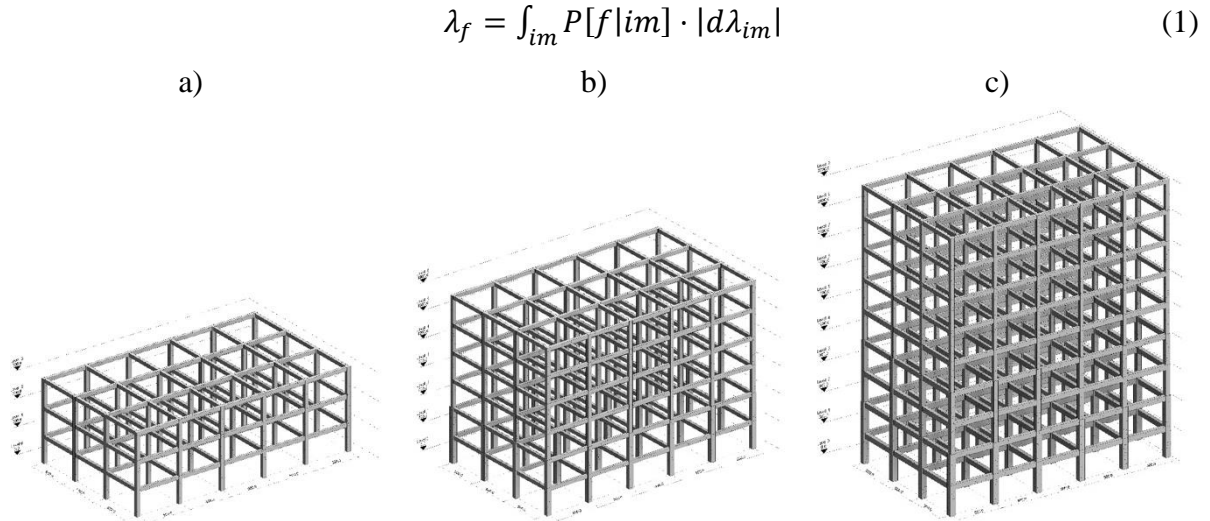


Figure 2: RC frame layouts analyzed: 3- (a), 6- (b) and 9-story (c) building archetypes.

#### 4.1 Seismic hazard estimation

The so-called Probabilistic Seismic Hazard Analysis [30-31], for the computation of  $\lambda_{im}$  associates to each  $im$  value, the annual rate of events that exceed it at a given site. The seismicity of a given area  $d_i$  defined by three main components: the earthquake occurrence model, the spatial seismogenic model and the attenuation model.  $|d\lambda_{im}|$  represents the mean number of events per year with an intensity of exactly  $im$  and is obtained as:

$$|d\lambda_{im}| = -\frac{d\lambda_{im}}{d(im)} d(im) \quad (2)$$

On the other hand,  $\lambda_{im}$  is obtained via the following PSHA integral:

$$\lambda_{im} = \sum_{i=1}^{n_{SZ}} \nu_{m_{min,i}} \int_{m_{min,i}}^{m_{max,i}} \int_{r_{min,i}}^{r_{max,i}} P[IM > im|m, r] f_{M_i}(m) f_{R_i}(r) dm dr \quad (3)$$

where  $\nu_{m_{min,i}}$  is the rate of occurrence of earthquakes greater than a suitable minimum magnitude  $m_{min,i}$  of the  $i^{th}$  seismogenic zone (SZ),  $f_{M_i}(m)$  is the magnitude distribution for the  $i^{th}$  SZ and  $f_{R_i}(r)$  is the distribution of the source  $i^{th}$ -to-site distance. Given a combination of magnitude  $m$  and distance  $r$ ,  $P[IM > im|m, r]$  is the probability to exceed  $im$ . The seismic hazard map for Italy is provided by the National Institute of Geology and Volcanology (INGV) [32]. To compute the failure rate a continuous hazard function is needed. Since INGV provides hazard data (values of the 16<sup>th</sup>, 50<sup>th</sup> and 84<sup>th</sup> percentile) only for nine return times, it is possible to fit the median values (i.e., the 50<sup>th</sup> percentile) with a quadratic function in the logarithmic space as:

$$\lambda(s) = k_0 e^{(-k_1 \ln(s) - k_2 \ln^2(s))} \quad (4)$$

In assessing seismic reliability, instead of the median hazard curve, it is more suitable to refer to the mean one which is possible to derive with the following equation:

$$\bar{\lambda}(s) = \lambda(s) e^{\left(\frac{1}{2}\beta_H^2\right)} \quad (5)$$

where  $\beta_H$  can be estimated as:

$$\beta_H = \frac{\ln(S_{84\%}) - \ln(S_{16\%})}{2} \quad (6)$$

#### 4.2 Seismic fragility analysis

The fragility function ( $P[f|im]$ ) represents the probability to reach and exceed a certain damage state given a specific intensity  $im$ . Several frameworks for fragility function estimation exists in literature, the most popular ones are the Incremental Dynamic analysis [33], the Cloud Analysis [34] and the Multi-Stripes Analysis [35].

In this work the Cloud Analysis method is adopted. The fragility parameters are estimated starting from a set of  $n$  natural ground motion records. The fragility function is computed as follows:

$$[f|im] = P[EDP > \overline{edp}|im] = 1 - P[EDP \leq \overline{edp}|im] = 1 - \Phi \left[ \frac{\ln(\overline{edp}) - \ln(edp)}{\beta} \right] \quad (7)$$

$\overline{edp}$  is the median threshold value of the assumed structural limit state, and  $edp$  represents the median estimate of the demand that can be computed with a ln-linear regression model, as:

$$\ln(edp) = a + b \cdot \ln(im) \quad (8)$$

$\beta$  is the standard deviation of the demand conditioned on  $im$  and can be estimated from the regression of the seismic demands as:

$$\beta_H = \frac{\ln(S_{84\%}) - \ln(S_{16\%})}{2} \quad (9)$$

### 5 SEISMIC RELIABILITY ASSESMENT OF THE ANALYZED EAF RC FRAME ARCHETYPES

NLTHAs were carried out with SeismoStruct software [36]. A diffused plasticity model, using a fiber section discretization, was adopted to consider material non-linearities. Unconfined and confined concrete was modeled via the Mander et al. [37] model whereas the Menegotto-Pinto [38] steel model was used for the non-linear behavior of rebars. EAF concrete characteristics are computed using the ratio coefficients in Table 2 and the reference concrete material (C25/30) characteristics.

	Class EAF-C1	Class EAF-C2	Class EAF-A
$\rho_{c,EAF} / \rho_{c,Ref}$	1.166	1.166	1.154
$f_{c,EAF} / f_{c,Ref}$	1.395	1.404	0.915
$f_{ct,EAF} / f_{ct,Ref}$	1.280	1.100	1.080
$E_{c,EAF} / E_{c,Ref}$	1.330	1.100	1.040

Table 2: Ratios between EAF and Reference concrete properties.

Fragility analysis is computed from a set of point data representing the Intensity Measure (IM) of a given seismic event and the corresponding non-linear response parameter (i.e Engineering Demand Parameter (EDP)). Since the Performance Based Earthquake Engineering was introduced, many researchers have tried to study IM and EDP parameters that best describe structure response under seismic excitation [39-41]. In the present paper, the chosen EDP parameter is the maximum interstory drift ratio (IDR) while the peak ground acceleration (PGA) is used as IM. In addition, four damage states: Slight, Moderate, Extensive and Complete, with corresponding EPD threshold of 0.4%, 0.8%, 1.5% and 3%, were defined.

Threshold values result similar to those proposed for ductile RC moment frame structures by [39] and were defined from non-linear static analysis. For the mid-rise and high-rise buildings, a reduction factor of respectively 2/3 and 1/2 as proposed by [42] was considered to account for higher mode effects and differences between average computed in a non-linear static analysis and maximum individual IDR from NLTHAs.

