The Gaia-ESO Survey: evidence of atomic diffusion in M67?


Affiliations are listed at the end of the paper

1 INTRODUCTION

Based on the commonly accepted knowledge that most stars form in associations or gravitationally bound clusters that dissolve with time and release their members into the field population (Lada & Lada 2003), the suggestion that stars can be traced back to their parent cluster based on their chemical composition, the so-called chemical tagging (see e.g. Freeman & Bland-Hawthorn 2002), has become very popular over the past years.

While chemical tagging is a potentially powerful tool for the understanding of the Galactic evolutionary history, there are limitations to this method that need to be accounted for. In fact, the common and reasonable assumption that stars born as a single stellar population from the same molecular cloud share the same chemical composition only holds for the initial surface abundances, which may vary as stars start following their evolutionary track. During the life of a star, several physical processes are at play in modifying its surface chemical composition. Although these changes are not dramatic, they do put constraints on the resolution achievable in studies of chemical tagging (see e.g. Blanco-Cuaresma et al. 2015 for chemical tagging applied to open clusters). In addition, two stars formed from two different molecular clouds might happen to present the same surface abundances. This could be because the clouds of origin shared the same chemical composition or because the two objects have different mass and find themselves in different evolutionary stages, which might have led by chance to the same surface abundances, even if the initial ones were different (see e.g. Dotter et al. 2017; Ness et al. 2018). In this scenario, it would be impossible to tag the two stars back to a particular cluster of origin based on their present-day chemical composition alone. As Dotter et al. (2017) suggested, one would need to use stellar evolutionary

ABSTRACT

Investigating the chemical homogeneity of stars born from the same molecular cloud at virtually the same time is very important for our understanding of the chemical enrichment of the interstellar medium and with it the chemical evolution of the Galaxy. One major cause of inhomogeneities in the abundances of open clusters is stellar evolution of the cluster members. In this work, we investigate variations in the surface chemical composition of member stars of the old open cluster M67 as a possible consequence of atomic diffusion effects taking place during the main-sequence phase. The abundances used are obtained from high-resolution UVES/FLAMES spectra within the framework of the Gaia-ESO Survey. We find that the surface abundances of stars on the main sequence decrease with increasing mass reaching a minimum at the turn-off. After deepening of the convective envelope in subgiant branch stars, the initial surface abundances are restored. We found the measured abundances to be consistent with the predictions of stellar evolutionary models for a cluster with the age and metallicity of M67. Our findings indicate that atomic diffusion poses a non-negligible constraint on the achievable precision of chemical tagging methods.

Key words: stars: abundances – stars: evolution – Galaxy: abundances – Galaxy: evolution.

⋆ E-mail: cbertelli@ari.uni-heidelberg.de

© 2018 The Author(s)
Published by Oxford University Press on behalf of the Royal Astronomical Society
models to infer the initial abundances of stars from the observed ones.

Stellar evolutionary effects are best studied with a sample of stars belonging to the same stellar population and most likely sharing the same initial chemical composition. While globular clusters are known to host two or more populations of stars with different light-element abundances among their members (see e.g. Gratton, Sneden & Carretta 2004; Kayser et al. 2008; Carretta et al. 2009; Gratton, Carretta & Bragaglia 2012), this is not the case for open clusters (see e.g. Bragaglia et al. 2012; Bragaglia et al. 2014; Carraro et al. 2014), which are therefore ideal test benches for our study. Unfortunately, for most open clusters only the brighter stars in the red clump (RC) and upper red giant branch (RGB) are usually considered for spectroscopic studies, mainly because the main sequence (MS) and the turn-off (TO) regions are usually relatively faint and require very long exposure times. This makes it difficult to find in the literature suitable data for the investigation of evolutionary effects, which require stars at different evolutionary stages. Furthermore, we also need to test these effects in a range of metallicity and age (i.e. stellar mass).

In this framework M67 plays a special role. With an age of 3.75–4 Gyr (see e.g. Sarajedini, Dotter & Kirkpatrick 2009; Bellini et al. 2010; Kharichenko et al. 2013), a distance of 800–900 pc from the Sun (see e.g. Sarajedini et al. 2009), and approximately solar metallicity (see e.g. Shetrone & Sandquist 2000; Tautvaisiene et al. 2000; Yong, Carney & Teixera de Almeida 2005; Randich et al. 2006; Pace, Pasquini & François 2008; Ŭnojha, Gustafsson & Korn 2014; Bertelli Motta et al. 2017), this old open cluster is considered a proxy for solar studies and is used as a calibrator in many spectroscopic surveys. M67 hosts a solar twin with one of the most similar chemical compositions to the Sun discovered so far (M67-1194; Ŭnojha et al. 2011) and is subject to a search for extrasolar planets around its member stars (Pasquini et al. 2012; Brucalassi et al. 2014, 2016, 2017). It has been speculated that this old open cluster could be very similar to (or even be) the environment in which the Sun formed. For all these reasons M67 has been studied in great detail in the past and, unlike most open clusters, high-resolution spectra of a large number of cluster members in all evolutionary stages are available for analysis, making M67 an excellent test case for evolutionary studies.

Atomic diffusion (see Michaud, Alecian & Richer 2015) is expected to alter the surface abundance of stars during the main-sequence phase due to the combined effect of gravitational settling, causing different elements to sink towards the interior of the star, and radiative acceleration working against it. In low-mass stars, the overall trend is similar for all elemental species: surface abundances decrease along the MS with increasing stellar mass, reaching a minimum at the TO. The amplitude of the abundance variation between the early MS and the TO depends on the efficiency of radiative acceleration, i.e. on the degree of absorption of the outgoing photon flux for the different species. When the outer convective zone becomes deeper (after the TO), material from the stellar interior is brought to the surface. For most elements, this means a recovery of the initial surface abundances, with the exception of species that undergo nuclear processing, such as $^3$He, Li, Be, and B (the surface abundances of C and N also vary due to the dredge-up of the material involved in the CNO cycle once the convective envelope reaches the innermost part of the star, see Bertelli Motta et al. 2017, and references therein). While metals sink towards the stellar interior, hydrogen is pushed into the outer layers, depriving the nucleus of fuel and thus shortening the life of the star on the MS (see e.g. Salaris & Weiss 2001 and Jofrée & Weiss 2011). This poses a further constraint on chemical tagging, since taking into account diffusion when estimating the age of a cluster through isochrone fitting can reduce ages by up to $\sim$10 per cent for the oldest globular clusters. The reduction in age is proportionally smaller for younger systems such as open clusters, but still present.

Thus, in order to study atomic diffusion, stars along the MS, TO, subgiant branch (SGB), and RGB are needed. In Bertelli Motta et al. (2017), we investigated the effects of the first dredge-up affecting stars on the SGB and lower RGB of M67 with data from the Apache Point Observatory Galactic Evolution Experiment – APOGEE – (see Majewski et al. 2017). M67 was furthermore included in the study of Šmiljanic et al. (2016) where, using data from the Gaia-ESO Survey (GES; Gilmore et al. 2012; Randich, Gilmore & Gaia-ESO Consortium 2013), the authors investigated variations in Na and Al abundances as a consequence of mixing processes in the stellar interiors. In this work, we extend this study to the variations in surface abundances due to atomic diffusion by investigating the MS, TO, SGB, and RGB phase of M67 with GES data.

In Sections 2 and 3, we present the data set and the models used for comparison in this study. In Section 4, we present the results and, in Section 5, we discuss them together with possible caveats. Finally, in Section 6 we draw our conclusions.

2 DATA

One of the main goals of GES is the observation of a large number of open clusters covering a wide range in age, mass, metallicity, and Galactocentric distance. This is achieved by combining observations with FLAMES–GIRAFFE and FLAMES–UVES at the Very Large Telescope (VLT; see e.g. Dekker et al. 2000; Pasquini et al. 2002). Main-sequence and TO stars in old open clusters were normally observed with the GIRAFFE set-ups HR9B ($514.3–535.6$ nm, $R \sim 32$ 000) and HR15N ($647–679$ nm, $R \sim 20$ 000). They cover a wavelength range that allows for precise measurements of the radial velocity, in addition to the abundances of Fe, Cr, and Ti for HR9B, and of Ca, Ti, Si, Al, and Li for HR15N, although with low precision. High-precision abundances of a large number of chemical species were calculated from FLAMES–UVES spectra generally obtained for stars on the MS, RGB, and on the RC with the set-up U580 ($200$ nm around the central wavelength $580$ nm, $R \sim 47$ 000). M67 is included in the list of open clusters analysed within GES. The observations were collected from the ESO archive. In particular, they were part of the program 082.D–0726 (PI Gustafsson), which observed with FLAMES–UVES 25 stars in the field of M67 in all evolutionary stages between the MS and the lower RGB (see Table 1). Thus, M67 is one of the few clusters in GES for which detailed chemical abundances from high-resolution spectroscopy are available for stars on the MS, TO, and RGB.

Fourteen of the stars distributed on the MS, TO, and early SGB branch were analysed in Ŭnojha et al. (2014), who searched the data for possible diffusion effects. They found differences in abundance between stars at the upper MS and TO stars on the SGB of the order of $\sim$0.02 dex (we note that they divide the sample that we define as TO in this work into TO and early SGB and compare the abundances of the first two with those of the third group). Although their results were not conclusive, also due to the small variation in abundances predicted by the models between these groups of stars, they seemed to support the presence of atomic diffusion.

We used the recommended results of the GES fifth internal data release (GES iDR5) for all the 25 stars and performed a membership analysis based on their radial velocities. We first excluded all stars known as binaries from Geller, Latham & Mathieu (2015).
We then computed the mean radial velocity of the remaining 17 stars \((RV_{\text{mean}} = 34.54 \pm 0.83 \text{ km s}^{-1}\)) and found that all stars lie within \(3\sigma\) from this value. The mean error on the radial velocity (0.36 km s\(^{-1}\)) is smaller than the internal dispersion. This result is consistent with other mean radial velocity determinations of M67 known from the literature (see e.g. Yadav et al. 2008; Geller et al. 2015) within few \(\sigma\). In addition, we cross-matched the sample with the Hot Stuff for One Year (HSOY) catalogue (Ałtmann et al. 2017) in order to check also the mean proper motion (PM) of the cluster \((\bar{\mu}_R = -9.67 \pm 0.64 \text{ mas yr}^{-1}, \bar{\mu}_\text{Dec} = -3.35 \pm 0.88 \text{ mas yr}^{-1})\). We excluded one star that does not have an entry in the HSOY catalogue, and one because its PM is inconsistent with that of the cluster. Moreover, we verified that the 2MASS photometry (Skrutskie et al. 2006) of the remaining 15 stars is consistent with a 3.75 Gyr PARSEC isochrone (Bressan et al. 2012) calculated with \((m - M)_0 = 9.64 \text{ mag, } E(B - V) = 0.023 \text{ mag, and [Fe/H]} = 0.06 \text{ dex (Bellini et al. 2010; a list of the selected members and their parameters can be found in Table A1. This leaves 11 stars in common between our sample and the sample from Ònehag et al. (2014). We excluded three of their stars during our membership analysis (one as a binary and two because of PM criteria) and gained four additional ones along the SGB and lower RGB (see Table 1). In particular, the inclusion of three RGB stars into our analysis is of great importance for the study of diffusion effects. In addition, we transformed the s parameter of the M67 members selected from the GES archive plotted using 2MASS photometry as a function of their \(T_{\text{eff}}\) derived within GES. Main-sequence stars are plotted as green diamonds, TO stars as blue squares, and red giant stars as red circles. The star S806 is plotted as an orange triangle. The solar twin M67-1194 is plotted as a green cross. The stars selected in Ònehag et al. (2014) are plotted as black circles. The solid line represents the isochrone from Michaud et al. (2004) for an age of 3.7 Gyr.

Evidence of atomic diffusion in M67?

For all the 15 stars in our sample, the chemical analysis was performed by GES working group (WG) 11, responsible for the analysis of UVES F, G, K stars (see Smiljanic et al. 2014 for a description of the abundances derivation and Sacco et al. 2014 for details about the reduction of UVES data).

In the GES iDR5 archive, abundances are given in the form

\[ A(X) = \log{(X/H)} + 12, \]

and we transformed them for our purposes into

\[ [X/H] = \log{(X/H)} - \log{(X_{1194}/H_{1194})} \]

subtracting the GES abundances of the solar twin M67-1194 [ID \(08510080+1148527, A(X)_{1194}\)] from \(A(X)\).