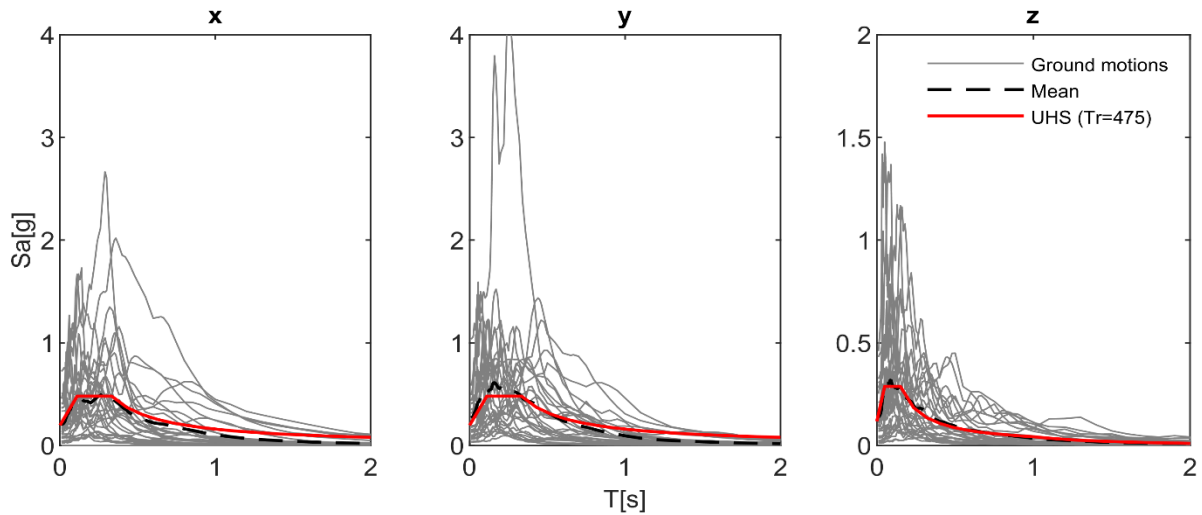


Figure 3: Selected seismic records: X-, Y- and Z- direction.

## 6 RESULTS AND DISCUSSION

For the NLTHAs a set of 30 natural unscaled ground motion records were adopted. In the seismic simulation all three components of the seismic wave, which spectral response is shown in figure 3, were considered. The structural response was then evaluated with respect to the four DSs previously defined, varying from Slight to Complete. Fragility functions were computed for each of the 12 cases, resulting from different geometrical and material combinations, using the Cloud Method described in Section 4.2.

Fragility curves for Slight, Moderate, Extensive and Complete damage are shown in Figure 4 in green, yellow, orange and red color respectively. Additionally, solid lines were used for frames realized with the reference concrete; instead, dotted, dashed and dash-dot lines were used for EAF-C1, EAF-C2 and EAF-A concretes, respectively.

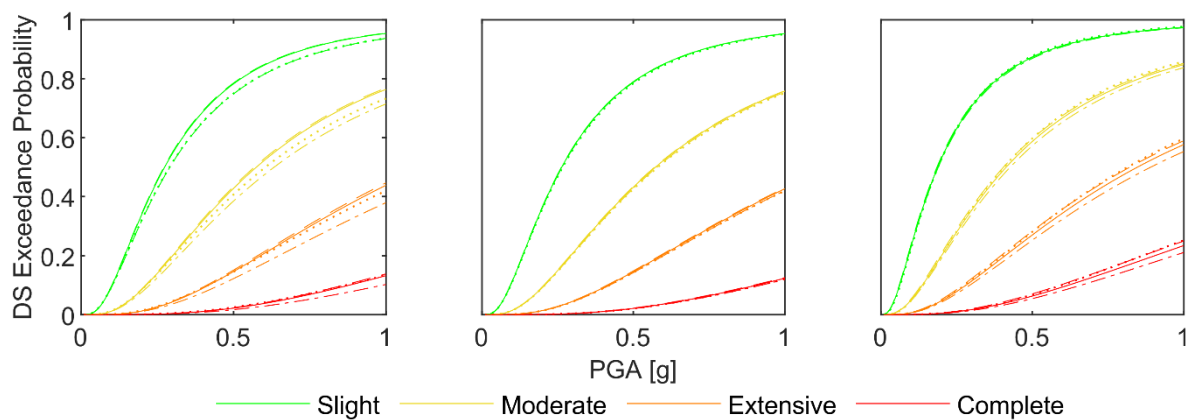


Figure 4: Slight, Moderate, Extensive and Complete DS fragility curves for 3- (a), 6- (b) and 9- (c) story RC frame archetypes (Solid - reference material (C25/30); Dotted - EAF-C1; Dashed - EAF-C2; Dash-dot – EAF-A).