3 MODELS

We compared the results with the stellar evolutionary models calculated in Michaud et al. (2004) (with an extension of the calculation to a slightly older age for the 1.35 solar mass model) for stars of solar metallicity, ages of 3.7–4 Gyr, and masses ranging from 0.5 to 1.4 \(M_\odot\). The calculations follow the description of Turcotte et al. (1998) and Richard, Michaud & Richer (2001), including gravitational settling and radiative acceleration. Whereas all chemical species are affected by gravitational settling during the MS, different elements experience a varying amount of radiative acceleration, depending on the fraction of the total photon flux they absorb. After the TO, the convective envelope deepens into the stellar interior and the effects of atomic diffusion are subverted, thus restoring in most cases the original surface abundances. Fig. 1 compares the \(K_s\) magnitude (2MASS), corrected for reddening, of the stars in our sample as a function of the effective temperatures derived by

\[ K_s \text{ magnitude (2MASS), corrected for reddening, of the stars in our sample as a function of the effective temperatures derived by} \]

\[ A(X) = \log{(X/H)} + 12, \]

and we transformed them for our purposes into

\[ [X/H] = \log{(X/H)} - \log{(X_{1194}/H_{1194})} \]

subtracting the GES abundances of the solar twin M67-1194 [ID \(08510080+1148527, A(X)_{1194}\)] from \(A(X)\).

3 MODELS

We compared the results with the stellar evolutionary models calculated in Michaud et al. (2004) (with an extension of the calculation to a slightly older age for the 1.35 solar mass model) for stars of solar metallicity, ages of 3.7–4 Gyr, and masses ranging from 0.5 to 1.4 \(M_\odot\). The calculations follow the description of Turcotte et al. (1998) and Richard, Michaud & Richer (2001), including gravitational settling and radiative acceleration. Whereas all chemical species are affected by gravitational settling during the MS, different elements experience a varying amount of radiative acceleration, depending on the fraction of the total photon flux they absorb. After the TO, the convective envelope deepens into the stellar interior and the effects of atomic diffusion are subverted, thus restoring in most cases the original surface abundances. Fig. 1 compares the \(K_s\) magnitude (2MASS), corrected for reddening, of the stars in our sample as a function of the effective temperatures derived by

\[ K_s \text{ magnitude (2MASS), corrected for reddening, of the stars in our sample as a function of the effective temperatures derived by} \]
GES with the theoretical isochrones from Michaud et al. (2004) corresponding to an age of 3.7 Gyr. From the plot, it is evident that the calculated effective temperatures are systematically slightly colder but nevertheless agree within the errors with the predicted ones.

The models from Michaud et al. (2004) are divided into two sets of calculations. While the first one does not include turbulent transport, the second one is calculated including a density-dependent turbulent diffusion coefficient that is 400 times the He diffusion coefficient at \( \log T = 6.09 \), and that decreases inwards from there as \( \rho^{-3} \) (hereafter we will refer to this calculation as T6.09). This parametrization of turbulent transport was chosen by Michaud et al. (2004) since it showed a minimization of the Li depletion in Pop II stars (see Richard et al. 2002). The presence of turbulence reduces the effects of gravitational settling and, as a consequence, also the underabundances at the TO, as can be seen in Fig. 2, where the models are plotted as isochrones, each data point representing a different mass (see Table 2 for a summary of the \( T_{\text{eff}} \) and \( \log g \) corresponding to each mass). The turbulent mixing efficiency necessary to match the observed variations in surface abundances due to atomic diffusion has been shown to vary for different globular clusters, more metal-rich clusters needing more efficient mixing (see e.g. Korn et al. 2007; Gruyters et al. 2013, 2016). In the models, the outer atmosphere pressure is obtained using an approximate \( T-\tau \) relationship (where \( T \) is the temperature and \( \tau \) is the mean optical depth; for details see Krishna Swamy 1966; Michaud et al. 2004).

In interpreting abundance isochrones, for instance of M67, it is worth remembering that for \( T_{\text{eff}} \lesssim 5000 \) (or \( \log g < 3.6 \)) the dredge-up is essentially complete for those species that have not been influenced by nuclear reactions. This implies, for instance, that the lowest log \( g \) points in Fig. 2 (\( \log g \sim 3.3 \)), dashed lines) would have been at very nearly the same abundance when \( \log g = 3.6 \) for that star. The shape of the isochrones is affected by the finite (and small) number of models calculated and so by the small number of straight line segments available for the isochrones. The convergence of abundances for the models with and without turbulence is shown on Fig. A1.

4 RESULTS

In the following, we present the results of our study and compare the measured abundances from the GES data with the models of Michaud et al. (2004). In Fig. 2, the elemental abundances of stars from the MS, SGB, and RGB are plotted as a function of log \( g \). The abundances shown and discussed in this work refer to the elements in their neutral state. We present and discuss in this work only elements for which we have both the measured abundances from GES iDR5 and the predictions from the models by Michaud et al. (2004). The star with GES-ID 08510017+1154321 is highlighted as an orange triangle for the reasons explained in Section 5.1. The solar twin M67-1194 is plotted as a green cross and is not included in the calculations when computing the average abundances of the MS stars. In fact, M67-1194 lies on the ‘lower’ MS with respect to the rest of the sample and presents for most elements an abundance more similar to the RGB than to the MS and TO samples, as predicted by the models of Michaud et al. (2004) for stars of the same mass. Models of stellar evolution including turbulent diffusion are shown as a black solid line, while models without turbulence are displayed as a dashed black line.

Since the effects of diffusion on the stellar surface chemical composition is very small (typically less than \( \sim 0.1 \) dex for stars in the mass range of M67 members), precise measurements are required. Indeed, if the scatter of the observationally derived abundances is larger than or even comparable to the expected variation, no sensible conclusion can be drawn. For this reason, we performed a statistical analysis of the abundances aimed at determining which of the elements derived within GES clearly show trends consistent with the effects of atomic diffusion predicted by the models of Michaud et al. (2004).

Table 3 summarizes the mean elemental abundances and relative standard deviations obtained within GES for two groups of stars in M67: the upper MS and the RGB stars. Table 4 shows the difference in surface chemical abundances between these two groups for the species studied in this work, with errors calculated as

\[
\text{err}_{\Delta}[X/H] = \sqrt{\sigma_{\Delta X}^2 + \sigma_{\Delta g}^2}
\]

where \( \sigma_{\Delta X} \) and \( \sigma_{\Delta g} \) are the standard deviations of the abundance distributions of the upper MS and RGB stars, respectively; the last two columns show the maximum difference in surface abundance predicted by the models. We calculated this abundance difference between the models with mass 1.2 M\(_\odot\) along the upper MS, respectively with and without turbulence, and the model with 1.35 M\(_\odot\) on the RGB without turbulence. As already pointed out in Section 3, the models with and without turbulence converge to the same abundances on the RGB (see Fig. A1). Since the models with turbulence are evolved to a slightly younger age than those without turbulence, we compared the 1.2 M\(_\odot\) model with turbulence with the more evolved 1.35 M\(_\odot\) model without turbulence, assuming that the corresponding model with turbulence would show the same abundance at the same age. TO stars were excluded from this discussion because the maximum abundance variation predicted by the models is reached at the log \( g \) corresponding to the upper MS (\( \sim 1.2 \) M\(_\odot\) in the models).

For Al, Si, Ca, Ti, Cr, Mn, and Ni, \( \Delta[X/H] \) is larger than 3 \( \times \) err\_\(\Delta[X/H]\), while for Fe, \( \Delta[X/H] \) is larger than 2 \( \times \) err\_\(\Delta[X/H]\). We conclude that for these elements the presence of a trend in log \( g \) is clear and the offset in surface abundance between upper MS and RGB can be considered statistically significant. \( \Delta[X/H] \) is larger than 1 \( \times \) err\_\(\Delta[X/H]\) for C, O, Na, and Mg making the offset between the two samples less clear, but still visible. [S/H] is available only for stars on the upper MS and on the TO. We will thus exclude S from the following discussion.

For the elements of the oxygen group (O, Na, Mg, Al, Si, and S), the models predict the largest difference between initial surface abundance and values at the TO. This is due to the small radiative acceleration that these elements experience below the surface convection zone (for details, see Michaud et al. 2004, fig. 3). As shown in Fig. 2, the models are consistent with GES [Na/H], [Mg/H], and [Si/H] abundances of the M67 stars within 1 – 3 \( \times \) err\_\(\Delta[X/H]\). For Al, the difference between \( \Delta[X/H] \) and the offset predicted by the models is larger than 3 \( \times \) err\_\(\Delta[X/H]\). As explained above, the measured [O/H] abundances present a large scatter, even if \( \Delta[X/H] \) is consistent with the predictions of the models. This is due to the weakness of the forbidden [O I] line at 630.03 nm used to derive the O abundance and to the fact that the telluric lines in that region are not corrected for by the pipeline.

Species between P and Ti are expected to experience a larger radiative acceleration as compared to lighter elements (see fig. 3 in Michaud et al. 2004). This reduces the effect of gravitational settling, resulting in a much smaller difference between the surface abundances of TO and RGB stars as compared to Al or O. Fig. 2 shows how the [Ca/H] and [Ti/H] both suffer from an offset with...
Evidence of atomic diffusion in M67?

Figure 2. The different panels show from top to bottom and from left to right the abundances of the species analysed in this work as a function of \( \log g \). The symbols are the same as in Fig. 1. We also overplotted models of stellar evolution with (black solid line) and without (dashed black line) turbulence in the stellar interior. Note that the lowest \( \log g \) point of the dashed lines could be horizontally shifted to the left to the same \( \log g \) as the solid lines. The large shift is due to the rapid variation of \( \log g \) with age for the 1.35 solar mass model at that evolutionary stage and the slight age difference between the models with and without turbulence.

respect to the model abundances, which is more prominent for [Ti/H] than for [Ca/H]. Nevertheless, looking at Tables 3 and 4, one can see that a trend in \( \log g \) is present for Ca and Ti and is slightly more pronounced than predicted by the models, but still consistent within \( 3 \times \text{err} \Delta[X/H] \).

Elements of the iron group (Cr, Mn, Fe, Ni) are predicted to experience less radiative acceleration as compared to Ca or Ti, but more than the elements in the oxygen group, resulting in very similar but slightly smaller underabundances at the TO. Cr is systematically underabundant compared to the theoretical predictions. The trend between MS and giant branch is consistent with the models in the case of Cr and slightly smaller for Fe. A similar trend between the TO and the SGB/low-RGB was also found for [Fe/H] by Casey (2016), analysing lower resolution spectra. For Mn and Ni, \( \Delta[X/H] \)
differed by $3 \times \text{err}_{\Delta}[X/H]$ or more from the abundance differences predicted by the models.

We note that, since we are interested in a relative comparison between two groups of stars analysed within GES iDR5 rather than in the absolute abundances of the stars, \text{err}_{\Delta}[X/H]$ is calculated only from the internal scatter of the measured abundances and does not take into account the error of the measurements.

### 5 DISCUSSION

In the following, we discuss the interpretation of the results presented so far as well as possible caveats, such as corrections for Non Local Thermodynamic Equilibrium (NLTE) effects, abundance trends in a cluster for which we do not expect to see diffusion effects, and trends of the abundances of M67 with temperature derived from APOGEE infrared spectra.

#### 5.1 S806

Fig. 2 shows that one star (GES-ID: 08510017+1154321; S806 in the notation from Sanders 1977) in M67 presents for almost all elements investigated in this work higher abundances with respect to its companions. The star matches all criteria (kinematic and photometric) considered in the membership analysis of the cluster, but its chemical composition is not consistent with that of other cluster members with the same gravity.

Of course, the possibility exists that S806 is not a member of M67, although this is not very likely given the perfect match with the clusters kinematics. Nevertheless, the surface abundances measured in S806 cannot be explained by simple stellar evolutionary processes. We therefore need to explain its position on the SGB and its peculiar chemical composition.

A possible explanation for the peculiar surface abundances of S806 (with respect to its log $g$) is that the star might be part of a binary system initially composed of one massive companion, and a secondary companion with a mass of approximately $1.3 \, M_\odot$ now lying on the SGB. If the massive companion evolved into an AGB star and expelled part of its envelope, the surface of the secondary companion would have been polluted by the ejected material (the s-element abundances for S806 are also higher than in the other cluster members). At an age of $\sim 4$ Gyr, the massive companion would have evolved into a white dwarf and thus would not contribute significantly to the luminosity of the binary system. In this scenario, the binary would have to be face-on, since S806 has been classified as a single star in Geller et al. (2015). Alternatively, the system could have been disrupted by encounters with other stars within the cluster. In this case, we would only be observing the low-mass companion.