A comparison of the seismic performance of structures built with the reference concrete and EAF concrete is given in Figure 4. It can be noted that the overall performance of EAF concrete structures is close to the performance of the reference material one. The 6- story model has shown almost the same response for all considered materials, proven by the overlapping fragility curves, while the 3- and 9- story curves tend to vary more when considering different materials. Comparing the fragility curves for the different geometrical configurations considered, is noted that 3- and 6- story buildings fragilities result similar for all DSs considered, while the 9 story building results more vulnerable under seismic solicitation with respect to the low- and mid-rise buildings.

Mean failure rates were also computed for all building frames (Table 3). When compared to the reference material the EAF concrete buildings report similar mean failure rate values. This confirms that in terms of safety margins with respect to seismic actions, buildings designed with ordinary concrete but built with EAF aggregates are exposed to almost the same risk as those realized with NAs ones. This highlights that NAs replacement with EAF aggregates, in the same structural system, has a small impact in terms of seismic reliability levels achieved. It is also observed that the mean failure rate for the 9-story building is almost twice the ones computed for the 3- and 6- story archetypes. This great difference may be affected by the reduced damage states EDP threshold adopted for the 9- story by considering it a high-rise building but it also points out that current code recommendations does not guarantee building design characterized by the same level of seismic reliability but often some differences can be observed, especially when comparing different rise buildings.

The construction of the three hypothesized models would require more than 2000 m<sup>3</sup> of concrete. In terms of environmental benefits, considering about 1700kg of NA/m<sup>3</sup> in a mix design for a reference concrete, nearly 3400 tons of NA could be saved if natural material would be fully replaced with EAF slag.

DS	Story	C25/30	C1-EAF	C2-EAF	A-EAF
Slight	3-	4.31E-03	4.28E-03	4.37E-03	4.22E-03
	6-	4.97E-03	4.91E-03	5.05E-03	4.94E-03
	9-	1.08E-02	1.02E-02	1.12E-02	1.08E-02
Moderate	3-	8.98E-04	9.23E-04	9.23E-04	8.27E-04
	6-	9.93E-04	9.77E-04	1.01E-03	9.76E-04
	9-	2.46E-03	2.39E-03	2.61E-03	2.34E-03
Extensive	3-	1.80E-04	1.93E-04	1.88E-04	1.55E-04
	6-	1.89E-04	1.85E-04	1.94E-04	1.83E-04
	9-	5.27E-04	5.30E-04	5.78E-04	4.80E-04
Complete	3-	2.43E-05	2.76E-05	2.58E-05	1.90E-05
	6-	2.36E-05	2.31E-05	2.45E-05	2.26E-05
	9-	7.71E-05	8.13E-05	8.80E-05	6.58E-05

Table 3: Comparison between mean failure rates derived for 3-, 6- and 9-story RC frame archetypes.

## 7 CONCLUSIONS

The main goal of this paper was to investigate the seismic performance of different code conforming RC-frame archetypes (3-, 6- and 9- stories) built with different substitution rates of NAs with EAF slag. The impact of EAG slag in weight and stiffness variation can change the

eigen values of the structure, therefore, seismic loads and global response of the building. A seismic reliability assessment was carried out and mean failure rates were computed for each combination of geometrical configuration and concrete type considered starting from the fragility functions derived with the cloud analysis for four DSs. Based on the results of the present study the following conclusions can be highlighted:

- Using materials that were proved to have higher mechanical strength than the reference one, might not improve the global seismic behavior of the structure.
- The seismic reliability analysis demonstrates that when replacing NAs of ordinary concrete with EAF ones the seismic safety levels achieved are comparable to those of the same structural configuration built with ordinary concrete.
- For the low- and mid- rise buildings considered (3- and 6- stories) results showed a similar mean failure rate, while a significant variation was observed for the high-rise case (9- story). This marks out how current building codes may not ensure the same seismic reliability level for higher structures as for low- and mid- rise ones.

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