### Table 4. Difference between the mean abundances (and errors) of selected elements on the upper MS and on the RGB (columns two and three), compared to the theoretical counterpart calculated employing for the upper MS a 1.2 $M_\odot$ model, both with (column 5) and without (column 4) turbulence, and the 1.35 $M_\odot$ model without turbulence for the red giants (see the text for details).

<table>
<thead>
<tr>
<th>X</th>
<th>$\Delta[X/H]$</th>
<th>$\text{err}_{\Delta}[X/H]$</th>
<th>$\Delta[X/H]$</th>
<th>$\Delta[X/H]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>0.053</td>
<td>0.022</td>
<td>0.007</td>
<td>-0.018</td>
</tr>
<tr>
<td>O</td>
<td>0.111</td>
<td>0.084</td>
<td>0.102</td>
<td>0.075</td>
</tr>
<tr>
<td>Na</td>
<td>0.114</td>
<td>0.067</td>
<td>0.115</td>
<td>0.077</td>
</tr>
<tr>
<td>Mg</td>
<td>0.052</td>
<td>0.032</td>
<td>0.113</td>
<td>0.078</td>
</tr>
<tr>
<td>Al</td>
<td>0.222</td>
<td>0.018</td>
<td>0.109</td>
<td>0.077</td>
</tr>
<tr>
<td>Si</td>
<td>0.151</td>
<td>0.027</td>
<td>0.105</td>
<td>0.075</td>
</tr>
<tr>
<td>Ca</td>
<td>0.074</td>
<td>0.017</td>
<td>0.057</td>
<td>0.053</td>
</tr>
<tr>
<td>Ti</td>
<td>0.107</td>
<td>0.027</td>
<td>0.059</td>
<td>0.048</td>
</tr>
<tr>
<td>Cr</td>
<td>0.093</td>
<td>0.015</td>
<td>0.090</td>
<td>0.058</td>
</tr>
<tr>
<td>Mn</td>
<td>0.185</td>
<td>0.032</td>
<td>0.104</td>
<td>0.068</td>
</tr>
<tr>
<td>Fe</td>
<td>0.052</td>
<td>0.025</td>
<td>0.114</td>
<td>0.074</td>
</tr>
<tr>
<td>Ni</td>
<td>0.198</td>
<td>0.020</td>
<td>0.103</td>
<td>0.069</td>
</tr>
</tbody>
</table>

### Table 3. Mean surface chemical abundances and standard deviations for stars on the MS ([X/H]$_{\text{MS}}$) and giant stars ([X/H]$_{\text{RGB}}$) in M67.

<table>
<thead>
<tr>
<th>X</th>
<th>[X/H]$_{\text{MS}}$</th>
<th>$\sigma_{\text{MS}}$</th>
<th>[X/H]$_{\text{RGB}}$</th>
<th>$\sigma_{\text{RGB}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>-0.043</td>
<td>0.010</td>
<td>0.010</td>
<td>0.020</td>
</tr>
<tr>
<td>O</td>
<td>-0.008</td>
<td>0.083</td>
<td>0.103</td>
<td>0.015</td>
</tr>
<tr>
<td>Na</td>
<td>-0.018</td>
<td>0.022</td>
<td>0.097</td>
<td>0.064</td>
</tr>
<tr>
<td>Mg</td>
<td>-0.065</td>
<td>0.024</td>
<td>-0.013</td>
<td>0.021</td>
</tr>
<tr>
<td>Al</td>
<td>-0.145</td>
<td>0.010</td>
<td>0.077</td>
<td>0.015</td>
</tr>
<tr>
<td>Si</td>
<td>-0.028</td>
<td>0.022</td>
<td>0.123</td>
<td>0.015</td>
</tr>
<tr>
<td>Ca</td>
<td>-0.048</td>
<td>0.013</td>
<td>0.027</td>
<td>0.012</td>
</tr>
<tr>
<td>Ti</td>
<td>-0.110</td>
<td>0.022</td>
<td>-0.003</td>
<td>0.015</td>
</tr>
<tr>
<td>Cr</td>
<td>-0.080</td>
<td>0.014</td>
<td>0.013</td>
<td>0.006</td>
</tr>
<tr>
<td>Mn</td>
<td>-0.115</td>
<td>0.027</td>
<td>0.070</td>
<td>0.017</td>
</tr>
<tr>
<td>Fe</td>
<td>-0.055</td>
<td>0.024</td>
<td>-0.003</td>
<td>0.006</td>
</tr>
<tr>
<td>Ni</td>
<td>-0.108</td>
<td>0.017</td>
<td>0.090</td>
<td>0.010</td>
</tr>
</tbody>
</table>
5.2 NLTE effects

The abundances of GES iDR5 are calculated for 1D atmospheres and Local Thermodynamic Equilibrium (LTE). It is therefore interesting to discuss how corrections for NLTE would affect the abundances of the elements under study and if these alone can account for the abundance trends observed.

The upper MS stars of M67 have a mean $T_{\text{eff}} = 6031$ K and log $g = 4.21$ dex. For the giant stars, we find a mean $T_{\text{eff}} = 4875$ K and log $g = 3.24$. In Lind et al. (2011), this corresponds to corrections for the Na abundance of $\sim$−0.15 dex for the 568.2 nm line and of $\sim$−0.1 dex for the 615.4 nm line for both dwarfs and giants (assuming [Fe/H] = 0 dex and [Na/Fe] = 0 dex), thus leaving the offset between the two groups unchanged.

For Al, Nordlander & Lind (2017) predict a correction of $\sim$0.0 dex for the MS stars and of $\sim$−0.1 dex for the RGB stars for the line at 669.6 nm and [Fe/H] = 0 dex, [Al/Fe] = 0 dex. This would indeed diminish the offset observed between MS and RGB in the GES Al abundances, but a clear trend in log $g$ would still be visible.

Zhang et al. (2017) predict for a star with $T_{\text{eff}} = 6070$ K and log $g = 4.08$ an Mg correction in the optical of $+0.01$ dex. This corresponds to our MS group. In the sample of stars analysed by these authors, we could not find any star with the temperature and gravity of the M67 giants. The most similar one has $T_{\text{eff}} = 4901$ K and log $g = 2.76$ and corresponds to a correction of $\sim0.02$ dex in the optical. Thus, in the case of magnesium, the NLTE correction would not significantly change the difference in abundance between MS and RGB.

Similarly, for Si, the corrections calculated by Zhang et al. (2016) in the optical are $−0.01$ and $−0.04$ dex for the MS and the RGB, respectively (using the same objects as for Mg).

Going to heavier elements, NLTE corrections are available only for Fe from Lind, Bergemann & Asplund (2012). The authors calculate corrections of $\sim+0.02$ and $\sim+0.01$ dex for the MS and RGB, respectively, at [Fe/H] = 0 dex. These corrections would not change significantly the overall difference in abundance between the two groups.

5.3 NGC 6633

In the previous section, we have discussed that the abundance trends visible in the stars of M67 cannot be explained by NLTE effects, which remain unaccounted for in the GES iDR5 analysis. In order to be reasonably confident that the trends we observe are indeed due to diffusion effects, we need to rule out systematic offsets deriving from the analysis of stars in different evolutionary stages. We therefore choose a second cluster, NGC 6633, for which stars both on the MS and on the RGB/RC have been observed and analysed in GES iDR5. This cluster is much younger than M67, with an age of $\sim$540 Myr (Randich et al. 2017), and has a slightly subsolar metallicity of [Fe/H] = −0.06 dex (Jacobson et al. 2016).

After performing a membership analysis of the stars observed with UVES in the field of NGC 6633 based on radial velocities and HSOY PMs, we found five MS stars and three stars that could be red giants or RC stars based on their position in the colour–magnitude diagram (CMD). Their $K_s$ magnitude corrected for reddening is plotted as a function of effective temperature (green and red dots, respectively, for MS and RGB stars) in Fig. 3, together with a Padova isochrone with age 540 Myr, [Fe/H] = −0.05 dex and distance modulus $(m - M)_0 = 8.07$ mag (Randich et al. 2017). We also find three further stars on the MS that are probable members of the cluster based on their kinematic properties (orange triangles in Table 5, for all elements of the two groups, $\Delta [X/H]$ is smaller than $(1 - 2) \times \text{error}[X/H]$, i.e. the measured offsets are less significant than for the case of M67.

This is not the case for lighter elements of the oxygen group. Na in particular presents a large difference (0.278 dex) between the mean MS abundance and the average abundance of the giant stars. Nevertheless, this offset could be a physical effect: for stars in the mass range of the NGC 6633 giants ($\sim$2.5 $M_\odot$), we expect to see an enhancement in Na due to mixing effects after the dredge-up (see e.g. Smiljanic et al. 2016 and references therein). Besides, also NLTE effects might play a role: Lind et al. (2011) predict a correction for NLTE effects of the Na abundance between −0.1 and −0.15 dex for the NGC 6633 MS stars (with mean $T_{\text{eff}} = 5463$ K and log $g = 4.48$), and of $\sim$−0.2 dex for the giant stars (with $T_{\text{eff}} = 4995$ K and log $g = 2.74$) for the 568.2 nm line at solar metallicity. For the 615.4 nm line, the correction would be $\sim$−0.1 dex for both groups.

For Mg and Al, an offset is also present, although not as pronounced as for Na ($\Delta [X/H] < 2 \times \text{error}[X/H]$). The effects of mixing for Al should not be visible in stars less massive than 3 $M_\odot$ (Smiljanic et al. 2016) and this offset would probably not disappear
Figure 4. The different panels show from top to bottom and from left to right the abundances of the species discussed in this work as a function of log $g$ in NGC 6633. The symbols are the same as in Fig. 3.

if NLTE effects were taken into account in the abundance analysis. Nordlander & Lind (2017) predict for Al a correction for dwarf and giant stars of $\sim -0.1$ dex at solar metallicity for the line at 669.6 nm. For Mg, we do not expect NLTE effects to have a strong influence on the abundances. Zhang et al. (2017) calculate corrections of the order of $\pm 0.01$ dex for stellar parameters similar to our NGC 6633 sample. For the same stars, Zhang et al. (2016) predict corrections of the order of $-0.03$ (RGB) and 0.00 dex (MS) for Si. The latter, however, has $\Delta[X/H] \sim 3 \times \text{err}_{\Delta[X/H]}$, i.e. the offset is relatively large and cannot be explained by NLTE effects. Since also in the case of M67, we found that the offset in Si between the upper MS and RGB is larger than predicted by the models, this could mean that indeed for Si there is a bias in the analysis of dwarf and giant stars.

5.4 APOGEE DR14

The recent fourteenth data release of the Apache Point Observatory Galactic Evolution Experiment (hereafter APOGEE DR14; see Abolfathi et al. 2017; Majewski et al. 2017) contains very important
results concerning the abundances of M67 stars. In APOGEE DR14, stars in every evolutionary stage of M67 have been observed and analysed, from the MS to the RC. We decided to be as conservative as possible in the choice of the stars to be taken into consideration and we selected only those with STARFLAG, ASPCAPFLAG, and the ELMFLAG of the element under study equal to zero. By doing so, we aim at excluding as many possible biases due to unreliable results as possible.

APOGEE DR14 contains the abundances determined by the APOGEE Stellar Parameters and Chemical Abundances Pipeline (ASPCAP) (see Holtszman et al. 2015; García Pérez et al. 2016) as well as calibrated abundances. These are calculated under the assumption that abundances of open cluster members should be homogeneous and that therefore any trend with temperature must be corrected for. Since for our purposes it is important to take into consideration any trend of the chemical abundances as a function of temperature, we decided to use the uncalibrated abundances. We present the results in the form [X/H]. For the elements that were calculated as [X/M], we add the uncalibrated [M/H] of the star. The error bars only represent the errors on the fit of the uncalibrated abundances presented in the APOGEE DR14 catalogue (for the uncalibrated [M/H] no errors are given). These are very small and are not to be considered realistic errors.

Fig. 5 shows the CMD of the sample (not corrected for reddening) selected after a membership analysis based on radial velocity, PM, photometry and metallicity, and after all stars with the flags listed above not equal to zero were excluded. The stars are colour coded based on their iron abundance. It is already clear from this plot that [Fe/H] on the TO is lower than on the RGB and on the RC. Since no calibrated log g is available for dwarf stars in APOGEE DR14, we plotted in Fig. 6 the abundances of several species as a function of the effective temperature together with the models from Michaud et al. (2004). Several of the abundances obtained by APOGEE DR14 show offsets between TO and RGB similar to those predicted by the models, although, as in GES iDR5, for some elements large spreads as well as offsets in comparison to the models are present. This is nevertheless an interesting result for our study, since it shows that abundances computed with a completely independent method from infrared rather than optical spectra yield similar trends to those obtained within GES iDR5.

During the refereeing process, the work by Souto et al. (2018) appeared, in which the authors analyse the APOGEE spectra of eight M67 members in different evolutionary stages from the MS to the RGB. They derive abundances of 14 elements for these stars

<table>
<thead>
<tr>
<th>X</th>
<th>[X/H]_{MS}</th>
<th>σ_{MS}</th>
<th>[X/H]_{RGB}</th>
<th>σ_{RGB}</th>
<th>Δ[X/H]</th>
<th>err Δ[X/H]</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>0.072</td>
<td>0.109</td>
<td>-0.200</td>
<td>0.044</td>
<td>-0.272</td>
<td>0.118</td>
</tr>
<tr>
<td>Na</td>
<td>-0.128</td>
<td>0.040</td>
<td>0.150</td>
<td>0.017</td>
<td>0.278</td>
<td>0.044</td>
</tr>
<tr>
<td>Mg</td>
<td>-0.108</td>
<td>0.027</td>
<td>-0.047</td>
<td>0.035</td>
<td>0.061</td>
<td>0.044</td>
</tr>
<tr>
<td>Al</td>
<td>-0.114</td>
<td>0.047</td>
<td>-0.037</td>
<td>0.032</td>
<td>0.077</td>
<td>0.057</td>
</tr>
<tr>
<td>Si</td>
<td>-0.042</td>
<td>0.042</td>
<td>0.097</td>
<td>0.025</td>
<td>0.139</td>
<td>0.049</td>
</tr>
<tr>
<td>Ca</td>
<td>0.002</td>
<td>0.068</td>
<td>-0.017</td>
<td>0.025</td>
<td>-0.019</td>
<td>0.073</td>
</tr>
<tr>
<td>Ti</td>
<td>-0.052</td>
<td>0.067</td>
<td>0.123</td>
<td>0.038</td>
<td>0.071</td>
<td>0.077</td>
</tr>
<tr>
<td>Cr</td>
<td>-0.032</td>
<td>0.050</td>
<td>-0.087</td>
<td>0.032</td>
<td>-0.055</td>
<td>0.059</td>
</tr>
<tr>
<td>Mn</td>
<td>-0.078</td>
<td>0.063</td>
<td>-0.113</td>
<td>0.035</td>
<td>-0.035</td>
<td>0.072</td>
</tr>
<tr>
<td>Fe</td>
<td>-0.086</td>
<td>0.029</td>
<td>-0.040</td>
<td>0.027</td>
<td>0.046</td>
<td>0.039</td>
</tr>
<tr>
<td>Ni</td>
<td>-0.124</td>
<td>0.052</td>
<td>-0.093</td>
<td>0.023</td>
<td>0.031</td>
<td>0.057</td>
</tr>
</tbody>
</table>

and come to a similar conclusion as our study, i.e. that diffusion effects seem to be present in the member stars of M67.

6 SUMMARY

We studied the surface chemical composition of member stars in the old open cluster M67 analysed by the Gaia-ESO Survey, searching for evidence of atomic diffusion processes. We compared the abundances of C, O, Mg, Al, Na, Si, Ca, Ti, Cr, Mn, Fe, and Ni with different stellar evolutionary models calculated by Michaud et al. (2004) for the age and metallicity of M67 and found them to be roughly consistent with each other. Our results support the findings of Önehag et al. (2014), although the inclusion of three RGB stars compared to the sample of Önehag et al. (2014) renders the results more conclusive, since in RGB stars the initial surface abundances are essentially restored, after the effects of atomic diffusion have been cancelled by convection. Furthermore, the predicted abundance variations between upper MS and RGB are larger than between upper MS and TO/early SGB and thus, at least in theory, easier to measure. Also, Casey (2016) found a variation in metallicity [Fe/H] of ~0.05 dex between TO and SGB/low-RGB stars of M67 from lower resolution spectra. Recently, Souto et al. (2018) published similar results regarding a sample of eight M67 stars that hint at the presence of atomic diffusion effects in M67. Although we find indications of ongoing diffusion processes, it is not possible to state whether the models with or without turbulent diffusion better represent the data, given the spread and the errors on the measured abundances on the upper MS and TO.

We have also shown that the star S806 systematically presents higher surface abundances than its cluster companions. We suggest as a possible explanation that this star might be part of a binary system and has undergone accretion of expelled material from a putatively evolved more massive companion.

We have investigated the abundances in stars of the MS and RGB/RC of NGC 6633, a cluster young enough that we do not expect any signs of diffusion effects in the stars included in GES iDR5. As expected, for most elements the abundances of the two groups are consistent with each other within one sigma, except for few light elements of the Na group. For Na, the offset can be explained by mixing processes and NLTE effects, while at least for
Si the measured abundance difference between dwarfs and giants might be enhanced due to analysis effects. The latter may also explain the large Si offset measured in M67 (Fig. 2).

We found that the latest APOGEE data release DR14 presents for the stars of M67 similar trends to those measured in GES iDR5. Nevertheless, the large scatter and offsets affecting some elements may be a combination of true abundance variations and uncertainties in the analysis that are difficult to disentangle at the present time. This calls for further refinements in the determination of abundances from observed spectra.

The detection of true variations in the surface abundances of stars due to stellar evolutionary effects has strong implications for the field of Galactic archaeology, since it puts a constraint on the precision achievable with chemical tagging of the order of ∼0.1 dex, similar to what was indicated in Dotter et al. (2017). As a consequence, future studies will need to rethink chemical tagging methods taking into account stellar evolution or they will be applicable only to stars in the same evolutionary stage.

ACKNOWLEDGEMENTS

This work was supported by Sonderforschungsbereich SFB 881 ‘The Milky Way System’ (subproject B5) of the German Research Foundation (DFG). AB acknowledges support from the SFB 881 visitor program. CBM thanks Elisabetta Caffau for fruitful discussions and Don VandenBerg for providing the isochrones shown in Fig 1. The authors would like to thank the anonymous referee for the constructive comments that helped in improving the present work.

MTC acknowledges the financial support from the Spanish Ministerio de Economía y Competitividad, through grant AYA2016-75931. AD and GT acknowledge support by the Research Council of Lithuania (MIP-082/2015). UH acknowledges support from the Swedish National Space Board (SNSB/Rymdstyrelsen). TB was supported by the project grant ‘The New Milky’ from the Knut and Alice Wallenberg foundation. RS acknowledges support from the Polish Ministry of Science and Higher Education. SGS and VA acknowledge the support by Fundação para a Ciência e Tecnologia (FCT) through national funds and a research grant (project ref. UID/FIS/04434/2013, and PTDC/FIS-AST/7073/2014). SGS also acknowledges the support from FCT through Investigador FCT contract of reference IF/00028/2014 and POPH/FSE (EC) by FEDER funding through the program ‘Programa Operacional de Factores de Competitividade – COMPETE’.

VA acknowledges the support from FCT through Investigador FCT contract IF/00650/2015/CP1273/CT0001. EJA acknowledges
Evidence of atomic diffusion in M67? 435

partial support from the Spanish Ministry for Economy and Competitiveness and FEDER funds through grant AYA2013-40611-P. ARC is supported through an Australian Research Council Discovery Project under grant DP160100637. CL thanks the Swiss National Science Foundation for supporting this research through the Ambizione grant number PZ00P2_168065. AK acknowledges support from the Swedish National Space Board (SNSB). XF support from the Millennium Science Initiative (Chilean Ministry of Economy).

Based on data products from observations made with ESO Telescopes at the La Silla Paranal Observatory under programme ID 188.B-3002. These data products have been processed by the Cambridge Astronomy Survey Unit (CASU) at the Institute for Astronomy, University of Edinburgh, which is funded by the UK Science and Technology Facilities Council. This work was partly supported by the European Union FP7 programme through the HSOY catalogue, effective temperatures and gravities derived within GES with the respective errors are listed. In Table A2, the stars selected as members of M67 after our membership analysis. Besides GES-ID, RA, and Dec., the radial velocities, PMs from the HSOY catalogue, effective temperatures and gravities derived within GES with the respective errors are listed. In Table A2, the stars selected as members of M67 after our membership analysis.

REFERENCES
García Pérez A. E. et al., 2016, AJ, 151, 144
Gilmore G. et al., 2012, The Messenger, 147, 25
Pasquini L. et al., 2002, The Messenger, 110, 1
Skrutskie M. F. et al., 2006, AJ, 131, 1163
Yong D., Carney B. W., Teixera de Almeida M. L., 2005, AJ, 130, 597

APPENDIX A: ADDITIONAL MATERIAL

In Table A1, we present a summary of the main parameters for the 15 stars selected as members of M67 after our membership analysis. Besides GES-ID, RA, and Dec., the radial velocities, PMs from the HSOY catalogue, effective temperatures and gravities derived within GES with the respective errors are listed. In Table A2, the
abundances of the different elements are summarized for each of the 15 stars. Fig. A1 shows the evolution of different surface abundances as a function of log g for two models with and without turbulence representing a star of mass 1.35 M⊙. The model with turbulence did not reach the same age as the one without turbulence and hence is not as evolved as the three giants in our sample. The plot aims to demonstrate that once the RGB is reached, both models present the

Evidence of atomic diffusion in M67?

Figure A1. Comparison of the surface abundances of two different models with (solid black line) and without (dashed black line) turbulence for a star of 1.35 M\(_{\odot}\) as a function of log \(g\).

same surface abundances. This is evident, since after log \(g\) \(~\sim\) 3.6 both models converge.

1. Astronomisches Rechen-Institut, Zentrum für Astronomie der Universität Heidelberg, Mönchhofstr 12-14, D-69120 Heidelberg, Germany
2. Département de physique, Université de Montréal, Montréal, Québec H3C 3J7, Canada
3. Astrophysics Research Institute, Liverpool John Moores University, 146 Brownlow Hill, Liverpool L3 5RF, UK
4. INAF – Osservatorio di Astrofisica e Scienze dello Spazio, via Gobetti 93/3, I-40129 Bologna, Italy
5. INAF – Osservatorio Astrofisico di Arcetri, Largo E. Fermi 5, I-50125 Firenze, Italy
6. Instituto de Astrofísica e Ciências do Espaço, Universidade do Porto, CAUP, Rua das Estrelas, P-4150-762 Porto, Portugal
7. Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA
8. Institute of Theoretical Physics and Astronomy, Vilnius University, Saulėtekio av. 3, LT-10257 Vilnius, Lithuania
9. Dipartimento di Fisica & Astronomia, Università degli Studi di Bologna, via Gobetti 93/2, I-40129 Bologna, Italy
10. School of Physics, University of New South Wales, Sydney NSW 2052, Australia
11. Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
12. Instituto de Astrofísica de Andalucía, CSIC, Glorieta de la Astronomía, s/n, E-18008 Granada, Spain
13. Lund Observatory, Department of Astronomy and Theoretical Physics, Box 43, SE-221 00 Lund, Sweden
14. INAF – Osservatorio Astronomico di Palermo, Piazza del Parlamento 1, I-90134 Palermo, Italy
15. Department of Physics, McWilliams Center for Cosmology, Carnegie Mellon University, 5000 Forbes Avenue, Pittsburgh, PA 15213, USA
16. Department of Physics and Astronomy, Uppsala University, Box 516, SE-751 20 Uppsala, Sweden
17. Dipartimento di Fisica e Astronomia, Sezione Astrofisica, Università di Catania, via S. Sofia 78, I-95123 Catania, Italy
18. Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, ul. Bartycka 18, PL-00-716 Warsaw, Poland
19. Instituto de Física y Astronomía, Facultad de Ciencias, Universidad de Valparaíso, Av. Gran Bretaña 1111, Valparaíso, Chile
20. Núcleo Milenio Formación Planetaria - NPF, Universidad de Valparaíso, Av. Gran Bretaña 1111, Valparaíso, Chile
21. Dipartimento di Fisica e Astronomia, Università di Padova, Vicolo dell’Osservatorio 3, I-35122 Padova, Italy
22. School of Physics and Astronomy, Monash University, Clayton 3800, Victoria, Australia
23. Faculty of Information Technology, Monash University, Clayton 3800, Victoria, Australia
24. Departamento de Didáctica, Universidad de Cádiz, E-11519 Puerto Real, Cádiz, Spain
This paper has been typeset from a \TeX/\LaTeX\ file prepared by the author.